Energy-Efficient Routing for Time-Sensitive Data Traffic in Linear Wireless Sensor Networks

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Abstract—Linear wireless sensor networks (LWSN) are special class of wireless sensor networks where sensor nodes are deployed in a straight line. Monitoring industrial pipelines, railroads, tunnels, power lines, and borders are applications of LWSNs. Wireless sensors are tiny devices with limited energy resources; therefore, efficient energy routing in LWSNs is critical. In this paper, we propose energy-efficient routing schemes for time-sensitive data traffic in linear wireless sensor networks. We further simulate LWSNs and analyze the behavior of lifetime against varying network parameters.

I. INTRODUCTION

A linear wireless sensor network (LWSN) [1] is a special class of wireless sensor networks (WSN) [2] where sensors are deployed in a straight line as shown in figure 1. In [1, p. 1671], LWSNs are defined as “a new category of WSN where the nodes are placed in a strictly linear or semi-linear form”. LWSNs exist in a wide variety of applications such as industrial pipelines condition monitoring [3]–[5], railroads, tunnels, power lines, and borders monitoring [1]. In typical WSNs, the deployment of nodes is random but in LWSNs, the topology of the network is predetermined. Although generic WSN routing techniques can be implemented for LWSN, customized protocols that utilize linearity of the topology would improve network performance. WSN generic techniques like flooding might not be necessary in LWSN since the topology is already known. Other techniques such as Jump always and Redirect always [6] can be used in LWSNs because of network topology.

In a typical LWSN, all generated data traffic will be forwarded to the sink by a limited number of sensors, i.e. sensors adjacent to the sink. Thereby, those sensors will rapidly lose their energy and impact network performance [7], [8]. Therefore, the network must distribute data traffic load intelligently in order to properly consume energy and prolong its lifetime. On the contrary, data traffic generated by nodes far from sinks will have to be relayed through many sensors and endure extended delays. For time-sensitive applications like oil and gas pipelines monitoring, it is critical to report pipelines status within a certain delay margin [3]. Therefore, the network routing protocol should balance energy consumption while ensuring data traffic is being delivered within the accepted delay margin. In this paper, we propose energy-efficient routing schemes for time-sensitive data traffic in linear wireless sensor networks.

The rest of the paper is organized as follows. Section II highlights some LWSN related work. Section III describes the network model. Section IV formulates routing problems and establishes routing constraints. Section V describes the simulation setup and analyzes results. Section VI concludes the paper.

II. RELATED WORK

In [9], Ehsan et al. proposed a network lifetime maximizing MAC-aware schemes for routing rate-constrained traffic in WSN with a single sink. In [10], Xuguang et al. proposed a LWSN routing algorithm for monitoring roads post natural disasters. Caneva and Montessoro in [11] proposed a bidirectional wireless communication scheme called Wireless Wire (WiWi) with a contention-free MAC protocol as a virtualization of wire based links. In [12], Liu and Mohapatra studied the deployment of LWSN and addressed the problem of finding the optimal number of nodes given the initial amount of energy in each node and the required lifetime of the network and proposed a close-to-optimal greedy algorithm for deploying nodes in LWSN. Hassian et al. in [7] proposed a deployment scheme that enforces equal energy dissipation by each node per each data gathering cycle, and introduced a network energy metric that corresponds to the percentage of consumed network energy at the end of its lifetime. In [13], Chen et al. proposed a time-efficient MAC protocol (LC-MAC) for LWSNs to address extended end-to-end delay in power lines monitoring systems. Zimmerling et al. in [14] derived a theoretical lower bound for the optimal energy consumption in LWSNs with Poisson distributed sensor nodes in rail roads monitoring applications. Considering channel characteristics, radio components and distribution of nodes, they proposed two routing protocols (MERR) and (AMERR) to minimize energy consumption in LWSNs. In [15], Stoianov et al. proposed PipeNet, a water pipelines leakage detection system based on Intel’s mote. Guo et al. in [16] studied nodes deployment techniques that maximize network lifetime in LWSNs for oil pipeline monitoring. They formulated a single-sink LWSN with discrete power-level sensors as a mixed integer linear program, and proposed equal-power consumption placement heuristics to maximize the network lifetime.
III. NETWORK MODEL

