Computer Graphics Lighting

Why Do We Care About Lighting?

Lighting "dis-ambiguates" 3D scenes

Without lighting

With lighting
**The Surface Normal**

A **surface normal** is a vector perpendicular to the surface.

Sometimes surface normals are defined or computed **per-face**, like this.

\[ n = ( P1 - P0 ) \times ( P2 - P0 ) \]

Sometimes they are defined **per-vertex**, like this, to best approximate the underlying surface that the face is representing.

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**Setting a Per-Face Surface Normal in OpenGL**

```gl
glMatrixMode( GL_MODELVIEW );

glTranslatef( tx, ty, tz );
glRotatef( degrees, ax, ay, az );
glScalef( sx, sy, sz );

glNormal3f( nx, ny, nz );
```

```gl
Per-face
```

```gl
glColor3f( r, g, b );
glBegin( GL_TRIANGLES );
    glVertex3f( x0, y0, z0 );
    glVertex3f( x1, y1, z1 );
    glVertex3f( x2, y2, z2 );
glEnd();
```
### Setting Per-Vertex Surface Normals in OpenGL

```c
glMatrixMode( GL_MODELVIEW );

glTranslatef( tx, ty, tz );
glRotatef( degrees, ax, ay, az );
glScalef( sx, sy, sz );

Per-vertex

glColor3f( r, g, b );
gBegin(GL_TRIANGLES );
    glNormal3f( nx0, ny0, nz0 );
glVertex3f( x0, y0, z0 );
    glNormal3f( nx1, ny1, nz1 );
glVertex3f( x1, y1, z1 );
    glNormal3f( nx2, ny2, nz2 );
glVertex3f( x2, y2, z2 );
gEnd( );
```

### Flat Shading (Per-face)

```c
glMatrixMode( GL_MODELVIEW );

Per-face

glTranslatef( tx, ty, tz );
glRotatef( degrees, ax, ay, az );
glScalef( sx, sy, sz );

Per-face

glShadeModel( GL_FLAT );
glNormal3f( nx, ny, nz );

Per-face

gColor3f( r, g, b );
gBegin(GL_TRIANGLES );
    glVertex3f( x0, y0, z0 );
    glVertex3f( x1, y1, z1 );
    glVertex3f( x2, y2, z2 );
gEnd( );
```
glMatrixMode(GL_MODELVIEW);

glTranslatef(tx, ty, tz);
glRotatef(degrees, ax, ay, az);
glScalef(sx, sy, sz);

**glShadeModel(GL_SMOOTH);**

glColor3f(r, g, b);
glBegin(GL_TRIANGLES);
glNormal3f(nx0, ny0, nz0);
glVertex3f(x0, y0, z0);
glNormal3f(nx1, ny1, nz1);
glVertex3f(x1, y1, z1);
glNormal3f(nx2, ny2, nz2);
glVertex3f(x2, y2, z2);
glEnd();
OpenGL Surface Normals Need to be Unitized by Someone

```c
glTranslatef( tx, ty, tz );
glRotatef( degrees, ax, ay, az );
glScalef( sx, sy, sz );
glNormal3f( nx, ny, nz );
```

OpenGL expects the normal vector to be a **unit vector**, that is: $nx^2 + ny^2 + nz^2 = 1$

If it is not, or if you are using scaling transformations, you can force OpenGL to do the unitizing for you with:

```c
glEnable( GL_NORMALIZE );
```

---

The OpenGL “built-in” Lighting Model

- **I**: Light intensity
- **L**: Unit vector from point to light
- **n**: Unit vector surface normal
- **R**: Perfect reflection unit vector
- **E**: Unit vector to eye position
- **P**: Point being illuminated
1. **Ambient** = a constant
   Accounts for light bouncing “everywhere”

2. **Diffuse** = \( I \cdot \cos \Theta \)
   Accounts for the angle between the incoming light and the surface normal

