Vertex Buffer Objects: The Big Idea

- Store vertex coordinates and vertex attributes on the **graphics card**.
- Optionally store the connections on the graphics card too.
- Every time you go to redraw, coordinates will be pulled from GPU memory, avoiding a potentially significant amount of bus latency.

```
static GLfloat CubeVertices[33] = {
    { -1.0, -1.0, -1.0 },
    { -1.0, -1.0,  1.0 },
    { -1.0,  1.0, -1.0 },
    { -1.0,  1.0,  1.0 },
    {  1.0, -1.0, -1.0 },
    {  1.0, -1.0,  1.0 },
    {  1.0,  1.0, -1.0 },
    {  1.0,  1.0,  1.0 },
};

static GLfloat CubeColors[39] = {
    { 0.0, 0.0, 0.0 },
    { 1.0, 0.0, 0.0 },
    { 0.0, 1.0, 0.0 },
    { 1.0, 1.0, 0.0 },
    { 0.0, 0.0, 1.0 },
    { 1.0, 0.0, 1.0 },
    { 0.0, 1.0, 1.0 },
    { 1.0, 1.0, 1.0 },
};

static GLuint& CubeQuadsIndices[4] = {
    { 0, 2, 3, 1 },
    { 4, 5, 6 },
    { 1, 3, 7, 5 },
    { 0, 4, 6, 2 },
    { 2, 6, 7, 3 },
    { 0, 1, 5, 4 },
};
```
The Cube Can Also Be Defined with Triangles

```c
GLuint CubeQuadIndices[4] = {
    { 0, 2, 3, 1 },
    { 4, 5, 7, 6 },
    { 1, 3, 7, 5 },
    { 0, 4, 6, 2 },
    { 2, 6, 7, 3 },
    { 0, 1, 5, 4 }
};

GLuint CubeTriangleIndices[3] = {
    { 0, 2, 3 },
    { 0, 3, 1 },
    { 4, 7, 6 },
    { 1, 3, 7 },
    { 1, 7, 5 },
    { 0, 4, 6 },
    { 0, 6, 2 },
    { 2, 6, 7 },
    { 2, 7, 3 },
    { 0, 1, 5 },
    { 0, 5, 4 }
};
```

Did any of you ever watch *Star Trek: Deep Space Nine*?

It was about life aboard a space station. Ships docked there to unload cargo and pick up supplies. When a ship was docked at docking port “A”, for instance, the supply-loaders didn’t need to know what ship it was. They could just be told, “send these supplies out docking port A, and pick up this cargo from docking port A”.

Surprisingly, this has something to do with computer graphics!
The OpenGL Rendering Context

The OpenGL Rendering Context (also called “the state”) contains all the characteristic information necessary to produce an image from geometry. This includes the current transformation, color, lighting, textures, where to send the display, etc.

Each window (e.g., glutCreateWindow) has its own rendering context.

More Background – “Binding” to the Context

The OpenGL term “binding” refers to “attaching” or “docking” (a metaphor which I find to be more visually pleasing) an OpenGL object to the Context. You can then assign characteristics, and they will “flow in” through the Context into the object.

Ships docked there to unload cargo and pick up supplies. When a ship was docked at docking port “A”, for instance, the supply-loaders didn’t need to know what ship it was. They could just be told, “send these supplies out docking port A, and pick up this cargo from docking port A.”
More Background – “Binding” to the Context

When you want to use that Vertex Buffer Object, just bind it again. All of the characteristics will then be active, just as if you had specified them again. Its contents will “flow out” of the object into the Context.

```c
glBindBuffer( GL_ARRAY_BUFFER, bufA);
glDrawArrays( GL_TRIANGLES, 0, numVertices );
```

If you were writing OpenGL in C, how would you implement the State?

You would probably make all of that information into a big C struct

```c
struct OpenGLState
{
    float  CurrentColor[3];
    float  CurrentLineWidth;
    float  CurrentMatrix[4][4];

    struct TextureObject  *CurrentTexture0;
    struct ArrayBufferObject  *CurrentArrayBuffer;
    
    
} TheState;
```
If you were writing OpenGL in C, how would you implement the State?

