Tessellation Shaders

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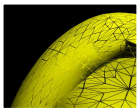
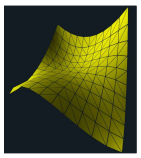
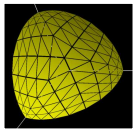
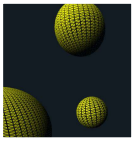








Tessellation Fun Facts

I once won an OpenGL t-shirt at the SIGGRAPH conference by knowing how to correctly spell "tessellation". (It's 2 s's and 2 l's.)

The only reason I knew it was that the week before I had been experimenting with the newly-released tessellation shaders for the first time and my program wouldn't compile because I had misspelled tessellation. The week of the conference, it was still fresh in my mind how to spell it correctly.

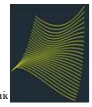
Please don't tell anyone. Spelling correctly undermines one's CS credibility… ☺

Why do we need a Tessellation step right in the pipeline?

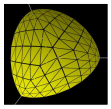
- You can perform adaptive subdivision based on a variety of criteria (size, curvature, etc.)
- You can provide coarser models, but have finer ones displayed (≈ geometric compression)
- You can apply detailed displacement maps without supplying equally detailed geometry
- You can apply detailed normal maps without supplying equally detailed geometry
- You can adapt visual quality to the required level of detail
- You can create smoother silhouettes
- You can do all of this, and someone else will supply the geometic patterns for you!

What *built-in* patterns can the Tessellation shaders produce?

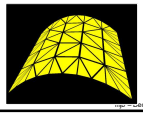
Lines



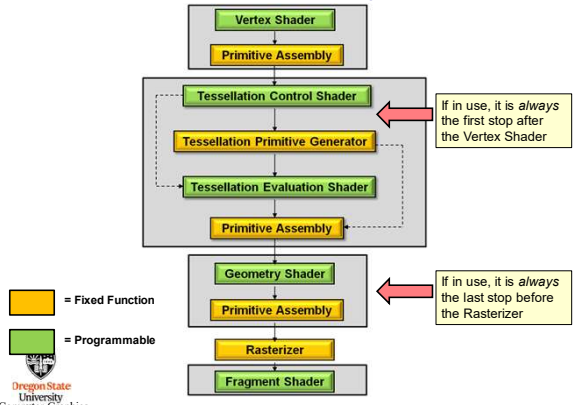
Triangles



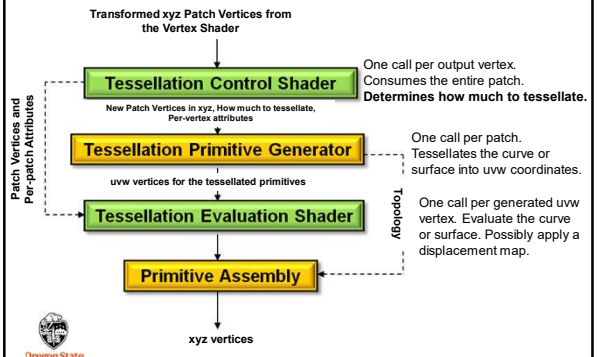
Quads (subsequently broken into triangles)



The Tessellation Shaders: Where Do they Fit in the Pipeline?



Tessellation Shader Organization



Tessellation Shader Organization

The **Tessellation Control Shader (TCS)** optionally can transform the input coordinates (but usually doesn't). It also computes the required tessellation level based on distance to the eye, screen space spanning, hull curvature, or displacement roughness. There is one TCS execution per vertex.

The Fixed-Function **Tessellation Primitive Generator (TPG)** generates semi-regular u-v-w coordinates in specific patterns. (In fact, if it had been up to me, this would have been called the **Tessellation *Pattern* Generator**. Nobody asked.)

The **Tessellation Evaluation Shader (TES)** Turns the TPG's u-v-w coordinates into x-y-z. It can apply displacements. There is one TES execution per generated vertex.

There is a new "Patch" primitive:

glBegin(GL_PATCHES)

followed by some number of glVertex3f( ) calls. There is no implied purpose, number of vertices, or vertex ordering – those are given by you in how you write the shader.

