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# Vulkan.

## Vulkan Ray Tracing – 5 New Shader Types!



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VulkanRayTracing457557.pptx

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Analog Ray Tracing Example ☺

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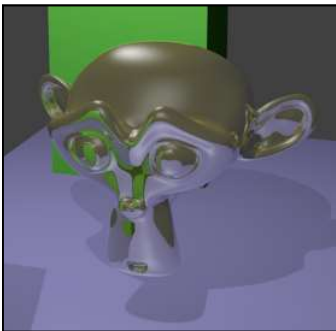
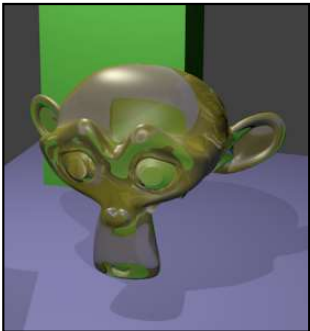


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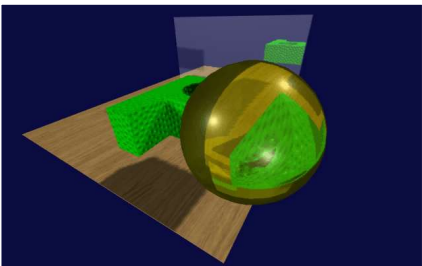
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### Digital Ray Tracing Examples

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Blender

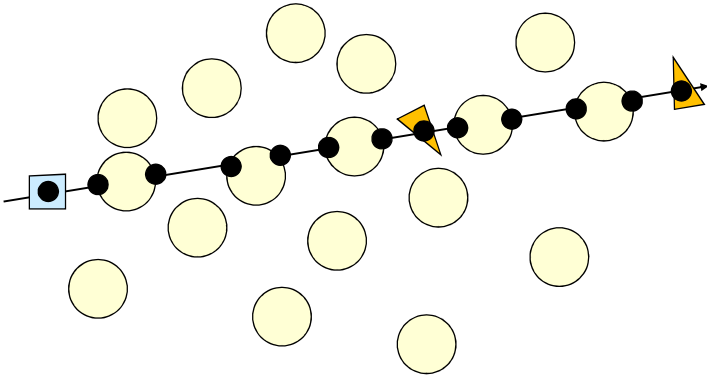


IronCad


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### In a Raytracing, each ray typically hits a lot of Things

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The diagram illustrates a ray starting from a light source (represented by a blue square) and passing through a series of yellow spheres. The ray is shown as a black line with black dots at each intersection point. The spheres are arranged in a path that curves upwards and then downwards. The ray starts from the left, passes through a square, then a series of spheres, and ends with a yellow triangle pointing right. The spheres are arranged in a path that curves upwards and then downwards.



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### Parametrizing a Ray

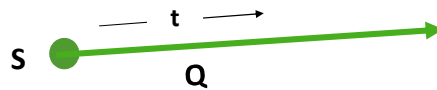
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**Given:**

**S** is the  $(x,y,z)$  starting point

**Q** is the  $(x,y,z)$  direction of travel

Then, the  $(x,y,z)$  position of a point **p** at some position along its direction of travel is:



$$p = S + tQ$$

$$t \geq 0.$$



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### Example: The Ray Intersection Process for a Sphere

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Sphere equation:  $(x-x_c)^2 + (y-y_c)^2 + (z-z_c)^2 = R^2$

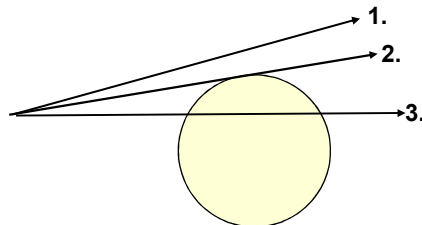
Ray equation:  $(x,y,z) = (x_0,y_0,z_0) + t^*(dx,dy,dz)$

Plugging  $(x,y,z)$  from the second equation into the first equation and multiplying-through and simplifying gives:

$$At^2 + Bt + C = 0 \quad \rightarrow \quad t_1, t_2 = \frac{-B \pm \sqrt{B^2 - 4AC}}{2A}$$

Solve for  $t_1, t_2$  and analyze the solution like this:

1. If both  $t_1$  and  $t_2$  are complex (i.e., have an imaginary component), then the ray missed the sphere completely.
2. If both  $t_1$  and  $t_2$  are real and identical, then the ray brushed the sphere at a tangent point.
3. If both  $t_1$  and  $t_2$  are real and different, then the ray entered and exited the sphere.



