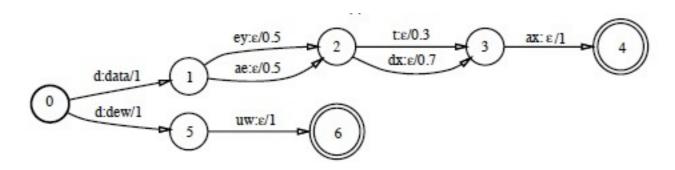
Language Technology

CUNY Graduate Center Fall 2014

Unit 3: Tree Models

Lectures 9-11: Context-Free Grammars and Parsing

required hard optional



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Big Picture

- only 2 ideas in this course: Noisy-Channel and Viterbi (DP)
- we have already covered...
 - sequence models (WFSAs, WFSTs, HMMs)
 - decoding (Viterbi Algorithm)
 - supervised training (counting, smoothing)
- in this unit we'll look beyond sequences, and cover...
 - tree models (prob context-free grammars and extensions)
 - decoding ("parsing", CKY Algorithm)
 - supervised training (lexicalization, history-annotation, ...)

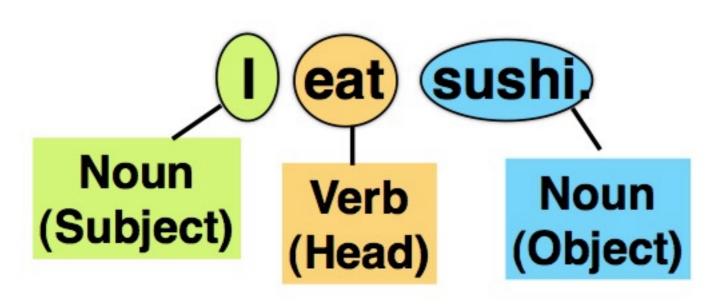
Limitations of Sequence Models

can you write an FSA/FST for the following?

```
• \{(a^n, b^n)\} \{(a^{2n}, b^n)\}
```

- \bullet { $a^n b^n$ }
- { w w^R }
- { (w, w^R) }
- does it matter to human languages?
 - [The woman saw the boy [that heard the man [that left]]].
 - [The claim [that the house [he bought] is valuable] is wrong].
 - but humans can't really process infinite recursions... stack overflow!

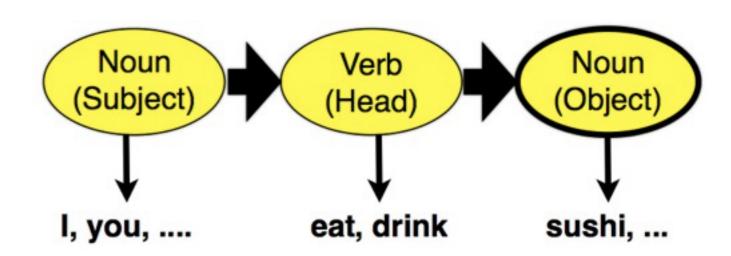
Let's try to write a grammar...



(courtesy of Julia Hockenmaier)

- let's take a closer look...
- we'll try our best to represent English in a FSA...
- basic sentence structure: N,V, N

Subject-Verb-Object



- compose it with a lexicon, and we get an HMM
- so far so good

CS 562 - CFGs and Parsing

(Recursive) Adjectives

(courtesy of Julia Hockenmaier)

the ball the big ball the big, red ball the big, red, heavy ball

- then add Adjectives, which modify Nouns
- the number of modifiers/adjuncts can be unlimited.
- how about no determiner before noun? "play tennis"

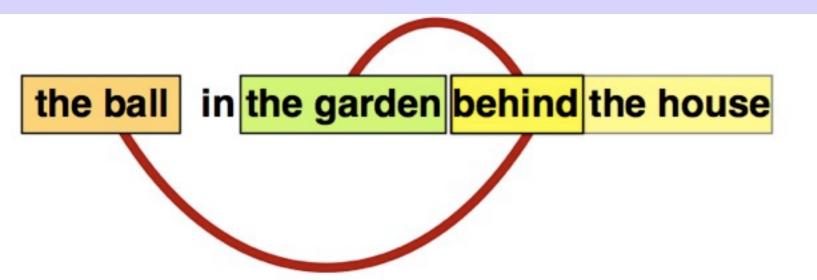
Recursive PPs

(courtesy of Julia Hockenmaier)

the ball in the garden the ball in the garden behind the house the ball in the garden behind the house near the school ...

- recursion can be more complex
- but we can still model it with FSAs!
- so why bother to go beyond finite-state?

FSAs can't go hierarchical!



(courtesy of Julia Hockenmaier)

- but sentences have a hierarchical structure!
 - so that we can infer the meaning
 - we need not only strings, but also trees
- FSAs are flat, and can only do tail recursions (i.e., loops)
- but we need real (branching) recursions for languages

FSAs can't do Center Embedding

The mouse ate the corn. (courtesy of Julia Hockenmaier)

The mouse that the snake ate ate the corn.

The mouse that the snake that the hawk ate ate ate the corn.

. . . .

VS.

The claim that the house he bought was valuable was wrong.

VS

I saw the ball in the garden behind the house near the school.

- in theory, these infinite recursions are still grammatical
 - competence (grammatical knowledge)
- in practice, studies show that English has a limit of 3
 - performance (processing and memory limitations)
- FSAs can model finite embeddings, but very inconvenient.

How about Recursive FSAs?

- problem of FSAs: only tail recursions, no branching recursions
 - can't represent hierarchical structures (trees)
 - can't generate center-embedded strings
- is there a simple way to improve it?
 - recursive transition networks (RTNs)

Context-Free Grammars

 \circ S \rightarrow NP VP

• N → {ball, garden, house, sushi }

- NP → Det N
- \bullet **P** \rightarrow {in, behind, with}
- \bullet NP \rightarrow NP PP
- V → ...

 \bullet PP \rightarrow P NP

• Det → ...

- \bullet VP \rightarrow V NP
- \bullet VP \rightarrow VP PP

Context-Free Grammars

A CFG is a 4-tuple $\langle N, \Sigma, R, S \rangle$

A set of nonterminals N

```
(e.g. N = \{S, NP, VP, PP, Noun, Verb, ....\})
```

A set of terminals Σ

```
(e.g. \Sigma = \{I, you, he, eat, drink, sushi, ball, \})
```

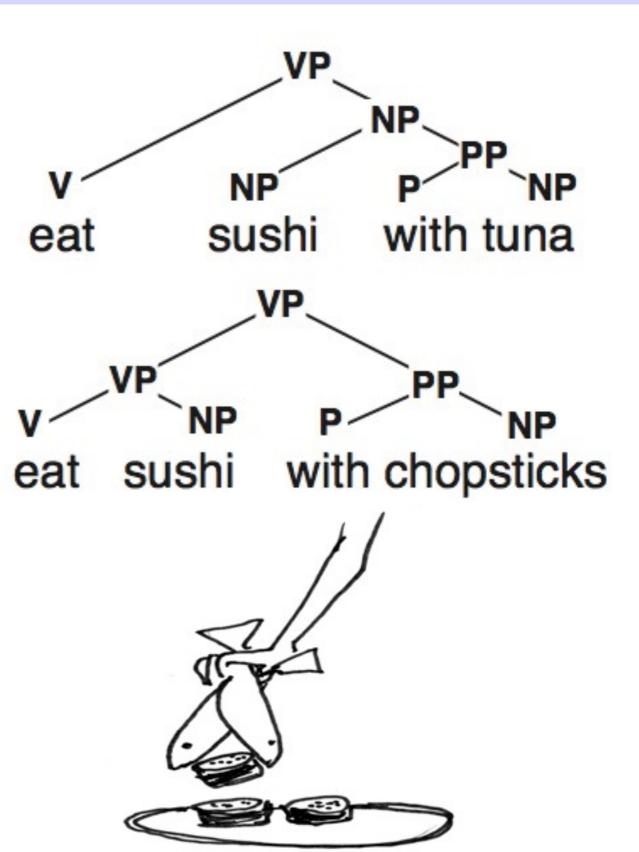
A set of rules R

```
R \subseteq \{A \rightarrow \beta \text{ with left-hand-side (LHS)} \mid A \in N \}
and right-hand-side (RHS) \beta \in (N \cup \Sigma)^* \}
```

A start symbol S (sentence)

Parse Trees

- **N** → {*sushi, tuna*}
- **P** → {with}
- **V** → {*eat*}
- $NP \rightarrow N$
- \bullet NP \rightarrow NP PP
- PP→P NP
- VP→V NP
- VP→VP PP



CFGs for Center-Embedding

The mouse ate the corn.