3. **Specular** = \( I \cdot \cos^S \phi \)
   Accounts for the angle between the “perfect reflector” and the eye. The exponent, \( S \), accounts for surface shininess

Note that \( \cos \Theta \) is just the dot product between unit vectors \( L \) and \( n \)

Note that \( \cos \phi \) is just the dot product between unit vectors \( R \) and \( E \)

---

**You are all familiar with the Diffuse Lighting effects**

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![Image of a coffee cup](image-url)
Diffuse Lighting actually works because of spreading out the same amount of light energy across more surface area.

\[ \text{Diffuse} = I \cdot \cos \theta \]

You are all familiar with the Specular Lighting effects. These all have metallic-looking surfaces. What tells you that?

It's the shiny-reflection spots.
You are all familiar with the Specular Lighting effects.

These are not actually metal. They are wood with special paint that mimics the metallic reflection highlights. We can mimic the same effects digitally!

The Specular Lighting equation is a heuristic that approximates reflection from a rough surface:

\[ \text{Specular} = I^* \cos^S \phi \]

- \( S \approx \) "shininess"
- \( 1/S \approx \) "roughness"
The Three Elements of Built-in OpenGL Lighting

Ambient + Diffuse + Specular =

Types of Light Sources

Point

Directional (Parallel, Sun)

Spotlight
Lighting Examples

Point Light at the Eye

Point Light at the Origin

Spot Lights
Colored Lights Shining on Colored Objects

What the light can produce

\[ E_R = L_R \cdot M_R \]
\[ E_G = L_G \cdot M_G \]
\[ E_B = L_B \cdot M_B \]

What the material can reflect

\[ M_R, M_G, M_B \]

What the eye sees

\[ L_R, L_G, L_B \]

White Light

Green Light

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Too Many Lighting Options

If there is one light and one material, the following things can be set independently:

- Global scene ambient red, green, blue
- Light position: x, y, z
- Light ambient red, green, blue
- Light diffuse red, green, blue
- Light specular red, green, blue
- Material reaction to ambient red, green, blue
- Material reaction to diffuse red, green, blue
- Material reaction to specular red, green, blue
- Material specular shininess

This makes for 25 things that can be set for just one light and one material! While many combinations are possible, some make more sense than others.

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Ways to Simplify Too Many Lighting Options

1. Set the ambient light globally using, for example,
   
   ```c
   glLightModelfv(GL_LIGHT_MODEL_AMBIENT, MulArray3(.3f, White))
   ```
   
   I.e., set it to some low intensity of white.

2. Set the light's ambient component to zero.

3. Set the light's diffuse and specular components to the full color of the light.

4. Set each material's ambient and diffuse to the full color of the object.

5. Set each material's specular component to some fraction of white.

---

```c
float White[] = {1.,1.,1.,1.};

// utility to create an array from 3 separate values:
float *
Array3(float a, float b, float c)
{
    static float array[4];
    array[0] = a;
    array[1] = b;
    array[2] = c;
    array[3] = 1.;
    return array;
}

// utility to create an array from a multiplier and an array:
float *
MulArray3(float factor, float array0[3])
{
    static float array[4];
    array[0] = factor * array0[0];
    array[1] = factor * array0[1];
    array[2] = factor * array0[2];
    array[3] = 1.;
    return array;
}
```

The 4th element of the array is being set to 1.0 is there on purpose. The reason for that is coming up soon!
Setting the Material Characteristics

```c
// Characteristics for the back-facing surfaces
glMaterialfv( GL_BACK,  GL_AMBIENT,    MulArray3( .4, White ) );
glMaterialfv( GL_BACK,  GL_DIFFUSE,     MulArray3( 1., White ) );
glMaterialfv( GL_BACK,  GL_SPECULAR, Array3( 0., 0., 0. ) );
glMaterialf (  GL_BACK,  GL_SHININESS, 5. );
glMaterialfv( GL_BACK,  GL_EMISSION,   Array3( 0., 0., 0. ) );

// Characteristics for the front-facing surfaces
glMaterialfv( GL_FRONT, GL_AMBIENT,    MulArray3( 1., rgb ) );
glMaterialfv( GL_FRONT, GL_DIFFUSE,     MulArray3( 1., rgb ) );
glMaterialfv( GL_FRONT, GL_SPECULAR, MulArray3( .7, White ) );
glMaterialf (  GL_FRONT,  GL_SHININESS, 8. );
glMaterialfv( GL_FRONT, GL_EMISSION,   Array3( 0., 0., 0. ) );
```