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### Parameterizing a Triangle

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It's often useful to be able to parameterize a triangle into  $(u,v)$ , like this:

Note! There is *no* place in this triangle where  $u = 1$  and  $v = 1$ .

$$p = P_0 + u*(P_1 - P_0) + v*(P_2 - P_0)$$

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### The Setup

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We want to find out where the ray intersects the triangle.  
That is, where is the point  $p$  that is common to both the ray and the triangle?

Such that:

$$t \geq 0.$$

$$0 \leq u \leq 1.$$

$$0 \leq v \leq 1 - u$$

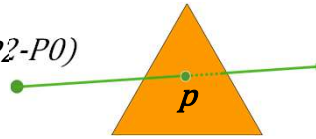
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## Equation Setup

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Triangle:  $p = P0 + u*(P1-P0) + v*(P2-P0)$

Ray:  $p = S + tQ$



Re-arranging:

$$P0 + u*(P1-P0) + v*(P2-P0) = S + tQ$$

Re-arranging some more:

$$-tQ + u*(P1-P0) + v*(P2-P0) = S - P0$$

Then collecting terms, we get:

$$At + Bu + Cv = D$$

where:

$$A = -Q$$

$$B = P1-P0$$

$$C = P2-P0$$

$$D = S - P0$$



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## Three Equations, Three Unknowns

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Remembering that this equation is really 3 equations in (x,y,z):

$$At + Bu + Cv = D$$

we have 3 equations with 3 unknowns, which can be cast into a matrix form

$$\begin{bmatrix} A_x & B_x & C_x \\ A_y & B_y & C_y \\ A_z & B_z & C_z \end{bmatrix} \begin{Bmatrix} t \\ u \\ v \end{Bmatrix} = \begin{Bmatrix} D_x \\ D_y \\ D_z \end{Bmatrix}$$

Our goal is to solve this for  $t^*$ ,  $u^*$ , and  $v^*$



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**Solve for (t\*,u\*,v\*) using Cramer's Rule** 11


$$\begin{bmatrix} A_x & B_x & C_x \\ A_y & B_y & C_y \\ A_z & B_z & C_z \end{bmatrix} \begin{pmatrix} t \\ u \\ v \end{pmatrix} = \begin{pmatrix} D_x \\ D_y \\ D_z \end{pmatrix}$$

$$D_0 = \det \begin{bmatrix} A_x & B_x & C_x \\ A_y & B_y & C_y \\ A_z & B_z & C_z \end{bmatrix}$$

$$D_t = \det \begin{bmatrix} D_x & B_x & C_x \\ D_y & B_y & C_y \\ D_z & B_z & C_z \end{bmatrix} \quad t^* = \frac{D_t}{D_0}$$





$$D_u = \det \begin{bmatrix} A_x & D_x & C_x \\ A_y & D_y & C_y \\ A_z & D_z & C_z \end{bmatrix} \quad u^* = \frac{D_u}{D_0}$$


$$D_v = \det \begin{bmatrix} A_x & B_x & D_x \\ A_y & B_y & D_y \\ A_z & B_z & D_z \end{bmatrix} \quad v^* = \frac{D_v}{D_0}$$



