Zooming and Panning Around a Complex 2D Display

- Standard (Euclidean) geometry zooming forces much of the information off the screen
- This eliminates the context from the zoomed-in display
- This problem can be solved with hyperbolic methods if we are willing to give up Euclidean geometry
- At one time, this would have also meant severely giving up graphics performance, but not now
Zooming in Euclidean Space

123,101 line strips
446,585 points

Zooming in Polar Hyperbolic Space
Polar Hyperbolic Equations

Overall theme: something divided by something a little bigger

\[ \lim_{K \to 0} R' = 1 \]
\[ \lim_{K \to \infty} R' = 0 \]

\[ R = \frac{R}{R+K} \]
\[ \Theta' = \Theta \]
\[ X' = R' \cos \Theta' \]
\[ Y' = R' \sin \Theta' \]

Coordinates moved to outer edge when \( K = 0 \)
Coordinates moved to center when \( K = \infty \)

\[ R = \sqrt{X^2 + Y^2} \]
\[ \Theta = \tan^{-1} \left( \frac{Y}{X} \right) \]
\[ R' = \frac{R}{R+K} \]

\[ X' = X \frac{R}{R+K} \]
\[ Y' = Y \frac{R}{R+K} \]
Cartesian Hyperbolic Equations

\[ X' = \frac{X}{R + K} \]
\[ Y' = \frac{Y}{R + K} \]

\[ X' = \frac{X}{\sqrt{X^2 + K^2}} \]
\[ Y' = \frac{Y}{\sqrt{Y^2 + K^2}} \]

Polar

Cartesian

Coordinates moved to outer edge when \( K = 0 \)

Coordinates moved to center when \( K = \infty \)

Coordinates moved to outer edge when \( K = 0 \)

Coordinates moved to center when \( K = \infty \)

Zooming in Cartesian Hyperbolic Space
#version 330 compatibility

uniform bool uPolar;
uniform float uK;
uniform float uTransX;
uniform float uTransY;
out vec3 vColor;

void main( void )
{
    vColor = gl_Color.rgb;

    vec2 pos = ( gl_ModelViewMatrix * gl_Vertex ).xy;
    pos += vec2( uTransX, uTransY );
    float r = length( pos.xyz );
    vec4 pos2 = vec4( 0., 0., -5., 1. );
    if( uPolar )
        pos2.xy = pos / ( r + uK );
    else
        pos2.xy = pos / ( pos*pos + uK*uK );
    gl_Position = gl_ProjectionMatrix * pos2;
}

#version 330 compatibility

in vec3 vColor;

void main( )
{
    gl_FragColor = vec4( vColor, 1. );
}