The mouse that the snake ate ate the corn.

The mouse that the snake that the hawk ate ate the corn.

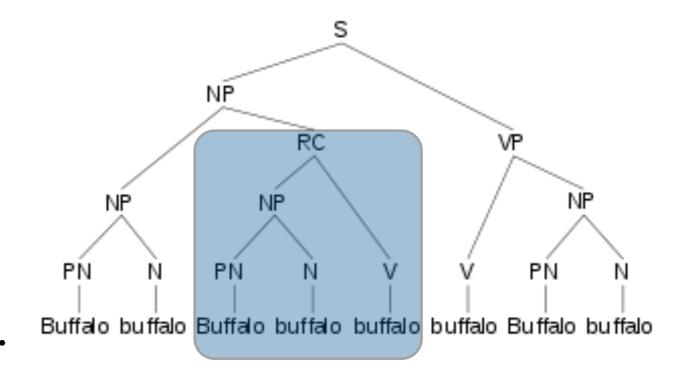
. . . .

- can you also do { aⁿ bⁿ cⁿ } ? or { w w^R w } ?
- what's the limitation of CFGs?
- CFG for center-embedded clauses:
 - S \rightarrow NP ate NP; NP \rightarrow NP RC; RC \rightarrow that NP ate

Review

- write a CFG for...
 - $\{a^m b^n c^n d^m\}$
 - $\{ a^m b^n c^{3m+2n} \}$

 - buffalo buffalo buffalo ...



- write an FST or synchronous CFG for...
 - $\bullet \{ (w, w^R) \} \qquad \{ (a^n, b^n) \}$
- HW3: including p(eprons) is wrong
- HW4: using carmel to test your own code

Chomsky Hierarchy

	Language	Automata	Parsing complexity	Dependencies
Type 3	Regular	Finite-state	linear	adjacent words
Type 2	Context-Free	Pushdown	cubic	nested
Type 1	Context- sensitive	Linear Bounded	exponential	
Type 0	Recursively	Turing machine		

Constituents, Heads, Dependents

There are different kinds of constituents:

Noun phrases: the man, a girl with glasses, Illinois

Prepositional phrases: with glasses, in the garden

Verb phrases: eat sushi, sleep, sleep soundly

Every phrase has a head:

Noun phrases: the man, a girl with glasses, Illinois

Prepositional phrases: with glasses, in the garden

Verb phrases: eat sushi, sleep, sleep soundly

The other parts are its **dependents**.

Dependents are either arguments or adjuncts

Constituency Test

He talks [in class].

Substitution test:

Can α be replaced by a single word? He talks [there].

Movement test:

Can α be moved around in the sentence? [In class], he talks.

Answer test:

Can α be the answer to a question? Where does he talk? - [In class].

how about "there is" or "I do"?

Arguments and Adjuncts

arguments are obligatory

Words subcategorize for specific sets of arguments:

Transitive verbs (sbj + obj): [John] likes [Mary]

All arguments have to be present:

*[John] likes. *likes [Mary].

No argument can be occupied multiple times:

*[John] [Peter] likes [Ann] [Mary].

Words can have multiple subcat frames:

Transitive eat (sbj + obj): [John] eats [sushi]. Intransitive eat (sbj): [John] eats.

Arguments and Adjuncts

adjuncts are optional

Adverbs, PPs and adjectives can be adjuncts:

Adverbs: John runs [fast].

a [very] heavy book.

PPs: John runs [in the gym].

the book [on the table]

Adjectives: a [heavy] book

There can be an arbitrary number of adjuncts

John saw Mary.
John saw Mary [yesterday].
John saw Mary [yesterday] [in town]
John saw Mary [yesterday] [in town] [during lunch]
[Perhaps] John saw Mary [yesterday] [in town] [during lunch]

Noun Phrases (NPs)

Simple NPs:

[He] sleeps. (pronoun)

[John] sleeps. (proper name)

[A student] sleeps. (determiner + noun)

Complex NPs:

```
[A tall student] sleeps. (det + adj + noun)
[The student in the back] sleeps. (NP + PP)
[The student who likes MTV] sleeps. (NP + Relative
Clause)
```

The NP Fragment

```
NP → Pronoun
NP → ProperName
NP → Det Noun
Det \rightarrow {a, the, every}
Pronoun → {he, she,...}
ProperName → {John, Mary,...}
Noun → AdjP Noun
Noun \rightarrow N
NP \rightarrow NP PP
NP → NP RelClause
```

ADJPs and PPs

```
AdjP → Adj
AdjP → Adv AdjP
Adj \rightarrow {big, small, red,...}
Adv \rightarrow \{very, really,...\}
PP \rightarrow P NP
P \rightarrow \{with, in, above,...\}
```

Verb Phrase (VP)

```
He [eats].
He [eats sushi].
He [gives John sushi].
He [eats sushi with chopsticks].
```

 $VP \rightarrow V$ $VP \rightarrow V NP$ $VP \rightarrow V NP PP$ $VP \rightarrow VP PP$

 $V \rightarrow \{eats, sleeps gives,...\}$

VPs redefined

```
He [eats].
He [eats sushi].
He [gives John sushi].
He [eats sushi with chopsticks].
```

```
VP → V intrans
VP \rightarrow V \text{ trans } NP
VP → V ditrans NP NP
VP \rightarrow VP PP
V_intrans → {eats, sleeps}
V_trans → {eats}
V_trans → {gives}
```

Sentences

```
[He eats sushi].
[Sometimes, he eats sushi].
[In Japan, he eats sushi].
```

```
S \rightarrow NPVP
```

 $S \rightarrow AdvPS$

 $S \rightarrow PPS$

```
He says [he eats sushi].
VP \rightarrow V_{comp} S
V_comp → {says, think, believes}
```

Sentence Redefined

```
[He eats sushi]. 🗸
*[I eats sushi]. ???
*[They eats sushi]. ????
S → NP.3sg VP.3sg
S → NP.1sg VP.1sg
S → NP.3pl VP.3pl
We need features to capture agreement:
  (number, person, case,...)
```

Probabilistic CFG

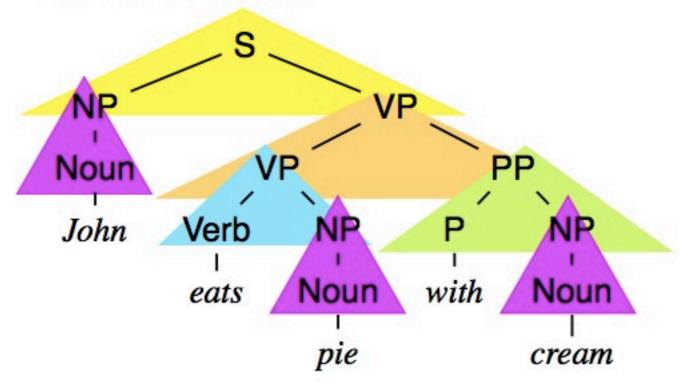
- normalization
 - sum_{\beta} $p(A \rightarrow \beta) = I$

- what's the most likely tree?
 - in finite-state world,
- what's the most likely string
- \rightarrow NP VP 0.8 0.2 \rightarrow S conj S \rightarrow Noun 0.2 NP 0.4 NP \rightarrow Det Noun 0.2 $NP \rightarrow NP PP$ $NP \rightarrow NP \text{ conj } NP$ 0.2 0.4 VP ightarrow Verb 0.3 $exttt{VP} o exttt{Verb} exttt{NP}$ 0.1 VP \rightarrow Verb NP NP 0.2 $VP \rightarrow VP PP$ 1.0 $PP \rightarrow P NP$
- given string w, what's the most likely tree for w
 - this is called "parsing" (like decoding)