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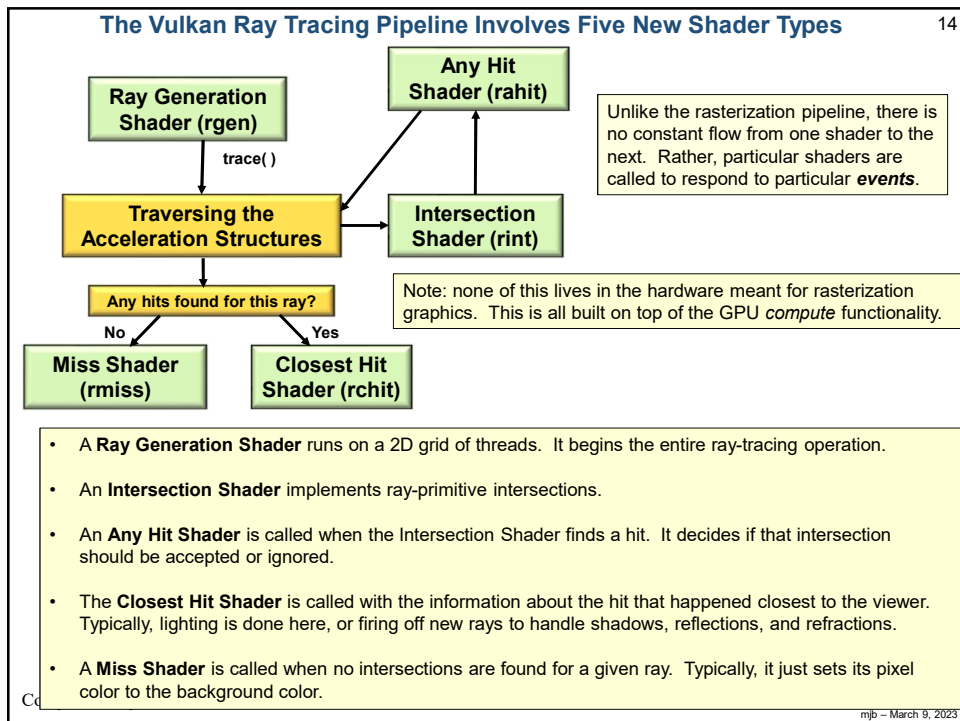
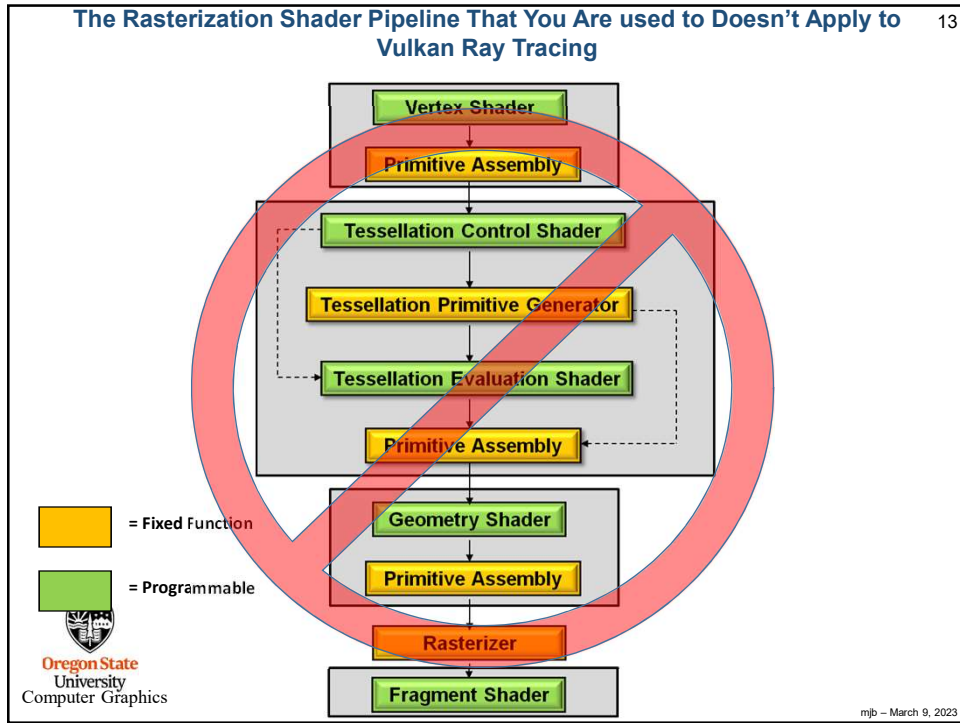
**The Steps** 12