Then, you could create any number of Array Buffer Objects, each with its own data and parameters. When you want to make a particular Array Buffer current, you just need to "bind" it to the state:

```
TheState.CurrentArrayBuffer = GpuAddressOf(bufA);
```

and, when you want to do something with it or to it, you just need to do an indirection:

```
TheState.CurrentBuffer->data[0].x = 42.0;
```

More Background – How do you Create an OpenGL “Buffer Object”?

When creating data structures in C++, objects are pointed to by their addresses.

In OpenGL, objects are pointed to by an unsigned integer “handle”. You can assign a value for this handle yourself (not recommended), or have OpenGL generate one for you that is guaranteed to be unique. For example:

```
GLuint bufA;
glGenBuffers( 1, &bufA );
```

OpenGL then uses these handles to determine the actual GPU memory addresses to use.
Loading data into the currently-bound Vertex Buffer Object

```c
glBufferData( type, numBytes, data, usage );
```

*type* is the type of buffer object this is:

Use `GL_ARRAY_BUFFER` to store floating point vertices, normals, colors, and texture coordinates.

*numBytes* is the number of bytes to store all together. It’s not the number of numbers, not the number of coordinates, not the number of vertices, but the number of bytes!

*data* is the memory address of (i.e., pointer to) the data to be transferred from CPU memory to the graphics memory. (This is allowed to be NULL, indicating that you will transfer the data over later.)

---

Loading data into the currently-bound Vertex Buffer Object

```c
glBufferData( type, numBytes, data, usage );
```

*usage* is a hint as to how the data will be used: `GL_xxx_yyy`

where *xxx* can be:

- `STATIC` this buffer will be re-written seldom
- `DYNAMIC` this buffer will be re-written often

and *yyy* can be:

- `DRAW` this buffer will be used for drawing
- `READ` this buffer will be copied into

For what we are doing in most classes, use `GL_STATIC_DRAW`

---

Adding data into the current Vertex Buffer Object

```c
glBufferSubData( type, offset, numBytes, data );
```
**Step #1 – Fill the C/C++ Arrays with Drawing Data (vertices, colors, ...)**

```c
GLfloat Vertices[ ][3] =
{
    { 1., 2., 3. },
    { 4., 5., 6. },
    ...
};
```

**Step #2 – Transfer the Drawing Data**

```c
glGenBuffers( 1, &bufA );

glBindBuffer( GL_ARRAY_BUFFER, bufA );
glBufferData( GL_ARRAY_BUFFER, 3*sizeof(GLfloat)*numVertices, Vertices, GL_STATIC_DRAW );
```

**Step #3 – Activate the Drawing Data Types That You Are Using**

```c
glEnableClientState( type )
```

where `type` can be any of:

- GL_VERTEX_ARRAY
- GL_COLOR_ARRAY
- GL_NORMAL_ARRAY
- GL_TEXTURE_COORD_ARRAY

- Call this as many times as you need to enable all the drawing data types that you are using.
- To deactivate a type, call:

```c
glDisableClientState( type )
```
Step #4 – To start the drawing process, bind the Buffer that holds the Drawing Data

```c
glBindBuffer( GL_ARRAY_BUFFER, bufA );
```

Step #5 – Then, specify how to get at each Data Type within that Buffer

```c
glVertexPointer( size, type, stride, offset);
glColorPointer( size, type, stride, offset);
glNormalPointer( type, stride, offset);
glTexCoordPointer( size, type, stride, offset);
```

- `size` is the “how many numbers per vertex”, and can be: 2, 3, or 4
- `type` can be:
  - `GL_SHORT`
  - `GL_INT`
  - `GL_FLOAT`
  - `GL_DOUBLE`
- `stride` is the byte offset between consecutive entries in the buffer (0 means tightly packed)
- `offset` is the byte offset from the start of the data array buffer to where the first element of this part of the data lives.
The Data Types in a vertex buffer object can be stored either as “packed” or “interleaved”