A LWSN is modeled as a directed acyclic graph \( G = (\mathcal{M}, \mathcal{F}) \) where \( \mathcal{M} \) and \( \mathcal{F} \) are finite nonempty sets of all nodes and all flows in \( G \) respectively. Let \( \mathcal{N} \) and \( \mathcal{K} \) be the subsets of \( \mathcal{M} \) that contain all sensor nodes (SR) and all sink nodes (SK), respectively. Each flow in \( \mathcal{F} \) corresponds to an ordered pair \( (n, m)' \) such that SR \( n \) is able to receive traffic originated at node \( l \) and forward it to SR \( m \) in order to be relayed to SK \( s \). At any given time, each SR \( i \) must associate with a single SK \( s \) and forward its data traffic toward \( s \). For the flow \( (n, m)' \) in \( \mathcal{F} \), SRs \( n, m \) and \( l \) must be associated with \( s \) and since \( n \) and \( m \) are associated with \( s \) and are able to communicate with each other, they are considered to be neighbors. It is assumed that at any given time, there exists at least one path from every SR to a single SK. An active SR is one that is able to communicate with its neighbors. An inactive SR is unable to communicate because either it has consumed all of its energy or it is isolated due to other inactive SRs along the path to the SK. In \( G \), all nodes are deployed equidistantly and all SRs are identical in term of capabilities and internal resources. Each SR has only one communication interface and all SRs are communicating on a single channel.

All SKs are assumed to have infinite amount of energy and to disseminate collected data traffic to the monitoring center via a separate network while not generating any data traffic into the LWSN. The first SK is always placed on one edge of the network and the second SK is always on the other edge. Any additional SKs are placed in the middle of the network. Each edge SK is collecting data traffic from a single direction while each intermediate SK is collecting data from both directions. The network is divided into multiple sections \( S_y \) where each section corresponds to each SK side(s) as shown in figure 2. Note that \( y \) is defined as \( 2|\mathcal{K}| - 2 \geq y \geq 1 \) where \( 2|\mathcal{K}| - 2 \) is the total number of sections in the network \( G \). Each SK must associate with at least one SR in each section. Let \( |\mathcal{N}|_{S_y} \) denote the number of SRs in a section \( S_y \) such that,

\[
|\mathcal{N}|_{S_y} = \begin{cases} 
\frac{|\mathcal{N}|}{2|\mathcal{K}|-2}, & \text{if } y \leq (|\mathcal{N}| \mod (2|\mathcal{K}| - 2)), \\
\frac{|\mathcal{N}|}{2|\mathcal{K}|-2}, & \text{otherwise}.
\end{cases}
\]

IV. ROUTING

In this section, routing constraints are established and routing is formulated as a linear optimization problem. In \( G \) and for each flow \( (i, j)' \) in \( \mathcal{F} \), let \( x^k_{ij} \) denote the forwarding data rates in bits per second and \( X = [x^k_{ij}]_{1 \leq i, j, k \leq |\mathcal{N}|} \) denote the rate vector of all data rates. When SR \( i \) is transmitting, it is assumed to send \( L \)-bit messages at an average rate of \( R_i \). Whenever a SR consumes its entire energy, the network will seize to function. Hence, the network lifetime \( T \) is defined as the time taken by the first SR to consume its entire energy. The wireless channel capacity \( W \) is defined as the maximum data rate the wireless medium can support. In this work, the goal is to find the optimal data rates vector \( X \) that maximizes the network lifetime \( T \) subject to the routing constraints.

