

Vulkan.

Vulkan Ray Tracing – 5 New Shader Types!



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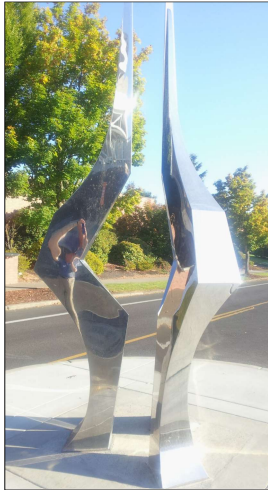





VulkanRayTracing457587.pptx

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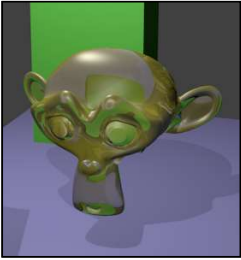
Analog Ray Tracing Example ☺

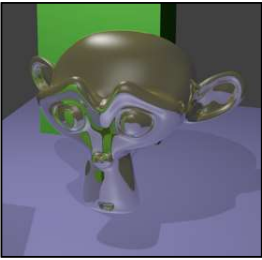




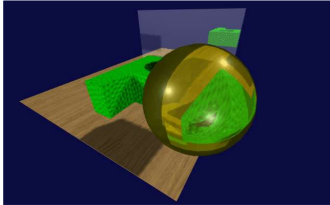
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Digital Ray Tracing Examples






Blender

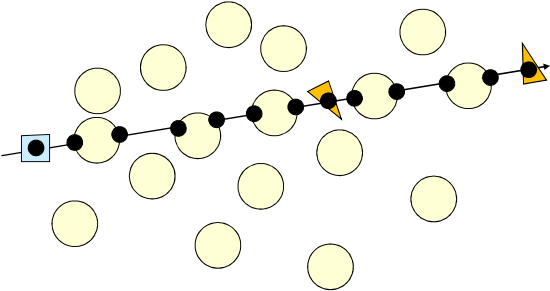



IronCad



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In a Raytracing, each ray typically hits a lot of Things





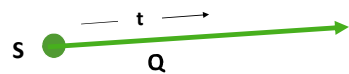
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Parametrizing a Ray


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Given:
S is the (x,y,z) starting point
Q is the (x,y,z) direction of travel

Then, the (x,y,z) position of a point **p** at some position along its direction of travel is:



$$p = S + tQ$$

$$t \geq 0.$$


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Example: The Ray Intersection Process for a Sphere

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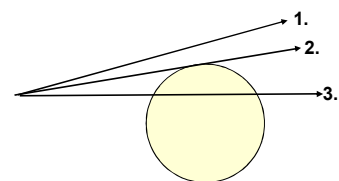

Sphere equation: $(x-x_c)^2 + (y-y_c)^2 + (z-z_c)^2 = R^2$
 Ray equation: $(x,y,z) = (x_0,y_0,z_0) + t(dx,dy,dz)$

Plugging (x,y,z) from the second equation into the first equation and multiplying-through and simplifying gives:

$$At^2 + Bt + C = 0 \quad \rightarrow \quad t_1, t_2 = \frac{-B \pm \sqrt{B^2 - 4AC}}{2A}$$

Solve for t_1, t_2 and analyze the solution like this:

1. If both t_1 and t_2 are complex (i.e., have an imaginary component), then the ray missed the sphere completely.
2. If both t_1 and t_2 are real and identical, then the ray brushed the sphere at a tangent point.
3. If both t_1 and t_2 are real and different, then the ray entered and exited the sphere.

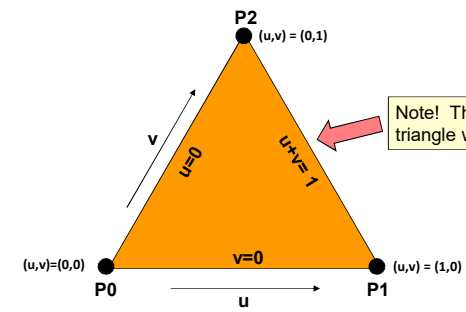



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Parameterizing a Triangle

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It's often useful to be able to parameterize a triangle into (u,v), like this:



Note! There is *no* place in this triangle where $u = 1$ and $v = 1$.