How Does OpenGL Define GL_FRONT and GL_BACK?

- **GL_FRONT**: Vertices are CCW from the point of view of the eye
- **GL_BACK**: Vertices are CW from the point of view of the eye
A Material-setting Shortcut I Like

```c
void SetMaterial( float r, float g, float b, float shininess )
{
    glMaterialfv( GL_BACK, GL_EMISSION, Array3( 0., 0., 0. ) );
    glMaterialfv( GL_BACK, GL_AMBIENT, MulArray3( .4f, White ) );
    glMaterialfv( GL_BACK, GL_DIFFUSE, MulArray3( 1., White ) );
    glMaterialfv( GL_BACK, GL_SPECULAR, Array3( 0., 0., 0. ) );
    glMaterialf( GL_BACK, GL_SHININESS, 2.f );

    glMaterialfv( GL_FRONT, GL_EMISSION, Array3( 0., 0., 0. ) );
    glMaterialfv( GL_FRONT, GL_AMBIENT, Array3( r, g, b ) );
    glMaterialfv( GL_FRONT, GL_DIFFUSE, Array3( r, g, b ) );
    glMaterialfv( GL_FRONT, GL_SPECULAR, MulArray3( .8f, White ) );
    glMaterialf( GL_FRONT, GL_SHININESS, shininess );
}
```

Setting the Light Characteristics

```c
glEnable( GL_LIGHTING );
glEnable( GL_LIGHT0 );
glLightModelfv( GL_LIGHT_MODEL_AMBIENT, MulArray3( .2, White ) );
glLightModeli( GL_LIGHT_MODEL_TWO_SIDE, GL_TRUE );

    glLightfv( GL_LIGHT0, GL_AMBIENT, Array3( 0., 0., 0. ) );
    glLightfv( GL_LIGHT0, GL_DIFFUSE, LightColor );
    glLightfv( GL_LIGHT0, GL_SPECULAR, LightColor );

    glLightf( GL_LIGHT0, GL_CONSTANT_ATTENUATION, 1. );
    glLightf( GL_LIGHT0, GL_LINEAR_ATTENUATION, 0. );
    glLightf( GL_LIGHT0, GL_QUADRATIC_ATTENUATION, 0. );

// this is here because we are going to do object (and thus normal) scaling:
reflect( GL_NORMALIZE );
```

Attenuation = \( \frac{1}{C + Ld + Qd^2} \) where \( d \) is the distance from the light to the point being lit.
Light Attenuation

\[
\text{Attenuation} = \frac{1}{C + Ld + Qd^2}
\]
where \(d\) is the distance from the light to the point being lit.

Physics tells us that light energy decreases with the inverse square of the distance, \(\frac{1}{d^2}\). To emulate this, we would set \(C=0.,\, L=0.,\, Q=1.\). Streetlights and car headlights are good uses for this.

Often, we don’t want any attenuation, that is, we want to see everything. In that case, set \(C=1.,\, L=0.,\, Q=0.\).

\[
\text{glLightf ( GL_LIGHT0, GL_CONSTANT_ATTENUATION, 1. );}
\]
\[
\text{glLightf ( GL_LIGHT0, GL_LINEAR_ATTENUATION, 0. );}
\]
\[
\text{glLightf ( GL_LIGHT0, GL_QUADRATIC_ATTENUATION, 0. );}
\]

And sometimes you might want to attenuate linearly. Why? Well, because you can! In that case, set \(C=0.,\, L=1.,\, Q=0.\).