In the OpenGL Program

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```
glPatchParameteri( GL_PATCH_VERTICES, num );   // # of vertices in each patch
glBegin( GL_PATCHES );
        glVertex3f( … );
        glVertex3f( … );
glEnd( );
```

These have no implied topology – they will be given to you in an array. It's up to your shader to interpret the order

```
GLuint tcs = glCreateShader( GL_TESS_CONTROL_SHADER );

GLuint tes = glCreateShader( GL_TESS_EVALUATION_SHADER );
```

Check the OpenGL extension:
"GL_ARB_tessellation_shader"

In GLSL:
#version 400
#ension GL_ARB_tessellation_shader : enable

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TCS Inputs

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gl_in[ ] is an array of structures:

```
struct
{
        vec4 gl_Position;
        float gl_PointSize;
        float gl_ClipDistance[ 6 ];
} gl_in[ ];
```

gl_InvocationID tells you which vertex you are working on, This is the index into the gl_in[ ] array.

gl_PatchVerticesIn is the number of vertices in each patch and the dimension of gl_in[ ]

gl_PrimitiveID is the number of primitives since the last glBegin( ) (the first one is #0)

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TCS Outputs

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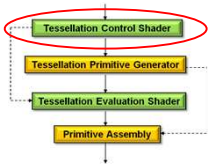
gl_out[ ] is an array of structures:

```
struct
{
        vec4 gl_Position;
        float gl_PointSize;
        float gl_ClipDistance[ 6 ];
} gl_out[ ];
```



layout(vertices = n) out; Used to specify the number of vertices sent to the TPG

gl_TessLevelOuter[4] is a built-in array containing up to 4 outside edges of tessellation levels

gl_TessLevelInner[2] is a built-in array containing up to 2 inside edges of tessellation levels

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In the TCS

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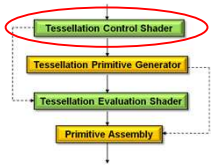
User-defined variables defined per-vertex are qualified as "out"

User-defined variables defined per-patch are qualified as "patch out"

Defining how many vertices this patch will use:

layout(vertices = 16) out;



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TES Inputs

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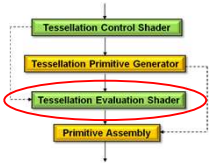
Reads one triplet of 0. <= (u,v,w) <= 1. coordinates in the built-in variable ***vec3 gl_TessCoord***

User-defined variables defined per-vertex are qualified as "out"
User-defined variables defined per-patch are qualified as "patch out"

gl_in[ ] is an array of structures coming from the TCS:

```
struct
{
        vec4 gl_Position;
        float gl_PointSize;
        float gl_ClipDistance[ 6 ];
} gl_in[ ];
```



$$\text{layout}\left(\begin{Bmatrix}\text{triangles}\\ \text{quads}\\ \text{isolines}\end{Bmatrix}, \begin{Bmatrix}\text{equal\_spacing}\\ \text{fractional\_even\_spacing}\\ \text{fractional\_odd\_spacing}\end{Bmatrix}, \begin{Bmatrix}\text{ccw}\\ \text{cw}\end{Bmatrix}, \text{point\_mode}\right)\ \text{in;}$$

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Tessellation ~~Primitive~~ Pattern Generator (TPG)

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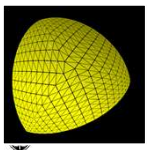
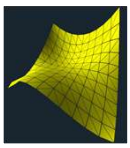
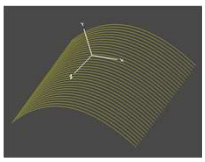
- The TPG is "fixed-function", i.e., you can't change its operation except by setting parameters
- The TPG consumes all vertices from the TCS and emits vertices for the ***triangles***, ***quads***, or ***isolines*** patterns
- The TPG outputs a series of vertices as coordinates in barycentric, i.e., in terms of the parameters (u,v,w)
- Really, only (u,v) are unique: for triangles w = 1. – u – v
- Just (u,v) are used for quads and isolines



Triangle pattern



Quad pattern



Isoline pattern

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TES Output Topologies: the Quad Pattern

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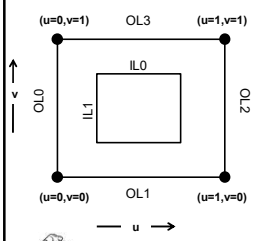
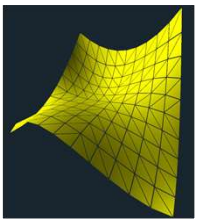
gl_TessLevelOuter[4] is an array containing up to 4 outside edges of tessellation levels.
gl_TessLevelInner[2] is an array containing up to 2 inside edges of tessellation levels.





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TES Output Topologies: the Isolines Pattern

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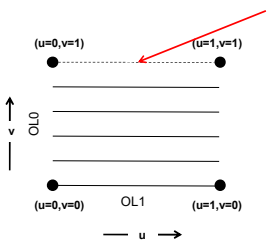
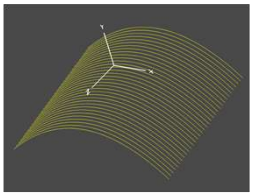
gl_TessLevelOuter[4] is an array containing up to 4 outside edges of tessellation levels.
gl_TessLevelInner[2] is an array containing up to 2 inside edges of tessellation levels.





OL0 == 1 implies that you just want to draw a single curve

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TES Output Topologies: the Triangle Pattern

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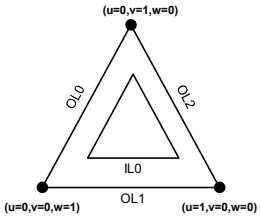
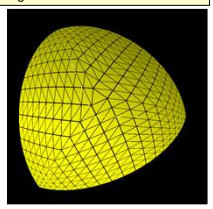
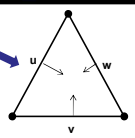
gl_TessLevelOuter[4] is an array containing up to 4 outside edges of tessellation levels.
gl_TessLevelInner[2] is an array containing up to 2 inside edges of tessellation levels.



u + v + w = 1



How triangle barycentric coordinates work



u + v + w = 1

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Examples

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In these examples:

1. I am using *glman* to run them. The only necessary input files are the *glman* .glib file and the shader files. If you aren't using *glman*, you can do this from a full OpenGL program.
2. All of the surface examples use the Geometry Shader triangle-shrink shader. This isn't necessary, but is educational to really see how the surfaces have been tessellated.

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Example: A Bézier Curve

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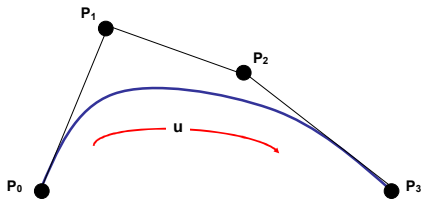

$$P(u) = (1-u)^3 P_0 + 3u(1-u)^2 P_1 + 3u^2(1-u) P_2 + u^3 P_3$$

Need to pass 4 points in to define the curve. Need to pass N points out to draw the curve as a line strip.

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Example: A Bézier Curve

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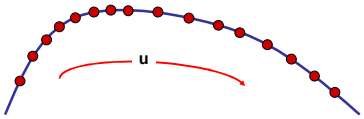

$$P(u) = (1-u)^3 P_0 + 3u(1-u)^2 P_1 + 3u^2(1-u) P_2 + u^3 P_3$$

1. You program the Tessellation Control Shader to decide how much to tessellate the curve based on screen area, curvature, etc.

Can even tessellate non-uniformly if you want, such as using more points where the curvature is higher

The OpenGL tessellation can do 1D curves. Just set OL0 == 1.

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Example: A Bézier Curve

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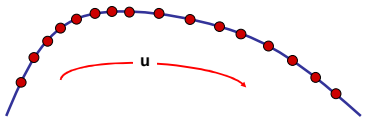

2. The Tessellation Primitive Generator generates u values for as many subdivisions as the TCS asked for.

Example: A Bézier Curve

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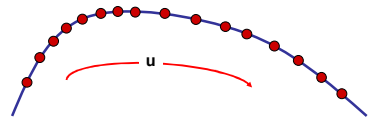

3. The Tessellation Evaluation Shader computes the x,y,z coordinates based on the TPG's *u* values and P_0, P_1, P_2, and P_3.

$$P(u) = (1-u)^3 P_0 + 3u(1-u)^2 P_1 + 3u^2(1-u)P_2 + u^3 P_3$$

$$where\ P\ is\ an\ abbreviation\ for\ \begin{Bmatrix} x \\ y \\ z \end{Bmatrix}$$

In an OpenGL Program

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In InitGraphics( ):