Probability of a tree

The probability of a tree τ is the product of the probabilities

of all its rules:



$$P(\tau) = \frac{0.8 \times 0.3 \times 0.2 \times 1.0 \times 0.2^{3}}{0.00384}$$

S	\rightarrow NP VP	0.8
S	ightarrow S conj S	0.2
NP	\rightarrow Noun	0.2
NP	\rightarrow Det Noun	0.4
NP	\rightarrow NP PP	0.2
NP	ightarrow NP conj NP	0.2
VP	ightarrow Verb	0.4
VP	ightarrow Verb NP	0.3
VP	ightarrow Verb NP NP	0.1
VP	\rightarrow VP PP	0.2
PP	\rightarrow P NP	1.0

Most likely tree given string

- parsing is to search for the best tree t* that:
 - $t^* = argmax_t p(t | w) = argmax_t p(t) p(w | t)$
 - = $argmax_{t: yield(t)=w} p(t)$
 - analogous to HMM decoding
- is it related to "intersection" or "composition" in FSTs?

CKY Algorithm

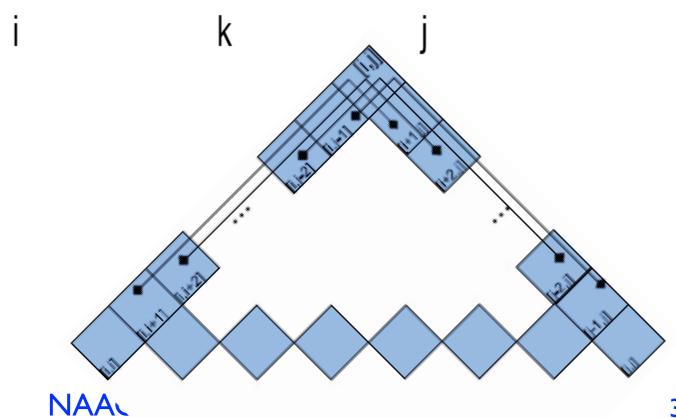
- For each diff (<= n)</p>
 - For each i (<= n)</p>
 - For each rule X → Y Z
 - For each split point k

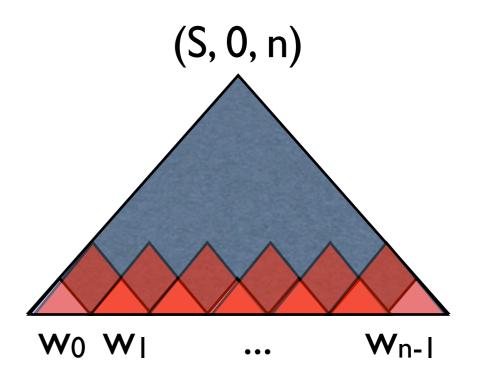
```
score[X][i][j] = max score[X][i][j],
```

score(X->YZ) *

score[Y][i][k]

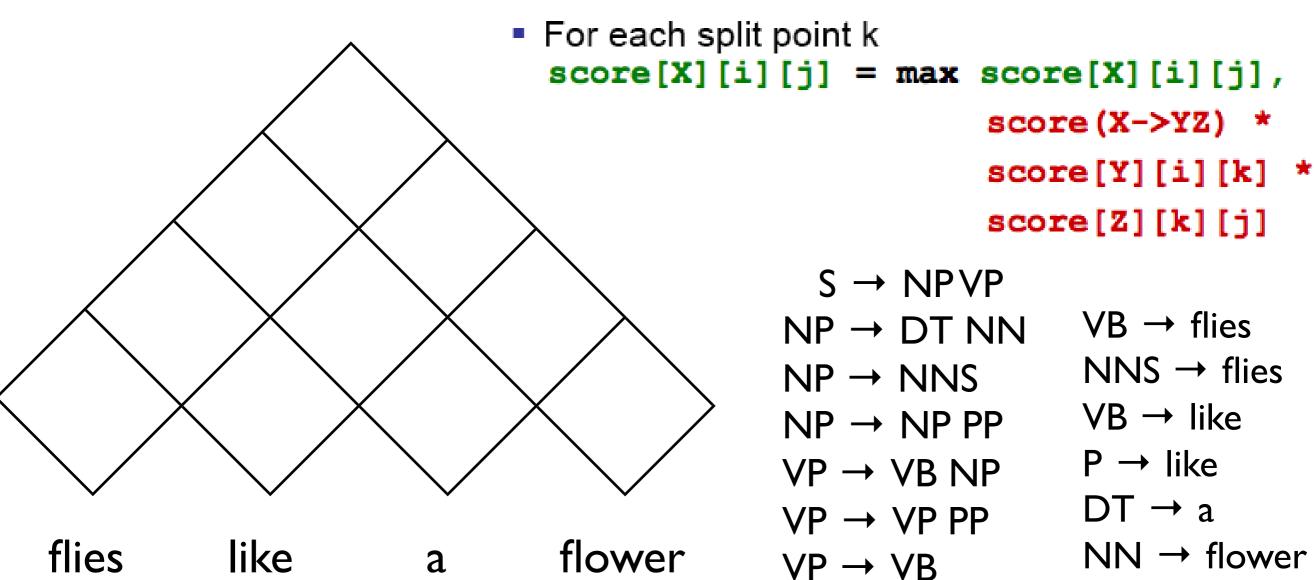
score[Z][k][j]





CKY Algorithm

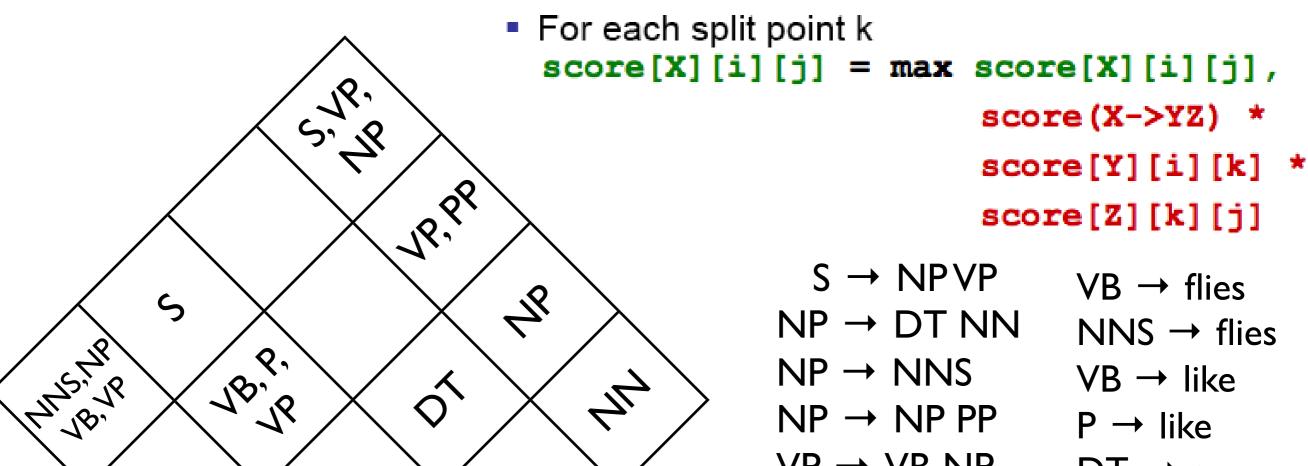
- For each diff (<= n)</p>
 - For each i (<= n)</p>
 - For each rule X → Y Z



 $PP \rightarrow P NP$

CKY Algorithm

- For each diff (<= n)</p>
 - For each i (<= n)</p>
 - For each rule X → Y Z



flies

like

flower

 $VB \rightarrow flies$ NNS → flies VB → like $P \rightarrow like$ $VP \rightarrow VB NP$ $DT \rightarrow a$ $VP \rightarrow VP PP$ NN → flower $VP \rightarrow VB$ $S \rightarrow VP$ $PP \rightarrow P NP$