Setting the Light Position

\[
\text{glMatrixMode( GL_MODELVIEW );}
\]
\[
\text{glLoadIdentity( );}
\]

The light position gets transformed by the ModelView matrix at the moment the \text{glLightfv( ..., GL_POSITION, ... )} function is called. It is really important to remember this!

\[
// 1. \text{ if we do this, then the light will be wrt the scene at XLIGHT, YLIGHT, ZLIGHT:}
\]
\[
\text{glLightfv( GL_LIGHT0, GL_POSITION, Array3(XLIGHT, YLIGHT, ZLIGHT) );}
\]

\[
// 2. \text{ if we do this, then the light will be wrt the eye at XLIGHT, YLIGHT, ZLIGHT:}
\]
\[
// \text{glLightfv( GL_LIGHT0, GL_POSITION, Array3(XLIGHT, YLIGHT, ZLIGHT) );}
\]
// perform the rotations and scaling about the origin:

glRotatef( Xrot, 1., 0., 0.);
glRotatef( Yrot, 0., 1., 0.);
glScalef( Scale, Scale, Scale );

// 3. if we do this, then the light will be wrt to the object at XLIGHT, YLIGHT, ZLIGHT:

// glLightfv( GL_LIGHT0, GL_POSITION, Array3(XLIGHT, YLIGHT, ZLIGHT) );

// specify the shading model:

glShadeModel( GL_SMOOTH );

// enable lighting:

glEnable( GL_LIGHTING );
glEnable( GL_LIGHT0 );

// draw the objects:

...glDisable( GL_LIGHTING );

```c
float * Array3( float a, float b, float c )
{
    static float array[4];
    array[0] = a;
    array[1] = b;
    array[2] = c;
    array[3] = 1.;
    return array;
}

Sidebar: Why are Light Positions 4-element arrays where the 4th element is 1.0? Homogeneous Coordinates!

We usually think of a 3D point as being represented by a triple: \((x,y,z)\).
Using homogeneous coordinates, we add a 4th number: \((x,y,z,w)\).
Graphics systems take \((x,y,z,w)\), perform all transformations, and then divide \(x\), \(y\), and \(z\) by \(w\) before using them.

\[
\begin{align*}
X &= \frac{x}{w}, & Y &= \frac{y}{w}, & Z &= \frac{z}{w}.
\end{align*}
\]

Thus \((1,2,3,1), (2,4,6,2), (-1,-2,-3,-1)\) all represent the same 3D point.
Homogeneous Coordinates let us Represent Points at Infinity

This is useful to be able specify a parallel light source by placing the light source position at infinity.

The point (1,2,3,1) represents the 3D point (1,2,3)
The point (1,2,3,.5) represents the 3D point (2,4,6)
The point (1,2,3,.01) represents the point (100,200,300)
So, (1,2,3,0) represents a point at infinity, along the ray from the origin through (1,2,3).
Points-at-infinity are used for parallel light sources (and some shadow algorithms)

Example of using a parallel light source

Additional Parameters for Spotlights

\texttt{glLightfv( GL\_LIGHT0, GL\_SPOT\_DIRECTION, Array3(xdir,ydir,zdir) );}
Specifies the spotlight-pointing direction. This gets transformed by the current value of the ModelView matrix.

\texttt{glLightf( GL\_LIGHT0, GL\_SPOT\_EXponent, e );}
Specifies the spotlight directional intensity. This acts very much like the exponent in the specular lighting equation.

\texttt{glLightf( GL\_LIGHT0, GL\_SPOT\_CUTOFF, deg );}
Specifies the spotlight maximum spread angle.

Three bouncing spotlights
A Light-setting Shortcut I Like