A. Routing Constraints

For \( X \) to be feasible in rate-constrained and time-sensitive LWSNs, the following constraints must be satisfied,

- **Flow Balance Constraints:**
  For each SR \( i \), the sum of all outgoing data rates must equal the sending rate of SR \( i \); i.e.,
  \[
  \sum_{j \in \mathcal{N}} x^k_{ij} = R_i; \quad \forall i \in \mathcal{N}.
  \]  
  (1)

  For each SK \( s \), the sum of all incoming data rates must equal the sum of all sending data rates of all transmitting SRs that are associated with \( s \). That is,
  \[
  \sum_{i, k \in \mathcal{N}} x^k_{is} = \sum_{k \in \mathcal{N}} R_k; \quad \forall s \in \mathcal{K}.
  \]  
  (2)

  The sum of all SR \( k \) flows forwarded to SR \( j \) must equal the sum of all \( k \) flows forwarded by \( j \). That is,
  \[
  \sum_{i \in \mathcal{N}} x^k_{ij} = \sum_{q \in \mathcal{N}} x^k_{jq}; \quad \forall j, k \in \mathcal{N}.
  \]  
  (3)

  Each SK \( s \) is assumed to neither generate, nor forward any data traffic in the network. That is,
  \[
  x^p_{si} = 0; \quad \forall i \in \mathcal{N}, \quad \forall s, p \in \mathcal{K}.
  \]  
  (4)

  Finally, all data rates must be positive; i.e.,
  \[
  x^k_{ij} \geq 0; \quad i, j, k \in \mathcal{N}.
  \]  
  (5)

- **Energy Consumption Constraints:**
  SRs consume energy while sensing, processing or communicating. In this work, only communication energy is being considered. We adopt the widely used energy consumption model of [17]. Let \( c_{ij} \) denote the amount of energy required to transmit one bit from node \( i \) to node \( j \). If the distance between \( i \) and \( j \) is denoted by \( d \) then \( c_{ij} = \beta d^\gamma \) where \( \beta \) accounts for energy dissipated in the transmitter amplifier and \( \gamma \) is the path loss exponent. In networks with a clear line-of-sight, \( \gamma \) is typically 2 and in dense urban areas it can go up to 6 [18]. In this work, \( \gamma \) is set to 2. Let \( B_i(t) \) be the amount of energy SR \( i \) has at time \( t \). According to our definition of the network lifetime \( T \) in section III, \( B_i(T) \geq 0 \) must hold for every SR in order for the network to be functional. Hence, if the LWSN is deployed at time \( t_0 \), then
  \[
  B_i(t_0) \geq T \times \sum_{j \in \mathcal{N}} c_{ij} x^k_{ij}
  \]  
  (6)

  must hold for every SR \( i \). Inequality (6) is not linear in variables \( T \) and \( x^k_{ij} \). But when letting \( F = 1/T \), it can be equivalently rewritten as
  \[
  F \geq \frac{1}{B_i(t_0)} \times \sum_{j \in \mathcal{N}} c_{ij} x^k_{ij},
  \]  
  (7)

  yielding an inequality that is linear in variables \( F \) and \( x^k_{ij} \). Note that minimizing \( F \) is equivalent to maximizing the lifetime \( T \).
• **Medium contention constraints:**
  In this work, we consider and implement IEEE 802.11 MAC protocol [19]. IEEE 802.11 MAC dictates that if SR $i$ is communicating with SR $j$, all nodes within the transmission range of either $i$ or $j$ can not communicate. We model the set of flows $\mathcal{F}$ as undirected graph $C = (\mathcal{F}, \mathcal{L})$ where $\mathcal{L}$ is the finite set of all distinct contending pairs of flows in $\mathcal{F}$. The graph $C$ is referred to as flow contention graph [20]. Let $\Psi_{ij}^k$ be the set of all flows that contend with the active flow $(i, j)^k$; i.e., $\Psi_{ij}^k = \{(p, q)^k \in \mathcal{F} : (i, j)^k \in \mathcal{L}, (p, q)^k \in \mathcal{L}\}$. The rate vector $X$ is feasible if, for all $i, j, k \in \mathcal{N}$, the following medium contention constraints hold [20],

$$x_{ij}^k + \sum_{(p, q)^k \in \Psi_{ij}^k} x_{pq}^s \leq W; \quad \forall s \in \mathcal{K}$$

