Using Shaders for Lighting
Lighting Definitions

\[ \text{N} = \text{Normal} \]
\[ \text{L} = \text{Light vector} \]
\[ \text{E} = \text{Eye vector} \]
\[ \text{R} = \text{Light reflection vector} \]
\[ \text{ER} = \text{Eye reflection vector} \]
\[ \text{Color} = \text{LightColor} \times \text{MaterialColor} \]

**Ambient** = Light intensity that is “everywhere”

**Diffuse** = Light intensity proportional to \( \cos(\Theta) \)

**Specular** = Light intensity proportional to \( \cos^S(\Phi) \)

**A-D-S** = Lighting model that includes Ambient, Diffuse, and Specular

**Flat Interpolation** = Use a single polygon normal to compute one A-D-S for the entire polygon

**Smooth Interpolation** = Use a normal at each vertex to compute one A-D-S for at each vertex

**Per-vertex lighting** = Compute A-D-S using each vertex normal and then interpolate the summed intensity over the entire polygon

**Per-fragment lighting** = Interpolate the vertex normals across the entire polygon and then compute A-D-S at each fragment

**CubeMap Reflection** = Using the Eye Reflection Vector (ER) to look-up the reflection of a “wall texture”
A-D-S Lighting

**Ambient:** $K_a$

**Diffuse:** $K_d \cdot \cos \theta$

**Specular:** $K_s \cdot \cos^s \phi$
A-D-S Lighting with Flat Interpolation

Each polygon has a single lighting value applied to every pixel within it.

\[
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\text{Color} = \text{LightColor} * \text{MaterialColor}
\]

Vertex Shader

\[
\begin{align*}
\text{vec3 ambient} & = \text{Color.rgb} \\
\text{diffuse} & = \max( \dot{\text{L}}(\text{N}), 0. ) \ast \text{Color.rgb} \\
\text{vec3 R} & = \text{normalize}( \text{reflect}( -\text{L}, \text{N} ) ) \\
\text{vec3 spec} & = \text{LightColor} \ast \text{pow}( \max( \dot{\text{R}}(\text{E}), 0. ), \text{Shininess} )
\end{align*}
\]

Fragment Shader

\[
\text{gl_FragColor.rgb} = \text{Ka} \ast \text{ambient} + \text{Kd} \ast \text{diffuse} + \text{Ks} \ast \text{spec};
\]
What the eye sees depends on the light color and the material color.

What you see depends on the light color and the material color.

$E_R = L_R \times M_R$
$E_G = L_G \times M_G$
$E_B = L_B \times M_B$

This is how you implement subtractive coloring.
A-D-S Lighting with Smooth Interpolation

Note: In per-vertex lighting, the **light intensity is computed at each vertex** and interpolated throughout the polygon. This creates artifacts such as Mach Banding and the fact that the bright spot is “jagged”.

You can do this in stock OpenGL or in a shader.

<table>
<thead>
<tr>
<th>N = Normal</th>
<th>L = Light vector</th>
<th>E = Eye vector</th>
<th>R = Light reflection vector</th>
<th>ER = Eye reflection vector</th>
<th>Color = LightColor * MaterialColor</th>
</tr>
</thead>
</table>

Vertex Shader

```
vec3 ambient = Color.rgb;
diffuse  = max( dot(L,N), 0. ) * Color.rgb;
vec3 R = normalize( reflect( -L, N ) );
vec3 spec = LightColor * pow( max( dot( R, E), 0. ), Shininess );
```

Fragment Shader

```
gl_FragColor.rgb = Ka*ambient + Kd*diffuse + Ks*spec;
```
A-D-S Lighting with Normal Interpolation

In per-fragment lighting, the normal is interpolated throughout the polygon. The light intensity is computed at each fragment. This avoids Mach Banding and makes the bright spot smooth.

You can only do this in a shader.