CKY Example

Input: POS-tagged sentence

John_N eats_V pie_N with_P cream_N

John		ea	ats	ķ	oie	with	CI	ream	
N	NP 0.2		S 0.2*0.4		S 0.2*0.08		S 0.2*0.0024*0.8		John
		٧	VP 0.4	C	VP 0.3*0.2		max(VP 0.008*0.2, 0*0.2*0.2)	eats
				N	NP 0.2			NP 2*0.2*0.2	pie
						Р		PP 1*0.2	with
							N	NP 0.2	cream

S	\rightarrow NP VP	0.8
S	\rightarrow S conj S	0.2
NP	\rightarrow Noun	0.2
NP	\rightarrow Det Noun	0.4
NP	\rightarrow NP PP	0.2
NP	ightarrow NP conj NP	0.2
VP	ightarrow Verb	0.4
VP	ightarrow Verb NP	0.3
VP	ightarrow Verb NP NP	0.1
VP	\rightarrow VP PP	0.2
PP	\rightarrow P NP	1.0

Chomsky Normal Form

- wait! how can you assume a CFG is binary-branching?
- well, we can always convert a CFG into Chomsky-Normal Form (CNF)
 - \bullet A \rightarrow B C
 - \bullet A \rightarrow a
- how to deal with epsilon-removal?
- how to do it with PCFG?

What if we don't do CNF...

Earley's algorithm (dotted rules, internal binarization)

Item form:
$$[A, i, j]$$

Axioms:
$$[A, i, i+1]$$
 $A \rightarrow w_{i+1}$

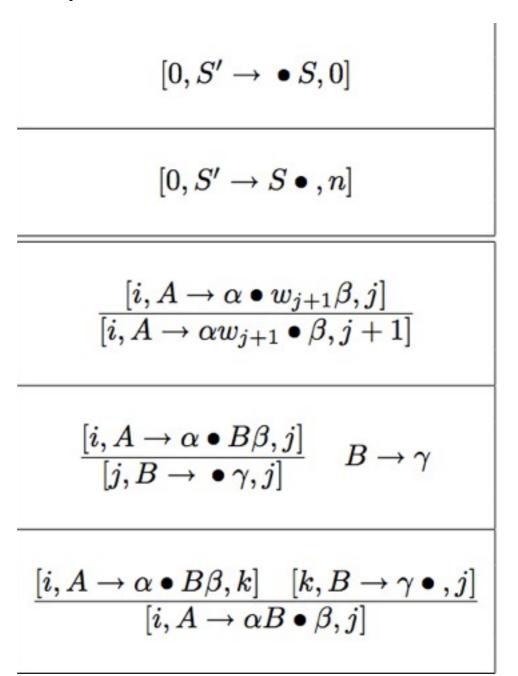
Goals:
$$[S, 0, n]$$

Inference rules:
$$\frac{[B,i,j] \quad [C,j,k]}{[A,i,k]} \quad A \to B \ C$$

CKY deductive system

What if we don't do CNF...

Earley's algorithm (dotted rules, internal binarization)



initial

goal

scan

predict

complete

Earley (1970) deductive system

Earley Algorithm

- why complete must be first?
- how do you extend it for PCFG?

```
procedure EARLEYPARSER(w_{1..n})
      addToChart(\langle TOP \rightarrow \bullet S, [0,0] \rangle)
     for all \langle rule, [k,i] \rangle \in \text{chart do}
           if rule matches X \rightarrow \gamma \bullet then
                                                                                                            COMPLETE X
                  for all (Y \to \alpha \bullet X\beta, [j,k]) \in \text{chart do}
                        addToChart(\langle Y \rightarrow \alpha X \bullet \beta, [j,i] \rangle)
            else if rule matches X \to \alpha \bullet Y\beta then
                                                                                                                ▶ PREDICT Y
                  for all Y \to \gamma \in \text{RULES do}
                        addToChart(\langle Y \rightarrow \bullet \gamma, [i, i] \rangle)
            else if rule matches X \to \alpha \bullet t\beta, and \langle t, w_i \rangle \in \text{LEX then}
                                                                                                                    ▷ SCAN Wi
                  addToChart(\langle X \to \alpha t \bullet \beta, [k, i+1] \rangle)
           if s=\langle TOP \rightarrow S \bullet, [0,n] \rangle \in \text{chart then return } s
            else fail
```

Parsing as Deduction

$$(B, i, k): a \qquad (C, k, j): b$$

$$A \rightarrow B C$$

$$(A, i, j): a \times b \times Pr(A \rightarrow B C)$$

Parsing as Intersection

$$(B, i, k): a \qquad (C, k, j): b$$

$$A \rightarrow B C$$

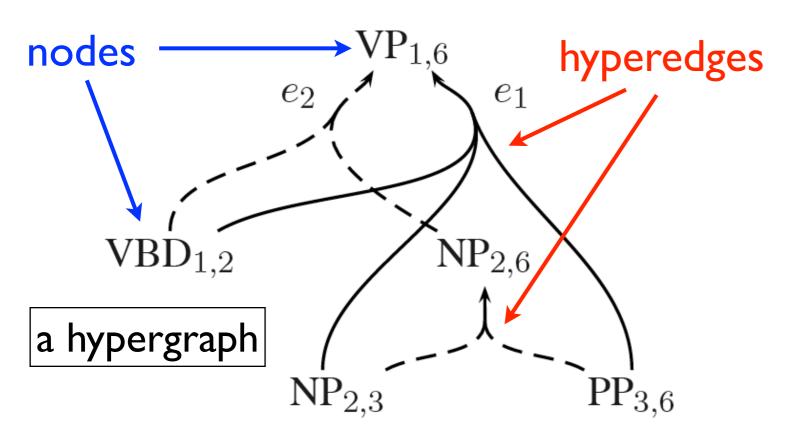
$$(A, i, j): a \times b \times Pr(A \rightarrow B C)$$

- intersection between a CFG G and an FSA D:
 - define L(G) to be the set of strings (i.e., yields) G generates
 - define $L(G \cap D) = L(G) \cap L(D)$
 - what does this new language generate??
 - what does the new grammar look like?
- what about CFG ∩ CFG ?

Parsing as Composition

Packed Forests

- a compact representation of many parses
 - by sharing common sub-derivations
 - polynomial-space encoding of exponentially large set



