

# Sets

identity maps, unordered collection

# Sets

- `[]` for lists, `()` for tuples, `{}` for dicts, and `{}` for sets (2.7)
- construction from lists, tuples, dicts (keys), and strs
- `in`, `not in`, `add`, `remove`

```
>>> a = {1, 2}
a
>> set([1, 2])
>>> a = set((1,2))
>>> a
set([1, 2])
>>> b = set([1,2])
>>> a == b
True
>>> c = set({1:'a', 2:'b'})
>>> c
set([1, 2])
```

```
>>> a = set([])
>>> 1 in a
False
>>> a.add(1)
>>> a.add('b')
>>> a
set([1, 'b'])
>>> a.remove(1)
>>> a
set(['b'])
```

# Set Operations

- union, intersection, difference, `is_subset`, etc..

```
>>> a = set('abracadabra')
>>> b = set('alacazam')
>>> a
set(['a', 'r', 'b', 'c', 'd'])
>>> a - b
set(['r', 'd', 'b'])
>>> a | b
set(['a', 'c', 'r', 'd', 'b', 'm', 'z', 'l'])
>>> a & b
set(['a', 'c'])
>>> a ^ b
set(['r', 'd', 'b', 'm', 'z', 'l'])
>>> a |= b
>>> a
set(['a', 'c', 'b', 'd', 'm', 'l', 'r', 'z'])
```

demo

# set and frozenset type

Operation	Equivalent	Result
<code>len(s)</code>		cardinality of set <i>s</i>
<code>x in s</code>		test <i>x</i> for membership in <i>s</i>
<code>x not in s</code>		test <i>x</i> for non-membership in <i>s</i>
<code>s.issubset(t)</code>	$s \leq t$	test whether every element in <i>s</i> is in <i>t</i>
<code>s.issuperset(t)</code>	$s \geq t$	test whether every element in <i>t</i> is in <i>s</i>
<code>s.union(t)</code>	$s   t$	new set with elements from both <i>s</i> and <i>t</i>
<code>s.intersection(t)</code>	$s \& t$	new set with elements common to <i>s</i> and <i>t</i>
<code>s.difference(t)</code>	$s - t$	new set with elements in <i>s</i> but not in <i>t</i>
<code>s.symmetric_difference(t)</code>	$s \wedge t$	new set with elements in either <i>s</i> or <i>t</i> but not both
<code>s.copy()</code>		new set with a shallow copy of <i>s</i>
<code>s.update(t)</code>	$s  = t$	return set <i>s</i> with elements added from <i>t</i>
<code>s.intersection_update(t)</code>	$s \&= t$	return set <i>s</i> keeping only elements also found in <i>t</i>
<code>s.difference_update(t)</code>	$s -= t$	return set <i>s</i> after removing elements found in <i>t</i>
<code>s.symmetric_difference_update(t)</code>	$s \wedge= t$	return set <i>s</i> with elements from <i>s</i> or <i>t</i> but not both
<code>s.add(x)</code>		add element <i>x</i> to set <i>s</i>
<code>s.remove(x)</code>		remove <i>x</i> from set <i>s</i> ; raises <code>KeyError</code> if not present
<code>s.discard(x)</code>		removes <i>x</i> from set <i>s</i> if present
<code>s.pop()</code>		remove and return an arbitrary element from <i>s</i> ; rais
<code>s.clear()</code>		remove all elements from set <i>s</i>

# Basic *import* and I/O

# import and I/O

- similar to `import` in Java
- File I/O much easier than Java

```
import sys                               demo
for line in sys.stdin:
    print line.split()
```

or

```
from sys import *
for line in stdin:
    print line.split()
```

```
import System;
```

Java

```
import System.*;
```

```
>>> f = open("my.in", "rt")
>>> g = open("my.out", "wt")
>>> for line in f:
...     print >> g, line,
...     g.close()
```

file copy

to read a line:

```
line = f.readline()
```

to read all the lines:

```
lines = f.readlines()
```

note this comma!