(8)

• **Delay constraints:**
  For time-sensitive WSN applications, data must be successfully delivered to the SK within a certain amount of time or it would otherwise be useless. Let $L_k^s$ denote SR $k$’s number of bits (size of one message) to be delivered to the SK, and $L_k^s$ denote SR $k$’s number of bits (out of the $L_k^s$ bits) to be forwarded over flow $(i, j)^k$ at the rate $x_{ij}^k$. It easily follows, from the flow balance constraints given above, that $L_k^i = (x_{ij}^k / R_k)L_k^s$. Let $t_{ij}^k = L_k^s / x_{ij}^k$ be the time taken by $i$ to send SR $k$’s data over flow $(i, j)^k$ at the rate $x_{ij}^k$. Replacing $L_k^i$ by its value given above yields $t_{ij}^k = L_k^s / R_k$. Let $\tau_{ij}^k$ be the time needed by intermediate SR $i$ to forward all flows along the longest path from SR $k$ to its destined sink $s$. Note that the time it takes any intermediate SR $i$ to forward a SR $k$’s data bits to another SR $j$ is the same regardless of $i$ (same for all intermediate SRs) and regardless of $j$ (same for all SR $i$’s neighbors).

Let $\tau_k^h$ denote the time needed for the network to deliver SR $k$’s $L_k^s$ bits to the SK. Letting $h_k^k$ denote the number of hops along the longest path from SR $k$ to its destined sink, we can write $\tau_k^h = h_k^k \tau_k$.

Let $\tau_{th}$ be the maximum tolerable delay for every SR to deliver its messages to its SK. We then have

$$\tau_k^h \leq \tau_{th}; \quad \forall k \in \mathcal{N}.$$  

(9)

Let $\mathcal{P}_k^k$ be the set of all flows that when utilized to forward SR $k$’s bits, the maximum delay of SR $k$’s data delivery does not exceed the threshold, $\tau_{th}$ (i.e., inequality (9) is met). Thus, in order for SR $k$ to meet its delay bound, $x_{pq}^s = 0$ must hold for every $(p, q)^k \notin \mathcal{P}_k$ and every SK $s$. Note that if the network is required to deliver all messages to the SK in the least possible time, each SR must continuously and exclusively communicate with its fullest neighbor. In this case and because there will be only one possible routing path, the network lifetime can be straightforwardly calculated. We use $\tau_{min}$ to refer to this case throughout the paper.

B. Routing Formulation

The routing problem is now formulated into two linear programs: LP1 and LP2.

• **LP1:** Minimize $F$

  Subject to:

  - Flow balance constraints: (1)—(5)
  - Energy consumption constraints: (7)
  - Medium contention constraints: (8)
  - Delay constraints: (9)

  LP1 provides an optimal data rate vector $X$ that maximizes the network lifetime subject to all constraints.

• **LP2:** Minimize $F$

  Subject to:

  - Flow balance constraints: (1)—(5)
  - Energy consumption constraints: (7)
  - Medium contention constraints: (8)

  LP2 provides an optimal rate vector $X$ that maximizes the network lifetime subject to all except delay constraints. LP2 distributes the data traffic load between all flows to ensure efficient energy consumption and maximum network lifetime. The achieved lifetime with LP2 can be considered as an upper bound on the lifetime achieved under LP1.

V. System Performance

A. Simulation Setup

Simulation results are conducted using MATLAB. We consider LWSNs consisting of $N = 60$ SRs and $S = 50$ SKs. The network length is set to $l = 1000$ m and all nodes are deployed equidistantly along a straight line as described in Section III. We assume that the wireless medium capacity $W = 1$ bps, and each SR sends data bits at a rate of $R = 10^{-2}$ bps (i.e.,
$R_k = R = 10^{-2}$ for all SR $k$). We also assume that $L^k = L$ for all SR $k$ (and hence $\tau^k = \tau = L/R$ for all SR $k$). The maximum transmission range of each SR is $d = 100$m, and the maximum accepted delay is $\tau_{th} = 2\tau$. Each SR $k$ has initially an energy level of $B_k(t_0) = B = 10^5$ Joule. We study network lifetime behavior while considering the following metrics/effects:

