

2.3-4

In order to insert an element to a $(n - 1)$ sorted array, we need to identify the place to insert and then move the element there. $T(n) = T(n - 1) + (n - 1)$
 $T(n) = \Theta(n^2)$

2.3-5

refer to http://en.wikipedia.org/wiki/Binary_search_algorithm

2.3-6

We can use binary search to improve the time of identifying the place to insert, but it will still take $O(n)$ to move the elements to that place. Therefore, using binary search cannot improve the worst-case running time of insert sort to $\Theta(n \lg n)$

7.2-1

Assume $T(n) = \Theta(n^2)$, do induction as follows:

For base case, it is obviously true;

Suppose it is true for all $m < n$, we have

$T(n - 1) \leq c(n - 1)^2$, so

$T(n) \leq c(n - 1)^2 + c_1n = cn^2 + (c_1 - 2c)n + c \leq cn^2$, when $c_1 - 2c < 0$.

7.2-2

The case yields the worst-case partitioning, and recursion is

$T(n) = T(n - 1) + T(0) + \Theta(n)$

so we get $T(n) = \Theta(n^2)$

7.2-5

In the partition step, one part, say A, is reduced to α of the original size, and the other part, say B, is reduced to α of the original size, until the size reaches 1. Take A for example, suppose its depth is k, then we have $\alpha^k n = 1$, which yields $k = \log_\alpha 1/n = -\lg n / \lg \alpha$

Similar for B, we have $(1 - \alpha)^k n = 1$, which yields $k = -\lg n / \lg(1 - \alpha)$