# import and `__main__`

- multiple source files (modules)

foo.py

- C: `#include "my.h"`
- Java: `import My`

- demo

```
def pp(a):                                demo
    print " ".join(a)

if __name__ == "__main__":
    from sys import *
    a = stdin.readline()
    pp (a.split())
```

- handy for debugging

```
>>> import foo
>>> pp([1,2,3])
1 2 3
```

interactive

# Quiz

- Palindromes

abcba

- read in a string from standard input, and print `True` if it is a palindrome, print `False` if otherwise

```
def palindrome(s):  
    if len(s) <= 1 :  
        return True  
    return s[0] == s[-1] and palindrome(s[1:-1])  
  
if __name__ == '__main__' :  
  
    import sys  
    s = sys.stdin.readline().strip()  
    print palindrome(s)
```



# Functional Programming

# map and filter

- intuition: function as data
- we have already seen functional programming a lot!
  - list comprehension, custom comparison function

```
map(f, a)
```

```
filter(p, a)
```

```
[ f(x) for x in a ]
```

```
[ x for x in a if p(x) ]
```

```
map(f, filter(p, a))
```

```
[ f(x) for x in a if p(x) ]
```

```
>>> map(int, ['1','2'])
[1, 2]
>>> " ".join(map(str, [1,2]))
1 2
```

```
>>> def is_even(x):
...     return x % 2 == 0
...
>>> filter(is_even, [-1, 0])
[0]
```

demo

# lambda

- map/filter in one line for custom functions?
- “anonymous inline function”
- borrowed from LISP, Scheme, ML, OCaml



```
>>> f = lambda x: x*2
>>> f(1)
2
>>> map (lambda x: x**2, [1, 2])
[1, 4]
>>> filter (lambda x: x > 0, [-1, 1])
[1]
>>> g = lambda x,y : x+y
>>> g(5,6)
11
>>> map (lambda (x,y): x+y, [(1,2), (3,4)])
[3, 7]
```

demo

# more on lambda

```
>>> f = lambda : "good!"
>>> f
<function <lambda> at 0x381730>
>>> f()
'good!'
```

lazy evaluation

```
>>> a = [5, 1, 2, 6, 4]
>>> a.sort(lambda x,y : y - x)
>>> a
[6, 5, 4, 2, 1]
```

custom comparison

```
>>> a = defaultdict(lambda : 5)
>>> a[1]
5
>>> a = defaultdict(lambda : defaultdict(int))
>>> a[1]['b']
0
```

demo

# Basic Sorting

```
>>> a = [5, 2, 3, 1, 4]
>>> a.sort()
>>> print a
[1, 2, 3, 4, 5]
```

```
>>> a = [5, 2, 3, 1, 4]
>>> a.sort(reverse=True)
>>> a
[5, 4, 3, 2, 1]
```

```
>>> a = [5, 2, 3, 1, 4]
>>> a.sort()
>>> a.reverse()
>>> a
[5, 4, 3, 2, 1]
```

**sort() is in-place,  
but sorted() returns new copy**

```
>>> a = [5, 2, 3, 1, 4]
>>> sorted(a)
[1, 2, 3, 4, 5]
>>> a
[5, 2, 3, 1, 4]
```

# Built-in and custom cmp

```
>>> a = [5, 2, 3, 1, 4]
```

```
>>> def mycmp(a, b):  
    return b-a
```

```
>>> sorted(a, mycmp)  
[5, 4, 3, 2, 1]
```

```
>>> sorted(a, lambda x,y: y-x)  
[5, 4, 3, 2, 1]
```

```
>>> a = zip([1,2,3], [6,4,5])
```

```
>>> a.sort(lambda (_,y1), (__, y2): y1-y2)
```

```
>>> a
```

```
[(2, 4), (3, 5), (1, 6)]
```

```
>>> a.sort(lambda (_,y1), (_, y2): y1-y2)
```

```
SyntaxError: duplicate argument '_' in function definition
```

demo

# Sorting by Keys or Key mappings

```
>>> a = "This is a test string from Andrew".split()
>>> a.sort(key=str.lower)
>>> a
['a', 'Andrew', 'from', 'is', 'string', 'test', 'This']
```

```
>>> import operator
>>> L = [('c', 2), ('d', 1), ('a', 4), ('b', 3), ('b', 1)]
```

```
>>> L.sort(key=operator.itemgetter(1))
>>> L
[('d', 1), ('b', 1), ('c', 2), ('b', 3), ('a', 4)]
```

demo

```
>>> sorted(L, key=operator.itemgetter(1, 0))
[('b', 1), ('d', 1), ('c', 2), ('b', 3), ('a', 4)]
```

sort by two keys

```
>>> operator.itemgetter(1,0)((1, 2, 3))
(2, 1)
```

# lambda for key mappings

- you can use lambda for both custom cmp and key map

```
>>> a = "This is a test string from Andrew".split()
>>> a.sort(lambda x, y: cmp(x.lower(), y.lower()))
>>> a
['a', 'Andrew', 'from', 'is', 'string', 'test', 'This']

>>> a.sort(key=lambda x: x.lower())

>>> L = [('c', 2), ('d', 1), ('a', 4), ('b', 3), ('b', 1)]

>>> L.sort(key=lambda (_, y): y)
>>> L
[('d', 1), ('b', 1), ('c', 2), ('b', 3), ('a', 4)]

>>> sorted(L, key=lambda (x, y): (y, x))
[('b', 1), ('d', 1), ('c', 2), ('b', 3), ('a', 4)]
```