```c
void SetPointLight( int ilight, float x, float y, float z, float r, float g, float b )
{
    glLightfv( ilight, GL_POSITION, Array3( x, y, z ) );
    glLightfv( ilight, GL_AMBIENT,   Array3( 0., 0., 0. ) );
    glLightfv( ilight, GL_DIFFUSE,   Array3( r, g, b ) );
    glLightfv( ilight, GL_SPECULAR,  Array3( r, g, b ) );
    glLightf ( ilight, GL_CONSTANT_ATTENUATION, 1. );
    glLightf ( ilight, GL_LINEAR_ATTENUATION, 0. );
    glLightf ( ilight, GL_QUADRATIC_ATTENUATION, 0. );
    glEnable( ilight );
}

void SetSpotLight( int ilight, float x, float y, float z, float xdir, float ydir, float zdir, float r, float g, float b )
{
    glLightfv( ilight, GL_POSITION, Array3( x, y, z ) );
    glLightfv( ilight, GL_SPOT_DIRECTION, Array3(xdir,ydir,zdir) );
    glLightf( ilight, GL_SPOT_EXPONENT, 1. );
    glLightf( ilight, GL_SPOT_CUTOFF, 45. );
    glLightfv( ilight, GL_AMBIENT,   Array3( 0., 0., 0. ) );
    glLightfv( ilight, GL_DIFFUSE,   Array3( r, g, b ) );
    glLightfv( ilight, GL_SPECULAR,  Array3( r, g, b ) );
    glLightf ( ilight, GL_CONSTANT_ATTENUATION, 1. );
    glLightf ( ilight, GL_LINEAR_ATTENUATION, 0. );
    glLightf ( ilight, GL_QUADRATIC_ATTENUATION, 0. );
    glEnable( ilight );
}
```

Sidebar: Note that we are computing the light intensity at each vertex first, and then interpolating that intensity across the polygon second.

That is, you are only using the lighting model at each vertex. You can do an even better job if you interpolate the normal across the polygon first, and then compute the light intensity with the lighting model at each fragment second:
But, for per-fragment, you will need shaders (coming up soon!)

Per-vertex

Per-fragment

Sidebar: Smooth Shading can also interpolate vertex colors, not just the results of the lighting model

Before, when we talked about normal vectors, we did this:

```c
glMatrixMode( GL_MODELVIEW );
glTranslatef( tx, ty, tz );
glRotatef( degrees, ax, ay, az );
glScalef( sx, sy, sz );
glShadeModel( GL_SMOOTH );
glColor3f( r, g, b );
```

We can also provide per-vertex colors to do this:

```c
glMatrixMode( GL_MODELVIEW );
glTranslatef( tx, ty, tz );
glRotatef( degrees, ax, ay, az );
glScalef( sx, sy, sz );
glShadeModel( GL_SMOOTH );
```

```c
glBegin(GL_TRIANGLES );
glColor3f( r0, g0, b0 );
glVertex3f( x0, y0, z0 );
glColor3f( r1, g1, b1 );
glVertex3f( x1, y1, z1 );
glColor3f( r2, g2, b2 );
glEnd( );
```
Smooth Shading can also interpolate vertex colors, not just the results of the lighting model.

This is especially useful when using colors for scientific visualization:

Tricky Lighting Situations

- Hair
- Fur
- Feathers

Watch for these in movies!
Tricky Lighting Situations

Notice the lighting in the fur!

Sony/Columbia Pictures

Sidebar: Beware of Mach Banding

Notice how these vertical stripes look “scalloped”, like a Greek column. But, they are solid-color stripes. What is going on?
Our vision systems can’t handle abrupt changes in intensity.

In fact, our vision systems can’t even handle abrupt changes in the slope of intensity.

Flat shading

Smooth shading

This “white line” doesn’t really exist – it is an artifact of our vision system!
Beware of Mach Banding

Think of the Mach Banding problem as being similar to trying to round second base at a 90° angle.