Noise!

- Noise can be 1D, 2D, or 3D.
- It is a function of input value(s).
- It ranges from -1.0 to +1.0 or from 0.0 to 1.0.
- It might look random, but really isn’t.
- It has continuity.
- It is repeatable (i.e., if you supply the same inputs, you will always get the same outputs).

Positional Noise

Idea: Pick a random number at the whole-number input values and then fit a piecewise smooth curve through those points.

Gradient Noise

Idea: Place points at the mid-line at the whole-number input values use random numbers to pick gradients (slopes) there, and then fit a piecewise smooth curve through those points with those slopes.
Quintic (5th order) Interpolation Creates More Continuity Than Cubic

Cubic: $C^1$ continuity at the whole-number values
Quintic: $C^2$ continuity at the whole-number values

Coefficients for Cubic and Quintic Forms

Cubic
\[ C_{N0} = 1 - 3t^2 + 2t^3 \]
\[ C_{N1} = 3t^2 - 2t^3 = 1 - C_{N0} \]
\[ C_{G0} = t - 2t^2 + t^3 \]
\[ C_{G1} = -t^2 + t^3 \]
\[ C_{C0} = 0 \]
\[ C_{C1} = 0 \]

Quintic
\[ C_{N0} = 1 - 10t^3 + 15t^4 - 6t^5 \]
\[ C_{N1} = 10t^3 - 15t^4 + 6t^5 = 1 - C_{N0} \]
\[ C_{G0} = t - 6t^3 + 8t^4 - 3t^5 \]
\[ C_{G1} = -4t^3 + 7t^4 - 3t^5 \]
\[ C_{C0} = \frac{1}{2}t^2 - \frac{3}{2}t^3 + \frac{3}{2}t^4 - \frac{1}{2}t^5 \]
\[ C_{C1} = \frac{1}{2}t^3 - t^4 + \frac{1}{2}t^5 \]

Noise Octaves

Idea: Add multiple noise waves, each one twice the frequency and half the amplitude of the previous one

Image Representation of 2D Noise

1 Octave
4 Octaves
3D Surface Representation of 2D Noise

3D Volume Rendering of 3D Noise

Has continuity in X, Y, and Z

3D Volume Isosurfaces of 3D Noise

The low half of the noise values are on one side of the surface, the high half are on the other side.

Examples

Color Blending for Clouds

Color Blending for Marble

Deciding when to Discard for Erosion
Turbulence

Idea: Take the absolute value of the noise about the centerline, giving the noise a “sharper” appearance and creating “creases”. Warning: this is not the same as fluid “turbulence”.

Normal

Turbulent

1 Octave

4 Octaves

How to Use Noise

Have actual input values of where we are right now

Add Noise to the actual input values to produce new “fake” input values

Use those new “fake” input values in the original equation

Idea: The graphics system will display “here”, using display parameters as if you were “over there.

N = NoiseMag * noise( NoiseFreq * PP );

How much to amplify the noise effect
Coordinates where you are now

How much to increase the sampling rate

Should PP be in Model or World coordinates? Why?
\[ N = \text{NoiseMag} \times \text{noise(NoiseFreq \times PP)}; \]
Displacement Only
Surface + Displacement
No Noise
Noise

What's the Difference Between These Two Images? Why?