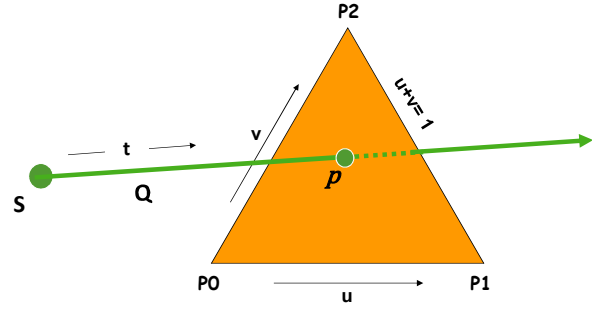
$$p = P0 + u*(P1-P0) + v*(P2-P0)$$


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The Setup

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We want to find out where the ray intersects the triangle.
 That is, where is the point **p** that is common to both the ray and the triangle?




Such that:

$$t \geq 0.$$

$$0 \leq u \leq 1.$$

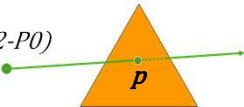
$$0 \leq v \leq 1-u.$$



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Equation Setup

Triangle: $p = P0 + u*(P1-P0) + v*(P2-P0)$
 Ray: $p = S + tQ$



Re-arranging:
 $P0 + u*(P1-P0) + v*(P2-P0) = S + tQ$

Re-arranging some more:
 $-tQ + u*(P1-P0) + v*(P2-P0) = S - P0$


Then collecting terms, we get:
 $At + Bu + Cv = D$

where:

$$A = -Q$$

$$B = P1-P0$$

$$C = P2-P0$$

$$D = S - P0$$


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Three Equations, Three Unknowns


Remembering that this equation is really 3 equations in (x,y,z):

$$At + Bu + Cv = D$$

we have 3 equations with 3 unknowns, which can be cast into a matrix form

$$\begin{bmatrix} A_x & B_x & C_x \\ A_y & B_y & C_y \\ A_z & B_z & C_z \end{bmatrix} \begin{Bmatrix} t \\ u \\ v \end{Bmatrix} = \begin{Bmatrix} D_x \\ D_y \\ D_z \end{Bmatrix}$$

Our goal is to solve this for t*, u*, and v*



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Solve for (t*,u*,v*) using Cramer's Rule

$$\begin{bmatrix} A_x & B_x & C_x \\ A_y & B_y & C_y \\ A_z & B_z & C_z \end{bmatrix} \begin{Bmatrix} t \\ u \\ v \end{Bmatrix} = \begin{Bmatrix} D_x \\ D_y \\ D_z \end{Bmatrix}$$

$$D_0 = \det \begin{bmatrix} A_x & B_x & C_x \\ A_y & B_y & C_y \\ A_z & B_z & C_z \end{bmatrix}$$





$$D_t = \det \begin{bmatrix} D_x & B_x & C_x \\ D_y & B_y & C_y \\ D_z & B_z & C_z \end{bmatrix} \quad t^* = \frac{D_t}{D_0}$$

$$D_u = \det \begin{bmatrix} A_x & D_x & C_x \\ A_y & D_y & C_y \\ A_z & D_z & C_z \end{bmatrix} \quad u^* = \frac{D_u}{D_0}$$


$$D_v = \det \begin{bmatrix} A_x & B_x & D_x \\ A_y & B_y & D_y \\ A_z & B_z & D_z \end{bmatrix} \quad v^* = \frac{D_v}{D_0}$$


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The Steps

1. Compute D_0
2. If $D_0 \approx 0$., then the ray is *parallel* to the plane of the triangle 
3. Compute D_t
4. Compute t^*
5. If $t^* < 0$., the ray goes away from the triangle 
6. Compute D_u
7. Compute u^*
8. If $u^* < 0$. or $u^* > 1$., then the ray hits outside the triangle 
9. Compute D_v
10. Compute v^*
11. If $v^* < 0$. or $v^* > 1-u^*$., then the ray hits outside the triangle 
12. The intersection is at the point $p = S + Qt^*$

Oregon State University Computer Graphics: This is known as the **Möller-Trumbore Triangle Intersection Algorithm**



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