1. Compute  $D_0$
2. If  $D_0 \approx 0.$ , then the ray is *parallel* to the plane of the triangle 
3. Compute  $D_t$
4. Compute  $t^*$
5. If  $t^* < 0.$ , the ray goes away from the triangle 
6. Compute  $D_u$
7. Compute  $u^*$
8. If  $u^* < 0.$  or  $u^* > 1.$ , then the ray hits outside the triangle 
9. Compute  $D_v$
10. Compute  $v^*$
11. If  $v^* < 0.$  or  $v^* > 1.-u^*$ , then the ray hits outside the triangle 
12. The intersection is at the point  $p = S + Qt^*$



This is known as the **Möller-Trumbore Triangle Intersection Algorithm**

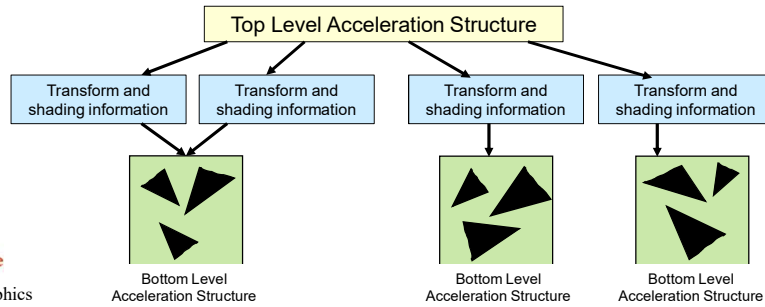
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### Acceleration Structures

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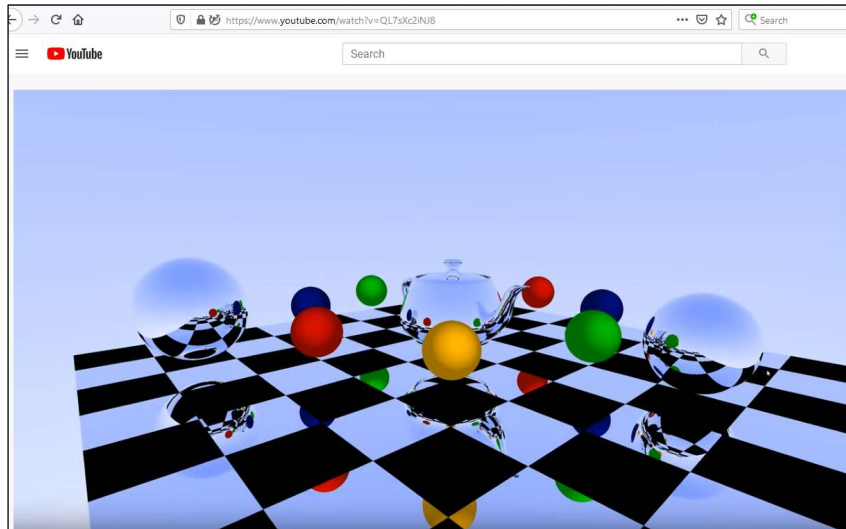
- A Bottom-level Acceleration Structure (BLAS) reads the vertex data from vertex and index VkBuffers to determine bounding boxes.
- You can also supply your own bounding box information to a BLAS.
- A Top-level Acceleration Structure (TLAS) holds transformations and pointers to multiple BLASes.
- The BLAS is essentially used as a Model Coordinate bounding box, while the TLAS is used as a World Coordinate bounding box.



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### Check This Out!

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<https://www.youtube.com/watch?v=QL7sXc2iNJ8>



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