# Decorate-Sort-Undecorate

```
>>> words = "This is a test string from Andrew.".split()

>>> deco = [ (word.lower(), i, word) for i, word in \
... enumerate(words) ]

>>> deco.sort()

>>> new_words = [ word for _, _, word in deco ]

>>> print new_words
['a', 'Andrew.', 'from', 'is', 'string', 'test', 'This']
```

demo

- Most General
- Faster than custom cmp (or custom key map) -- why?
- stable sort (by supplying index)

# Memoized Recursion v1

- Fibonacci revisited

```
def fib(n):  
    a, b = 1, 1  
    for _ in range(n-1):  
        a, b = b, a+b  
    return b
```

```
def fib(n):  
    if n <= 1:  
        return n  
    else:  
        return fib (n-1) + fib (n-2)
```

```
fibs = {0:1, 1:1}  
def fib(n):  
    if n in fibs:  
        return fibs[n]  
    fibs[n] = fib(n-1) + fib(n-2)  
    return fibs[n]
```

can we get rid of the global variable?

# Memoized Recursion v2

- Fibonacci revisited

```
def fib(n):  
    a, b = 1, 1  
    for _ in range(n-1):  
        a, b = b, a+b  
    return b
```

```
def fib(n):  
    if n <= 1:  
        return n  
    else:  
        return fib (n-1) + fib (n-2)
```

```
def fib(n, fibs={0:1, 1:1}):  
    if n in fibs:  
        return fibs[n]  
    fibs[n] = fib(n-1, fibs) + fib(n-2, fibs)  
    return fibs[n]
```

# Memoized Recursion v3

- Fibonacci revisited

```
def fib(n):  
    a, b = 1, 1  
    for _ in range(n-1):  
        a, b = b, a+b  
    return b
```

```
>>> fib(3)  
1 {1: 1}  
0 {0: 1, 1: 1}  
2 {0: 1, 1: 1, 2: 2}  
3 {0: 1, 1: 1, 2: 2, 3: 3}  
3  
>>> fib(2)  
2  
>>> print fibs  
Error!
```

draw the tree!

```
def fib(n, fibs={0:1, 1:1}):  
    if n in fibs:  
        return fibs[n]  
    fibs[n] = fib(n-1) + fib(n-2)  
    # print n, fibs  
    return fibs[n]
```

the **fibs** variable has a weird closure!! feature or bug?  
most people think it's a bug, but Python inventor argues it's a feature.

# Memoized Recursion v4

- Fibonacci revisited

```
def fib(n):  
    a, b = 1, 1  
    for _ in range(n-1):  
        a, b = b, a+b  
    return b
```

```
>>> fib(4)  
{0: 1, 1: 1, 2: 2}  
{0: 1, 1: 1, 2: 2, 3: 3}  
{0: 1, 1: 1, 2: 2, 3: 3, 4: 5}  
5  
>>> fib(3)  
{0: 1, 1: 1, 2: 2}  
{0: 1, 1: 1, 2: 2, 3: 3}  
3
```

```
def fib(n, fibs=None):  
    if fibs is None:  
        fibs = {0:1, 1:1}  
    if n in fibs:  
        return fibs[n]  
    fibs[n] = fib(n-1, fibs) + fib(n-2, fibs)  
    # print n, fibs  
    return fibs[n]
```

this is so far the cleanest way to avoid the bug.

# Implementation

- lists, tuples, and strings
  - random access:  $O(1)$
  - insertion/deletion/in:  $O(n)$
- dict
  - in/random access: almost  $O(1)$
  - insertion/deletion: almost  $O(1)$
  - but no linear ordering!

# Pythonic Styles

- do not write ... when you can write ...

<pre>for key in d.keys():</pre>	<pre>for key in d:</pre>
<pre>if d.has_key(key):</pre>	<pre>if key in d:</pre>
<pre>i = 0 for x in a:     ...     i += 1</pre>	<pre>for i, x in enumerate(a):</pre>
<pre>a[0:len(a) - i]</pre>	<pre>a[:-i]</pre>
<pre>for line in \     sys.stdin.readlines():</pre>	<pre>for line in sys.stdin:</pre>
<pre>for x in a:     print x, print</pre>	<pre>print " ".join(map(str, a))</pre>
<pre>s = "" for i in range(lev):     s += " " print s</pre>	<pre>print " " * lev</pre>