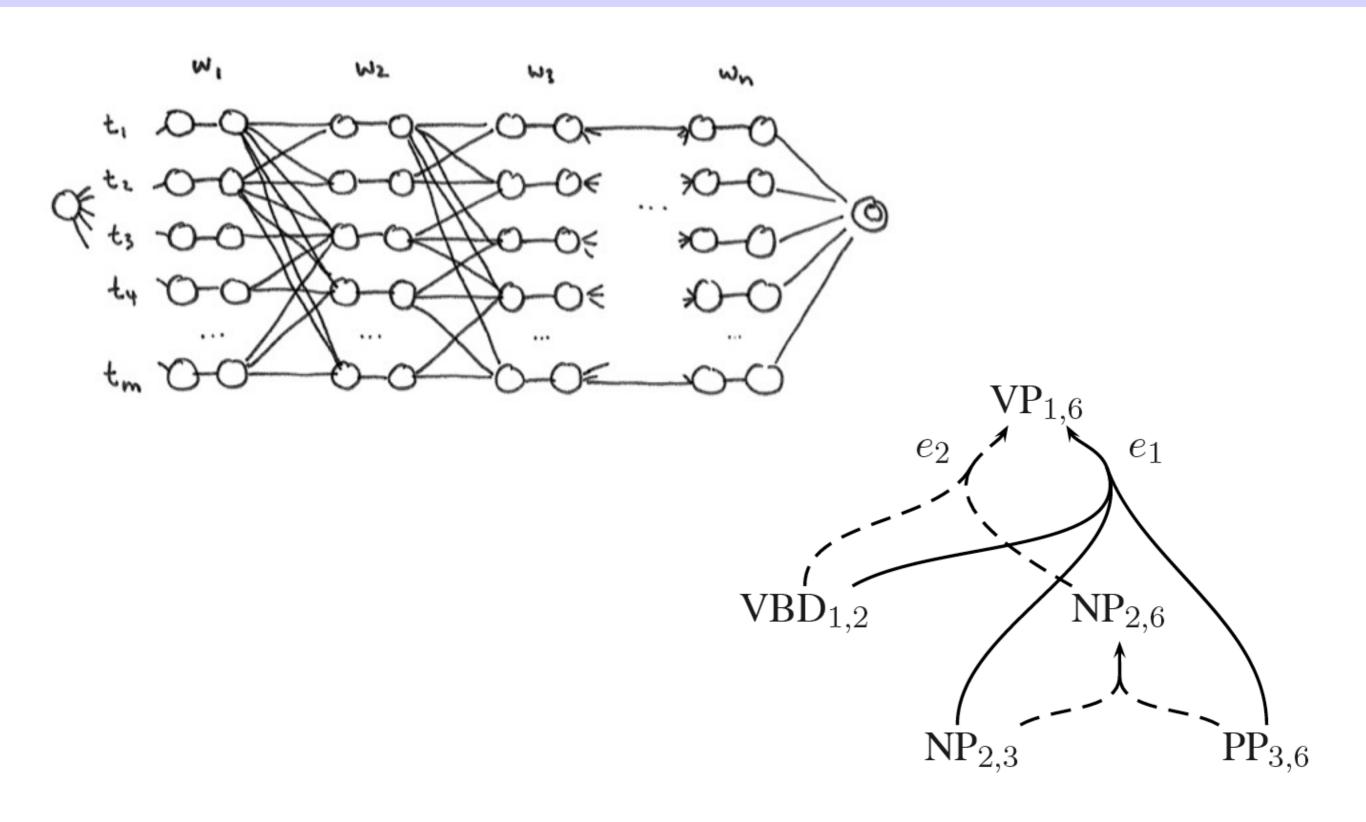


$$\frac{\text{VBD}_{1,2} \quad \text{NP}_{2,3} \quad \text{PP}_{3,6}}{\text{VP}_{1,6}}$$

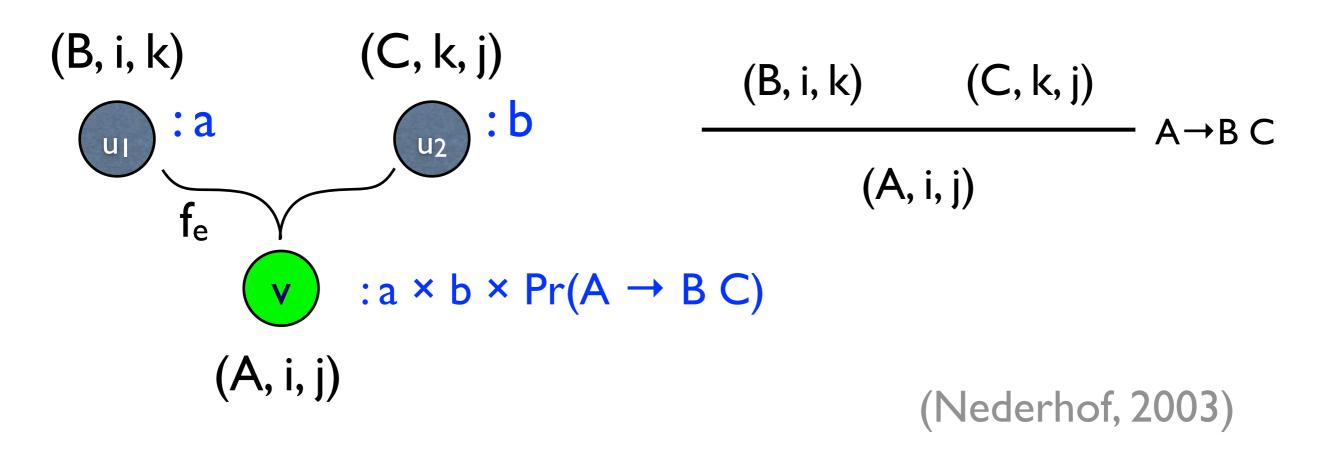
0 l saw 2 him 3 with 4 a 5 mirror 6

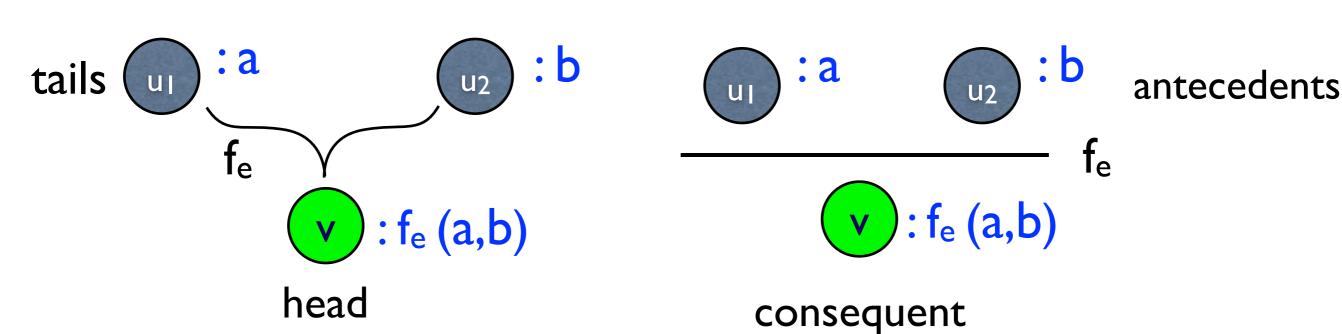
(Klein and Manning, 2001; Huang and Chiang, 2005)

Lattice vs. Forest



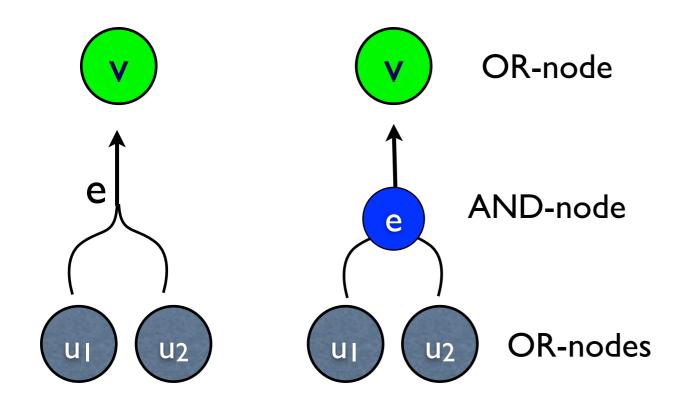
Forest and Deduction





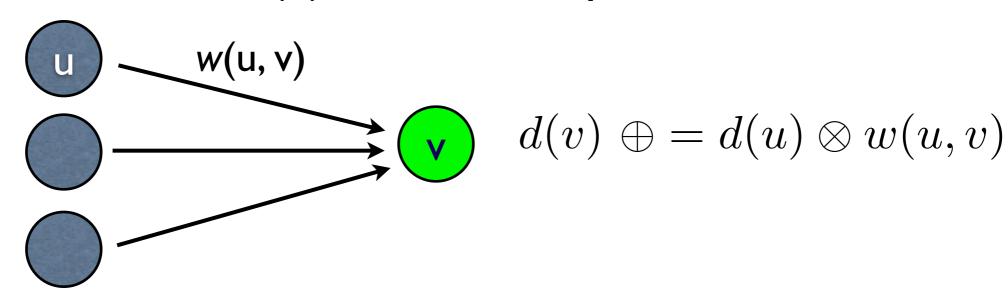
Related Formalisms

hypergraph	AND/OR graph	context-free grammar	deductive system
vertex	OR-node	symbol	item
source-vertex	leaf OR-node	terminal	axiom
target-vertex	root OR-node	start symbol	goal item
hyperedge	AND-node	production	instantiated deduction
		f	$\underline{u_1:a u_2:b}$
$(\{u_1,u_2\},v,f)$		$v\stackrel{\jmath}{ ightarrow} u_1\;u_2$	v:f(a,b)