- **Effect of MAC contention**: When maximizing lifetime without contention-awareness, the optimal data rates might not be practically feasible. Therefore, we study the behavior of the network lifetime with and without MAC constraints in a LWSN with a high traffic load.
- **Effect of SRs’ maximum transmission range**: The maximum transmission range of each SR is varied while the number of SRs and SKs is kept unchanged. Increasing the maximum transmission range will increase the number of neighbors of each SR; thus, additional flows will be available to be utilized for maximizing the network lifetime. The maximum transmission range is varied between 36m to 126m.
- **Effect of the number of SKs**: The number of SKs, $S$, is varied while the maximum transmission range and the number of SRs are kept the same. Increasing the number of SKs decreases the distance between nodes and the average number of SRs per section. Except for single-SK networks, each added SK increases the total number of sections by two and changes SRs association. Although the total generated data traffic in the network is unchanged, increasing the number of SKs will reduce the data traffic per SK. $S$ is varied from 5 to 26.
- **Effect of SR Density**: The number of SRs is varied while the maximum transmission range and number of SKs are unchanged. Increasing the number of SRs decreases the distance between nodes and increases the average number of SRs per section. The latter impact is less than when increasing the number of SKs because it does not change SRs associations and affects only the section where the new SR is placed in. Because each SR is sending data at a rate $R$, increasing the number of SRs will increase the total traffic in the network. Therefore, the total amount of traffic in the network is controlled by fixing the number of sending SRs. Let Sensor be an operating mode for active SRs in which active SRs will be generating their own data traffic and relaying other SRs’ data traffic as well, while Relay is the mode in which active SRs are not generating but only relaying other SRs’ data traffic. By fixing the number of Sensor SRs, the total amount of generated data in the network remains unchanged. All SRs in the Sensor mode are always assumed to be at the edge of each section furthest from SKs. Let $\eta$ denote SR density; i.e., $\eta = (N + S)/TD$.
- **Effect of network tolerance to SRs failure**: When maximizing the network lifetime for time-insensitive LWSN, the routing scheme will distribute the energy consumption between all SRs such that by the end of the network lifetime, the residual energy in each SR will be zero. When time sensitivity is important, the routing scheme will overuse some of the SRs in order to meet delay requirements and rapidly consume their energy. This will make the network non-operational—according to our definition of network lifetime—in despite of the amount of residual energy in the remaining active SRs. In this study, the validity of our network lifetime definition is examined by observing the amount of extra lifetime that can be achieved if the network is able to tolerate more than just the first failing SR. When a SR runs out of energy, it is ignored and new optimal data rates for the remaining network are determined. The new optimal data rates are calculated based on the status of the network when that SR ran out of energy. This is repeated until all SRs in a section run out of energy.

### B. Result Analysis

- **MAC contention**: Figure 3 illustrates the behavior of network lifetime against $\eta$. Initially at a lower density, each SR has only one neighbor; hence, there is only one possible routing path. Thus, MAC contention has no impact on lifetime. As density increases, SRs will have more neighbors and MAC contention will have an impact. The results here show that when considering MAC constraints, the network has a shorter lifetime compared to when MAC constraints are not considered. This is expected as having more constraints leads to less routing options, yielding smaller lifetimes. However, what is very important to mention here is that when not considering MAC constraints, the routing solution, though provides higher lifetime, may not actually be feasible. Similarly in figure 4, when varying the SR transmission range, the maximum achieved lifetime without considering MAC contention, expected to be higher due to lesser constraints, might not be feasible either.