Fragment Shader

```
vec3 ambient = Color.rgb;
diffuse = max( dot(L,N), 0. ) * Color.rgb;
vec3 R = normalize( reflect( -L, N ) );
vec3 spec = LightColor * pow( max( dot( R, E ), 0. ), Shininess );
gl_FragColor.rgb = Ka*ambient + Kd*diffuse + Ks*spec;
```
The Difference Between Per-Vertex Lighting and Per-Fragment Lighting

Per-vertex

Per-fragment
The Difference Between Per-Vertex Lighting and Per-Fragment Lighting

Per-vertex

Per-fragment
Flat shading

Normal interpolation
A-D-S Lighting with Normal Interpolation and a CubeMap Reflection

**Fragment Shader**

\[
\begin{align*}
\text{vec3 ambient} &= \text{Color.rgb;} \\
\text{diffuse} &= \max(\ \text{dot}(L,N), 0.) \times \text{Color.rgb;} \\
\text{vec3 R} &= \text{normalize( reflect( -L, N ) );} \\
\text{vec3 spec} &= \text{LightColor} \times \text{pow( max( dot( R, E ), 0. ), Shininess );} \\
\text{vec3 reflcolor} &= \text{textureCube( ReflectUnit, R ).rgb;} \\
\text{gl}_\text{FragColor.rgb} &= \text{Ka*ambient + Kd*diffuse + Ks*spec + Kr*reflcolor.rgb;}
\end{align*}
\]

Note: A cube map reflection is blended in, given a stronger impression that the surface is shiny.

\[
\begin{align*}
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\text{Color} &= \text{LightColor} \times \text{MaterialColor}
\end{align*}
\]

Smooth-rasterize N, L, E
A-D-S Anisotropic Lighting with Normal Interpolation

Note: The bright spot is not circular because the material has different properties in different directions. Materials such as fur, hair, and brushed metal behave this way.


N = Normal
L = Light vector
E = Eye vector
R = Light reflection vector
ER = Eye reflection vector
Color = LightColor * MaterialColor

```glsl
vec3 ambient = Color.rgb;
float dl = dot( T, L );
vec3 diffuse = sqrt( 1. - dl*dl ) * Color.rgb;
float de = dot( T, E );
vec3 spec = LightColor * pow( dl * de + sqrt( 1. - dl*dl ) * sqrt( 1. - de*de ), Shininess );
gl_FragColor.rgb = Ka*ambient + Kd*diffuse + Ks*spec;
```

Fragment Shader

Oregon State University
Computer Graphics
Summary

Flat

Smooth

Normal

Reflection

Anisotropic
#version 330 compatibility

uniform float uLightX, uLightY, uLightZ;

flat out vec3 vNf;
    out vec3 vNs;
flat out vec3 vLf;
    out vec3 vLs;
flat out vec3 vEf;
    out vec3 vEs;

vec3 eyeLightPosition = vec3( uLightX, uLightY, uLightZ );

void
main( )
{
    vec4 ECposition = gl_ModelViewMatrix * gl_Vertex;

    vNf = normalize( gl_NormalMatrix * gl_Normal ); // surface normal vector
    vNs = vNf;

    vLf = eyeLightPosition - ECposition.xyz; // vector from the point
    vLs = vLf; // to the light position

    vEf = vec3( 0., 0., 0. ) - ECposition.xyz; // vector from the point
    vEs = vEf; // to the eye position

    gl_Position = gl_ModelViewProjectionMatrix * gl_Vertex;
}
```glsl
#version 330 compatibility

uniform float uKa, uKd, uKs;
uniform vec4 uColor;
uniform vec4 uSpecularColor;
uniform float uShininess;
uniform bool uFlat;

flat in vec3 vNf;
    in vec3v Ns;
flat in vec3 vLf;
    in vec3v Ls;
flat in vec3 vEf;
    in vec3v vEs;

void main( )
{
    vec3 Normal;
    vec3 Light;
    vec3 Eye;

    if( uFlat )
    {
        Normal = normalize(vNf);
        Light  = normalize(vLf);
        Eye    = normalize(vEf);
    }
    else
    {
        Normal = normalize(vNs);
        Light  = normalize(vLs);
        Eye    = normalize(vEs);
    }
```

Per-fragment lighting: the fragment shader, I
vec4 ambient = uKa * uColor;

float d = max( dot(Normal,Light), 0. );
vec4 diffuse = uKd * d * uColor;

float s = 0.;
if( dot(Normal,Light) > 0. ) // only do specular if the light can see the point
{
    vec3 ref = normalize( 2. * Normal * dot(Normal,Light) - Light );
    s = pow( max( dot(Eye,ref),0. ), uShininess );
}

vec4 specular = uKs * s * uSpecularColor;

gl_FragColor = vec4( ambient.rgb + diffuse.rgb + specular.rgb, 1. );