Viterbi Algorithm for DAGs

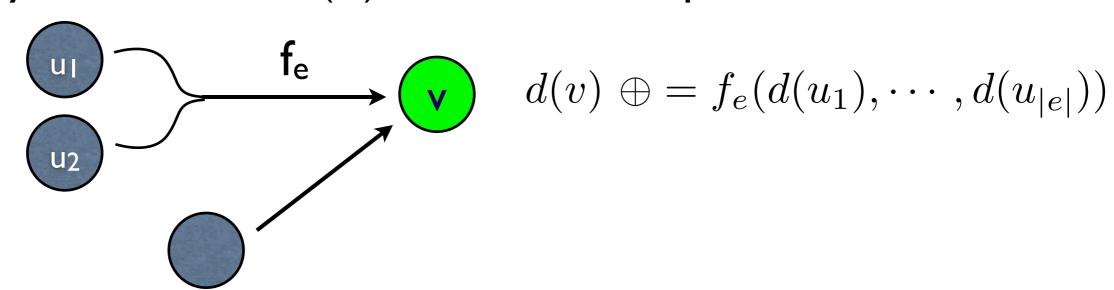
- 1. topological sort
- 2. visit each vertex v in sorted order and do updates
 - for each incoming edge (u, v) in E
 - use d(u) to update d(v):
 - key observation: d(u) is fixed to optimal at this time



time complexity: O(V + E)

Viterbi Algorithm for DAHs

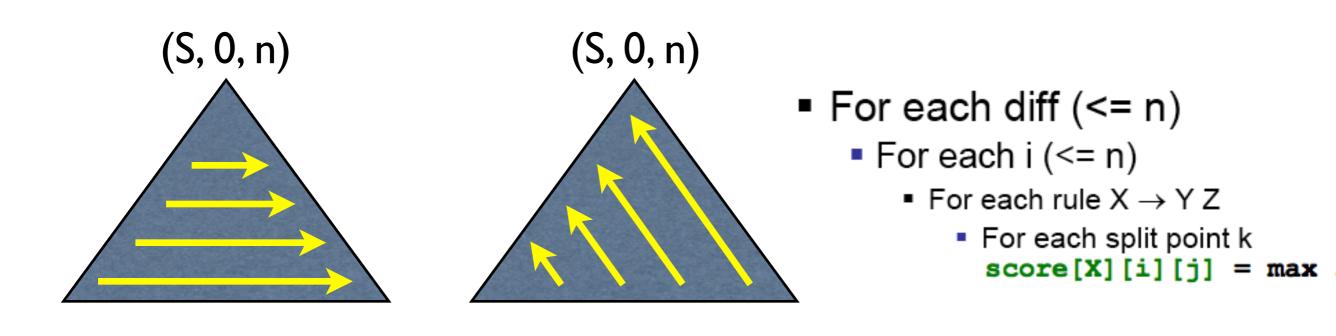
- 1. topological sort
- 2. visit each vertex v in sorted order and do updates
 - for each incoming hyperedge $e = ((u_1, ..., u_{|e|}), v, f_e)$
 - use d(u_i)'s to update d(v)
 - key observation: d(ui)'s are fixed to optimal at this time



time complexity: O(V + E) (assuming constant arity)

Example: CKY Parsing

- parsing with CFGs in Chomsky Normal Form (CNF)
- typical instance of the generalized Viterbi for DAHs
- many variants of CKY ~ various topological ordering



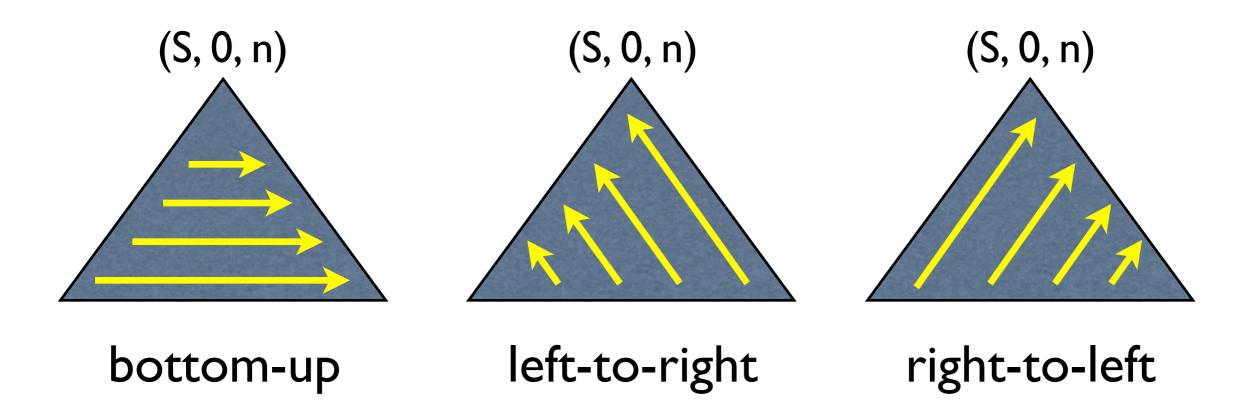
 $O(n^3|P|)$

bottom-up

left-to-right

Example: CKY Parsing

- parsing with CFGs in Chomsky Normal Form (CNF)
- typical instance of the generalized Viterbi for DAHs
- many variants of CKY ~ various topological ordering



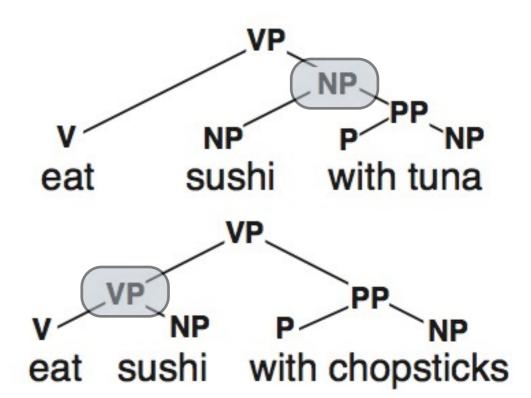
 $O(n^3|P|)$

Parser/Tree Evaluation

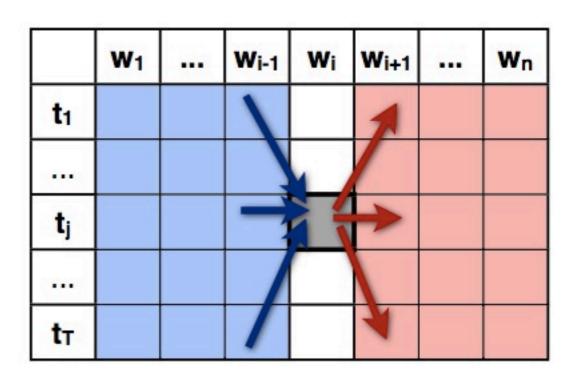
- how would you evaluate the quality of output trees?
- need to define a "similarity measure" between trees
 - for sequences, we used
 - same length: hamming distance (e.g., POS tagging)
 - varying length: edit distance (e.g., Japanese transliteration)
 - varying length: precision/recall/F (e.g., word-segmentation)
 - varying length: crossing brackets (e.g., word-segmentation)
 - for trees, we use precision/recall/F and crossing brackets
 - standard "PARSEVAL" metrics (implemented as evalb.py)

PARSEVAL

- comparing nodes ("brackets"):
 - labelled (by default): (NP, 2, 5);
 or unlabelled: (2, 5)
- precision: how many predicted nodes are correct?
- recall: how many correct nodes are predicted?
- how to fake precision or recall?
- F-score: F=2pr/(p+r)
- other metrics: crossing brackets