- **SRs maximum transmission range**: Figure 5 shows the effect of increasing the maximum transmission range on lifetime. Recall that LP1 gives maximum network lifetime when delay constraints are considered; LP2 gives maximum lifetime but without considering delay constraints; and $\tau_{min}$ corresponds to achievable network lifetimes while ensuring the minimum possible delay. Although SRs are able to communicate with more neighbors when the transmission range is increased, the lifetime achieved under LP1 and LP2 does not increase significantly. This is because communicating with those new further-away neighbors has a
high energy cost, forcing the routing scheme to avoid communicating through them. On the other hand, the lifetime achieved when ensuring the minimum possible delay, $\tau_{min}$, decreases as the transmission range increases. This is expected because SRs are always communicating with furthest neighbors, and hence, as new neighbors come within their range (due to increasing the transmission range), they will immediately route all their data traffic through these new neighbors, thereby consuming more energy.

- **Number of SKs:** In figure 6, the network lifetime behaves similarly in all scenarios when the number of SKs is increased. When more SKs are added to the network, the distance between nodes decreases and so does the energy cost per flow. Additionally, the number of sections increases and SK associations of most SRs change. It is also observed that by adding more SKs, the lifetime achieved under LP1 approaches that achievable under LP2. This is because the average number of SRs per section decreases and delay constraints become less restrictive. This study can be useful for determining optimal numbers of SKs when designing LWSNs.

- **SR density:** Figure 7 illustrates the behavior of network lifetime when varying the number of SRs (i.e., SR density). It is observed that the lifetime achieved under LP2 is constantly increasing when more SRs are added to the network. This is expected as LP2 does not consider delay constraints, and the higher the number of nodes, the greater the chances of increasing network lifetime, provided here that the number of sending SRs is kept the same in the process of increasing the total number of SRs. By adding more SRs while not increasing the number of sending SRs, the network is basically provided with more energy resources. On the contrary, the lifetime achieved under LP1 remains about the same when the number of SRs is increased. This is because when distance between nodes decreases (due to increasing SR density), SRs consume less energy per the same flow, yielding a (slight) lifetime increase. By adding more SRs, eventually new neighbors will be available at the edge of the transmission range. Typically, those neighbors should be ignored but because delay is considered in LP1, SRs end up communicating with the new neighbors so as to satisfy delay constraints, thus decreasing the lifetime. By adding more SRs, the energy cost per each flow decreases and the network lifetime slightly increases again. As for the network lifetime achieved when ensuring the minimum possible delay, $\tau_{min}$, it exhibits behavior that is similar to what has been observed in figure 5, and the same explanations apply here as well. Overall, it is observed that for time-sensitive LWSNs (when delay constraints are considered), increasing the number of SRs does not always increase the network lifetime.
**Network tolerance to SR failure:** Figure 8 shows the lifetime behavior when assuming that the network can still be operational even when some SRs die; that is, when the network tolerates SR failure. First, note the network lifetime achievable under LP2 is the same because when maximizing lifetime without considering delay, the optimal rate solution is such that all nodes deplete their energy resources at the same time. For the network lifetime achieved when ensuring the minimum possible delay, the extension in network lifetime is minimal but slowly increasing. Since each SR will route its entire traffic to the same neighbor, few SRs in the middle of each section will lose their energy faster than others. This is because those SRs will be relaying more traffic. After few iterations and when the length of the isolated parts is longer than the transmission range of nodes, parts of each section will be isolated. This can be observed in figure 8 when the lifetime suddenly and significantly increases because the total traffic in the network dramatically decreases due to isolated sections. When considering the lifetime under LP1, the routing scheme will balance energy consumption so SRs will run out of energy in groups. The increase in lifetime is due to isolated sections and fewer active nodes in each section.

**VI. CONCLUSION**

This paper proposes contention-aware routing schemes for lifetime maximization in delay-constrained LWSNs. We first show that MAC contention awareness is important for data rate feasibility. We also show that increasing transmission range of SRs does not necessarily increase the lifetime. Moreover, we show that controlling SR maximum transmission energy levels is not needed since the optimal data rates will optimize energy consumption anyway. We also show that for time-sensitive LWSNs, increasing the number of SRs does not always increase the network lifetime since by increasing SR density per section, SRs will have to transmit to further neighbors to satisfy delay constraints and as a result, they consume more energy.

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