Packed:
```
glVertexPointer( 3, GL_FLOAT, 3*sizeof(GLfloat), 0 );
glColorPointer( 3, GL_FLOAT, 3*sizeof(GLfloat), 3*sizeof(float) );
```

Interleaved:
```
glVertexPointer( 3, GL_FLOAT, 6*sizeof(GLfloat), 0 );
glColorPointer( 3, GL_FLOAT, 6*sizeof(GLfloat), 3*sizeof(float) );
```

Step #6 – Draw!
```
glDrawArrays( GL_TRIANGLES, first, numVertices );
```

Example:
```
glDrawArrays( GL_TRIANGLES, 0, 6 );
```

This is how you do it if your vertices are to be drawn in consecutive order
What if your vertices are to be accessed in random order?

```
GLfloat CubeVertices[][3] =
{
    {-1., -1., -1.},
    { 1., -1., -1.},
    {-1.,  1., -1.},
    { 1.,  1., -1.},
    {-1., -1.,  1.},
    { 1., -1.,  1.},
    {-1.,  1.,  1.},
    { 1.,  1.,  1.}
};
```

```
GLfloat CubeColors[][3] =
{
    { 0., 0., 0.},
    { 1., 0., 0.},
    { 0., 1., 0.},
    { 1., 1., 0.},
    { 0., 0., 1.},
    { 1., 0., 1.},
    { 0., 1., 1.},
    { 1., 1., 1.}
};
```

```
GLuint CubeQuadIndices[][4] =
{
    {0, 2, 3, 1},
    {4, 5, 7, 6},
    {1, 3, 7, 5},
    {0, 4, 6, 2},
    {2, 6, 7, 3},
    {0, 1, 5, 4}
};
```

Cube Example
glEnableClientState( GL_VERTEX_ARRAY );
glEnableClientState( GL_COLOR_ARRAY );
glVertexPointer( 3, GL_FLOAT, 0, (Gluchar*) 0 );
glColorPointer( 3, GL_FLOAT, 0, (Gluchar*) (3*sizeof(GLfloat)*numVertices) );
gBegin( GL_QUADS )
   glArrayElement( 0 );
   glArrayElement( 2 );
   glArrayElement( 3 );
   glArrayElement( 1 );
   glArrayElement( 4 );
   glArrayElement( 5 );
   glArrayElement( 7 );
   glArrayElement( 6 );
   glArrayElement( 1 );
   glArrayElement( 3 );
   glArrayElement( 7 );
   glArrayElement( 5 );
   glArrayElement( 0 );
   glArrayElement( 4 );
   glArrayElement( 6 );
   glArrayElement( 2 );
   glArrayElement( 2 );
   glArrayElement( 6 );
   glArrayElement( 7 );
   glArrayElement( 3 );
   glArrayElement( 0 );
   glArrayElement( 1 );
   glArrayElement( 5 );
   glArrayElement( 4 );
gEnd( );

GLuint CubeQuadIndices[ ][4] = {
   { 0, 2, 3, 1 },
   { 4, 5, 7, 6 },
   { 1, 3, 7, 5 },
   { 0, 4, 6, 2 },
   { 2, 6, 7, 3 },
   { 0, 1, 5, 4 }
};

But, it would be better if that index array was over on the GPU as well

glBindBuffer( GL_ARRAY_BUFFER, bufA );
glBufferData( GL_ARRAY_BUFFER, 3*sizeof(GLfloat)*numVertices, Vertices, GL_STATIC_DRAW );

gBindBuffer( GL_ELEMENT_ARRAY_BUFFER, bufB );
glBufferData( GL_ELEMENT_ARRAY_BUFFER, sizeof(GLuint)*numIndices, CubeIndices, GL_STATIC_DRAW );
The `glDrawElements()` call

```c
glBindBuffer( GL_ARRAY_BUFFER, bufA );
glBindBuffer( GL_ELEMENT_ARRAY_BUFFER, bufB );

glEnableClientState( GL_VERTEX_ARRAY );
glEnableClientState( GL_COLOR_ARRAY );

glVertexPointer( 3, GL_FLOAT, 0, (Gluchar*) 0 );
glColorPointer( 3, GL_FLOAT, 0, (Gluchar*) (3*sizeof(GLfloat)*numVertices) );

glDrawElements( GL_QUADS, 24, GL_UNSIGNED_INT, (Gluchar*) 0 );
```