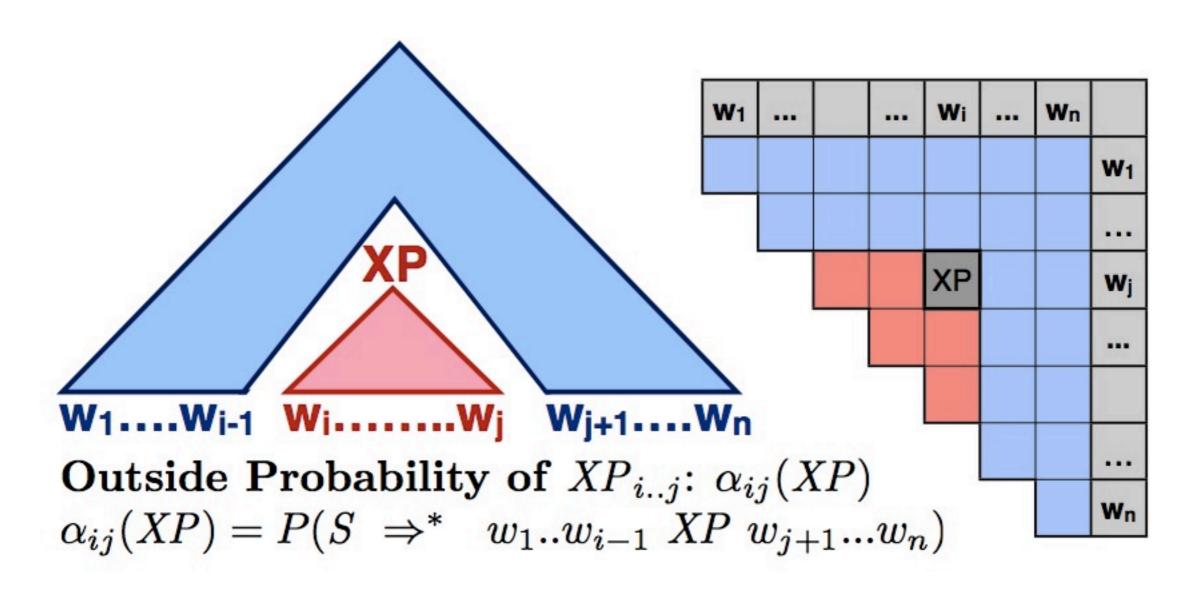
```
matched=6
predicted=7
gold=7
precision=6/7
recall=6/7
F=6/7
```



Forward Probability of t_i : $\alpha_i(t)$ $\alpha_i(t) = P(w_1...w_i, tag_i = t_i)$

Backward Probability of t_i : $\beta_i(t)$ $\beta_i(t) = P(w_{i+1}...w_n|tag_i = t)$

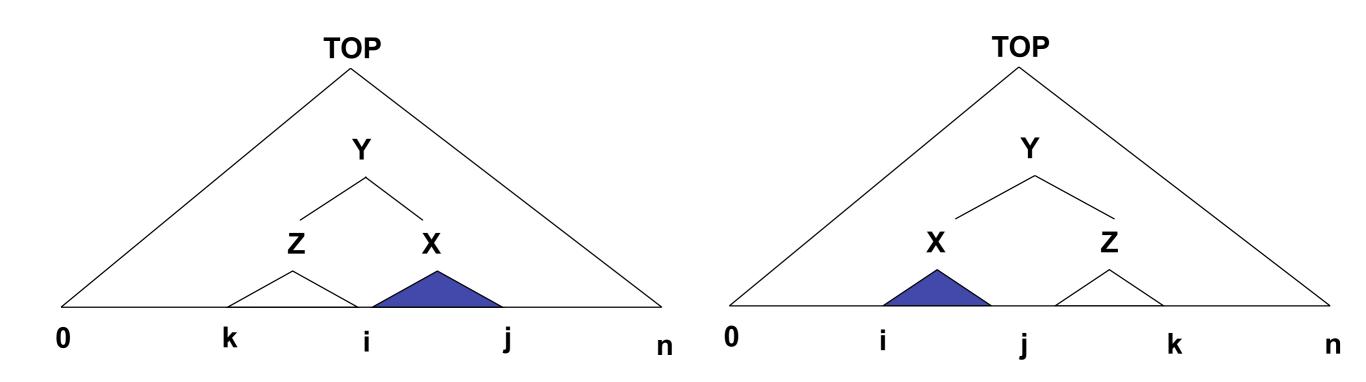
CS 498 JH: Introduction to NLP (Fall '08)



Inside Probability of
$$XP_{i..j}$$
: $\beta_{ij}(XP)$
 $\beta_{ij}(XP) = P(XP \Rightarrow^* w_i...w_j)$

CS 498 JH: Introduction to NLP (Fall '08)

- inside prob beta is easy to compute (CKY, max=>+)
- what is outside prob alpha(X,i,j)?
 - need to enumerate ways to go to TOP from X,i,j
 - X,i,j can be combined with other nodes on the left/right
 - L: sum_{Y->Z X, k} alpha(Y,k,j) Pr(Y->Z X) beta(Z,k,i)
 - R: $sum_{Y->X} Z, k$ alpha(Y,i,k) Pr(Y->X) beta(Z,j,k)
 - why beta is used in alpha? very diff. from F-W algorithm
- what is the likelihood of the sentence?
 - beta(TOP, 0, n) or alpha(w_i, i, i+1) for any i



- L: sum_{Y->Z X, k} alpha(Y,k,j) Pr(Y->Z X) beta(Z,k,i)
- R: sum_{Y->X Z, k} alpha(Y,i,k) Pr(Y->X Z) beta(Z,j,k)

- how do you do EM with alphas and betas?
 - easy; M-step: divide by fractional counts
 - fractional count of rule (X,i,j -> Y,i,k Z,k,j) is
 - alpha(X,i,j) prob(Y Z|X) beta(Y,i,k) beta(Z,k,j)
- if we replace "+" by "max", what will alpha/beta mean?
 - beta': Viterbi inside: best way to derive X,i,j
 - alpha': Viterbi outside: best way to go to TOP from X,i,j
- now what is alpha'(X, i, j) beta'(X, i, j)?
 - best derivation that contains X,i,j (useful for pruning)

traversing order

	ci avoi sing oi doi		
	topological (acyclic)	best-first (superior)	
graphs with semirings (e.g., FSMs)	Viterbi	Dijkstra	
hypergraphs with weight functions (e.g., CFGs)	Gen. Viterbi (e.g., CKY)	Knuth	

search space

How to generate from a CFG?

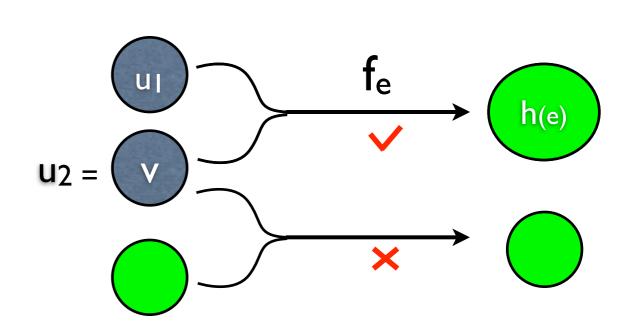
- analogy in finite-state world: given a WFSA, generate strings (either randomly or in order)
- Viterbi doesn't work (cycles)
- Dijkstra still works (as long as it's probabilities)
- What's the generalization of Dijkstra in the tree world?