---

Re-writing Data into a Buffer Object, Treating it as a C/C++ Array of Structures

```c
float * vertexArray = glMapBuffer( GL_ARRAY_BUFFER, usage );
```

`usage` is how the data will be accessed:

- **GL_READ_ONLY** the vertex data will be read from, but not written to
- **GL_WRITE_ONLY** the vertex data will be written to, but not read from
- **GL_READ_WRITE** the vertex data will be read from and written to

You can now use `vertexArray[ ]` like any other C/C++ floating-point array of structures.

When you are done, be sure to call:

```
glUnMapBuffer( GL_ARRAY_BUFFER );
```
Using a Vertex Buffer Object C++ Class

Declaring:
VertexBufferObject VB;

Filling:
VB.glBegin( GL_QUADS ); // can be any of the OpenGL topologies
for( int i = 0; i < 6; i++ )
{
    for( int j = 0; j < 4; j++ )
    {
        int k = CubeIndices[ i ][ j ];
        VB.glColor3fv( CubeColors[ k ] );
        VB.glVertex3fv( CubeVertices[ k ] );
    }
}
VB.glEnd( );

Drawing:
VB.Draw( );

VertexBufferObject Class Methods

void CollapseCommonVertices( bool );
  true means to not replicate common vertices in the internal
  vertex table. This is good if all uses of a particular vertex
  will have the same normal, color, and texture coordinates,
  like this – instead of like this.

void Draw( );
  Draw the primitive. If this is the first time Draw( ) is being
called, it will setup all the proper buffer objects, etc. If it as
a subsequent call, then it will just initate the drawing.

void glBegin( topology);
  Initiate the primitive.

void glColor3f( r, g, b);

void glColor3fv( rgb[ 3 ] );
  Specify a vertex’s color.

void glEnd( );
  Terminate the definition of a primitive.

void glNormal3f( nx, ny, nz );
  Specify a vertex’s normal.

void glNormal3fv( nxyz[ 3 ] );
**Vertex Buffer Object Class Methods**

- **void glTexCoord2f( s, t );**
  - Specify a vertex's texture coordinates.

- **void glTexCoord2fv( st[ 2 ];**
  - Specify a vertex's coordinates.

- **void glVertex3f( x, y, z);**
  - Specify a vertex's coordinates.

- **void glVertex3fv( xyz[ 3 ];**
  - Specify a vertex's coordinates.

- **void Print( char *text, FILE * );**
  - Prints the vertex, normal, color, texture coordinate, and connection element information to a file, along with some preliminary text. If the file pointer is not given, standard error (i.e., the console) is used.

- **void RestartPrimitive( );**
  - Causes the primitive to be restarted. This is useful when doing triangle strips or quad strips and you want to start another one without getting out of the current one. By doing it this way, all of the strips' vertices will end up in the same table, and you only need to have one VertexBufferObject class going.

**Notes**

- If you want to print the contents of your data structure to a file (for debugging or curiosity), do this:

  ```c
  FILE *fp = fopen( "debuggingfile.txt", "w" );
  if( fp == NULL )
  {
    fprintf( stderr, "Cannot create file 'debuggingfile.txt'
    );
  }
  else
  {
    VB.Print( "My Vertex Buffer :", fp );
    fclose( fp );
  }
  ```

- You can call the glBegin method more than once. Each call will wipe out your original display information and start over from scratch. This is useful if you are interactively editing geometry, such as sculpting a curve.

- In many cases, using standard glBegin( ) – glEnd( ) in a display list can be just about as fast as using vertex buffer objects if the vendor has written the drivers to create the display list on the graphics card. But, the vendors don’t always do this. You’re better off using vertex buffer objects because they are always fast.
A Caveat

Be judicious about collapsing common vertices! The good news is that it saves space and it might increase speed some (by having to transform fewer vertices). But, the bad news is that it takes much longer to create large meshes. Here’s why.

Say you have a 1,000 x 1,000 point triangle mesh, drawn as 999 triangle strips, all in the same VertexBufferObject class (which you can do using the RestartPrimitive method).

When you draw the Sth triangle strip, half of those points are coincident with points in the S-1st strip. But, to find those 1,000 coincident points, it must search through 1000*S points first. There is no way to tell it to only look at the last 1,000 points. Even though the search is only $O(\log N)$, where N is the number of points kept so far, it still adds up to a lot of time over the course of the entire mesh.

It starts out fast, but slows down as the number of points being held increases.

If you did have a 1,000 x 1,000 mesh, it might be better to not collapse vertices at all. Or, a compromise might be to collapse vertices, but break this mesh up into 50 VertexBufferObjects, each of size 20 x 1,000.

Just a thought…

Drawing the Cube With Collapsing Identical Vertices

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Drawing 24 array elements:

0 1 2 3
4 5 6 7
8 9 10 11
12 13 14 15

mjb – August 21, 2018
## Drawing the Cube Without Collapsing Identical Vertices

### Drawing 24 points

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### Drawing 24 array elements:

0 1 2
4 5 6
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12 13 14 15
16 17 18 19
20 21 22 23

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## A Comparison

### Not Collapsing Identical Vertices

### Drawing 24 points

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### Drawing 24 array elements:

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### Collapsing Identical Vertices

### Drawing 8 points

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### Drawing 24 array elements:

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Using Vertex Buffers with Shaders

Let's say that we have the following vertex shader and we want to supply the vertices from a Buffer Object.

```glsl
in vec3 aVertex;
in vec3 aColor;
out vec3 vColor;
void
main( )
{
    vColor = aColor;
    gl_Position = gl_ModelViewProjectionMatrix * vec4( aVertex, 1. );
}
```

Let's also say that, at some time, we want to supply the colors from a Buffer Object as well, but for right now, the color will be constant.

```glsl
glBindBuffer( GL_ARRAY_BUFFER, vertexBuffer );
glEnableClientState( GL_VERTEX_ARRAY );
glEnableClientState( GL_COLOR_ARRAY  );
GLuint vertexLocation = glGetAttribLocation( program, "aVertex" );
GLuint colorLocation = glGetAttribLocation( program, "aColor" );
glVertexAttribPointer( vertexLocation, 3, GL_FLOAT, GL_FALSE, 0, (GLuchar *)&0 );
glEnableVertexAttribArray( vertexLocation ); // dynamic attribute
glVertexAttrib3f( colorLocation,  r, g, b ); // static attribute
glDisableVertexAttribArray( colorLocation );
glDrawArrays( GL_TRIANGLES,  0,  3*NumTris );
```

Using Vertex Buffers with Shaders

We're assuming here that we already have the shader program setup in `program`, and already have the vertices in the `vertexBuffer`. 
Using Vertex Buffers with the Shaders C++ Class

We're assuming here that we already have the shader program setup in program, and already have the vertices in the vertexBuffer.

```c
void renderScene() {
    glBindBuffer( GL_ARRAY_BUFFER, vertexBuffer );
    glEnableClientState( GL_VERTEX_ARRAY );
    glEnableClientState( GL_COLOR_ARRAY );

    Pattern->SetVertexAttributePointer3fv( "aVertex", (GLfloat *)0 );
    Pattern->EnableVertexAttribArray( "aVertex" ); // dynamic attribute

    Pattern->SetVertexAttributeVariable( "aColor", r, g, b ); // static attribute
    Pattern->DisableVertexAttribArray( "aColor" );

    glDrawArrays( GL_TRIANGLES, 0, 3*NumTris );
}
```