Forward Variant for DA-s

- 1. topological sort
- 2. visit each vertex v in sorted order and do updates
 - for each outgoing hyperedge $e = ((u_1, ..., u_{|e|}), h(e), f_e)$
 - if d(u_i)'s have all been fixed to optimal
 - use d(u_i)'s to update d(h(e))

Q: how to avoid repeated checking?
maintain a counter r[e] for each e:
how many tails yet to be fixed?
fire this hyperedge only if r[e]=0

time complexity: O(V + E)



Example: Treebank Parsers

- State-of-the-art statistical parsers
 - (Collins, 1999; Charniak, 2000)
 - no fixed grammar (every production is possible)
 - can't do backward updates
 - don't know how to decompose a big item
 - forward update from vertex (X, i, j)
 - check all vertices like (Y, j, k) or (Y, k, i) in the chart (fixed)
 - try combine them to form bigger item (Z, i, k) or (Z, k, j)

Two Dimensional Survey

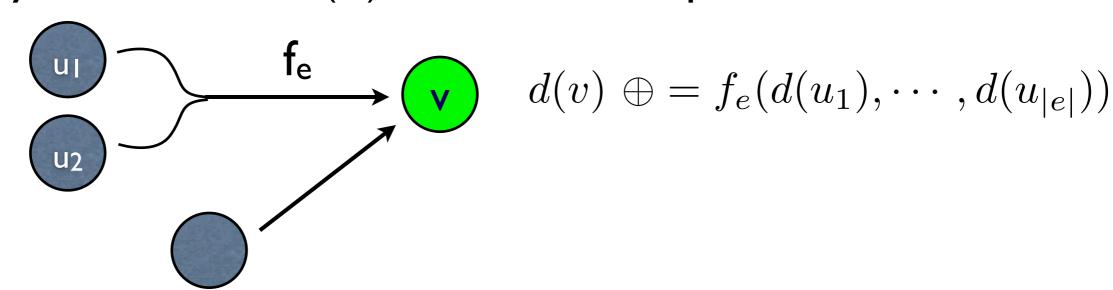
traversing order

best-first topological (acyclic) (superior) graphs with semirings Dijkstra Viterbi (e.g., FSMs) hypergraphs with Generalized weight functions Knuth Viterbi (e.g., CFGs)

search space

Viterbi Algorithm for DAHs

- 1. topological sort
- 2. visit each vertex v in sorted order and do updates
 - for each incoming hyperedge $e = ((u_1, ..., u_{|e|}), v, f_e)$
 - use d(u_i)'s to update d(v)
 - key observation: d(ui)'s are fixed to optimal at this time



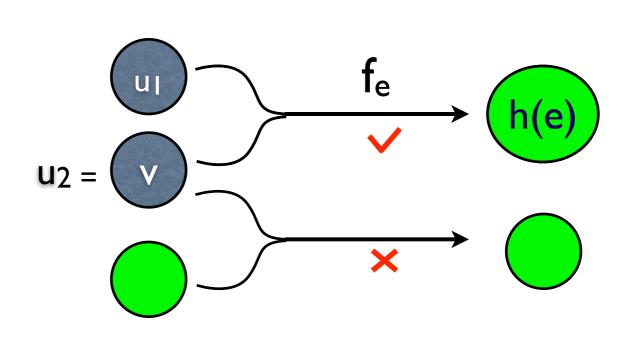
time complexity: O(V + E) (assuming constant arity)

Forward Variant for DA-s

- I. topological sort
- 2. visit each vertex v in sorted order and do updates
 - for each outgoing hyperedge $e = ((u_1, ..., u_{|e|}), h(e), f_e)$
 - if d(u_i)'s have all been fixed to optimal
 - use d(u_i)'s to update d(h(e))

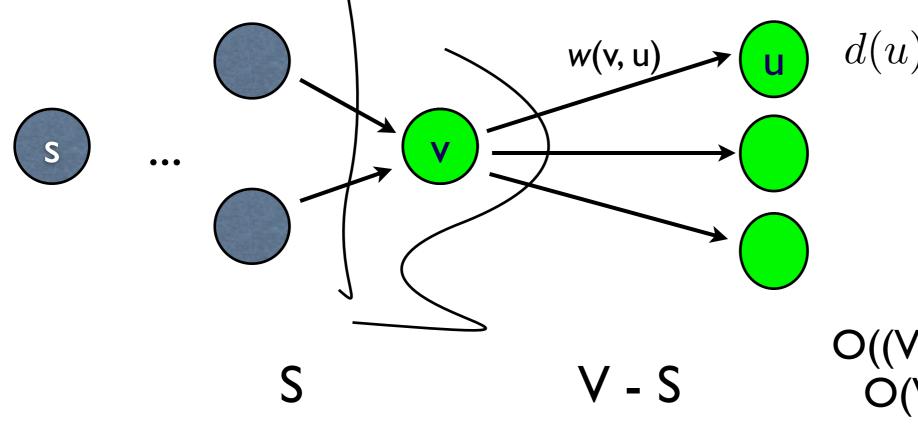
Q: how to avoid repeated checking?
maintain a counter r[e] for each e:
how many tails yet to be fixed?
fire this hyperedge only if r[e]=0

time complexity: O(V + E)



Dijkstra Algorithm

- keep a cut (S:V S) where S vertices are fixed
 - maintain a priority queue Q of V S vertices
- each iteration choose the best vertex v from Q
 - move v to S, and use d(v) to forward-update others

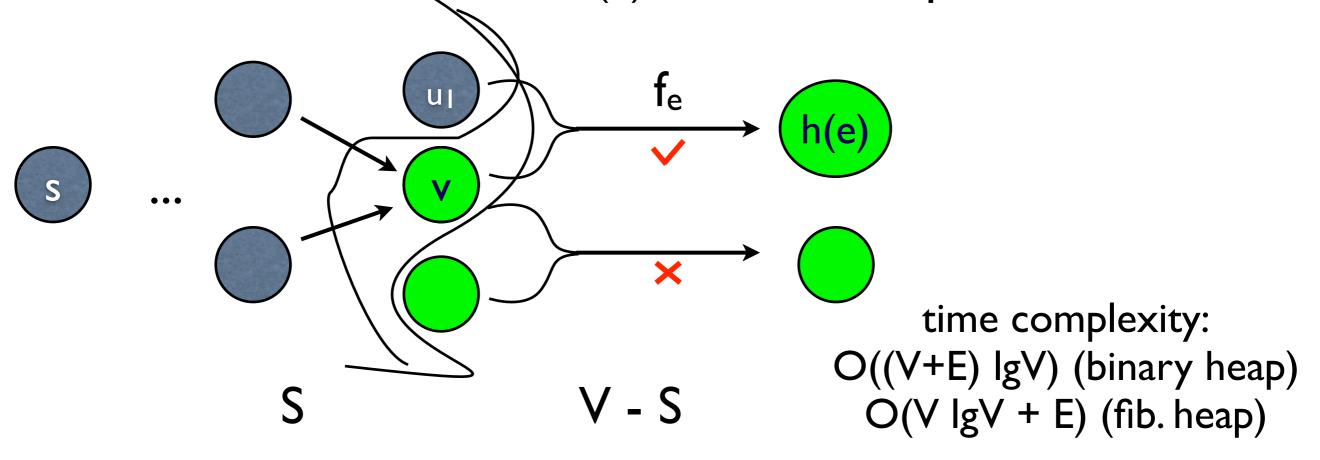


$$d(u) \oplus = d(v) \otimes w(v, u)$$

time complexity:
O((V+E) IgV) (binary heap)
O(V IgV + E) (fib. heap)

Knuth (1977) Algorithm

- keep a cut (S:V S) where S vertices are fixed
 - maintain a priority queue Q of V S vertices
- each iteration choose the best vertex v from Q
 - move v to S, and use d(v) to forward-update others



Summary of Perspectives on Parsing

- Parsing and can be viewed as:
 - search in the space of possible trees
 - (logical/probabilistic) deduction
 - intersection / composition
 - generation (from intersected grammar)
 - forest building
- Parsing algorithms introduced so far are DPs:
 - CKY: simplest, external binarization -- implement in hw5
 - intersection + Knuth 77: best-first search

Translation as Parsing

- translation with SCFGs => monolingual parsing
- parse the source input with the source projection
 - build the corresponding target sub-strings in parallel

```
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ightarrow & juxing \ le \ huitan, \ \mathbf{PP} & 
ightarrow & yu \ Shalong, \end{array}
```

complexity: same as CKY parsing -- $O(n^3)$

held a talk with Sharon

VPI,6

with Sharon held a talk

PPI,3 VP3,6

yu Shalong juxing le huitan

Adding a Bigram Model