```
Pattern.Init( );
Pattern.Create( "pattern.vert", "pattern.tcs", "pattern.tes", "pattern.frag" );
Pattern.SetUniformVariable( "uOuter0", 20 );
Pattern.SetUniformVariable( "uOuter1", 10 );
```

In Display( ):

```
glPatchParameteri( GL_PATCH_VERTICES, 4 );

glBegin( GL_PATCHES );
        glVertex3f( x0, y0, z0 );
        glVertex3f( x1, y1, z1 );
        glVertex3f( x2, y2, z2 );
        glVertex3f( x3, y3, z3 );
glEnd( );
```


In a .glib File

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```
##OpenGL GLIB
Perspective 70

Vertex          beziercurve.vert
Fragment        beziercurve.frag
TessControl     beziercurve.tcs
TessEvaluation  beziercurve.tes
Program BezierCurve  uOuter0 <0  1  5>  uOuter1 <3  5  50>

Color 1.  .5  0. 1.

NumPatchVertices 4
glBegin gl_patches
   glVertex 0. 0. 0.
   glVertex 1. 1. 1.
   glVertex 2. 1. 0.
   glVertex 3. 0. 1.
glend
```


In the TCS Shader

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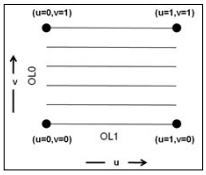


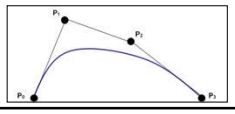

```
#version 400
#ension GL_ARB_tessellation_shader: enable

uniform int uOuter0, uOuter1;

layout( vertices = 4 )  out;

void
main( )
{
        gl_out[ gl_InvocationID ].gl_Position = gl_in[ gl_InvocationID ].gl_Position;

        gl_TessLevelOuter[0] = float( uOuter0 );
        gl_TessLevelOuter[1] = float( uOuter1 );
}
```



In the TES Shader

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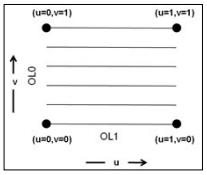
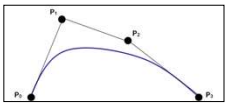



```
#version 400
#ension GL_ARB_tessellation_shader: enable

layout( isolines, equal_spacing)  in;

void
main( )
{
        vec4 p0 = gl_in[0].gl_Position;
        vec4 p1 = gl_in[1].gl_Position;
        vec4 p2 = gl_in[2].gl_Position;
        vec4 p3 = gl_in[3].gl_Position;

        float u = gl_TessCoord.x;

        // the basis functions:

        float b0 = (1.-u) * (1.-u) * (1.-u);
        float b1 = 3. * u * (1.-u) * (1.-u);
        float b2 = 3. * u * u * (1.-u);
        float b3 = u * u * u;

        gl_Position = b0*p0 + b1*p1 + b2*p2 + b3*p3;
}
```



Assigning the intermediate pi's is here to make the code more readable. From what I have seen, the compiler will optimize this away.

Example: A Bézier Curve

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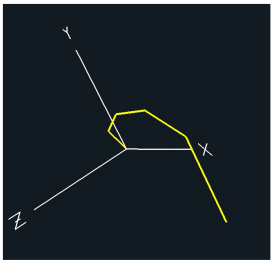
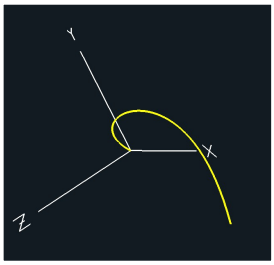


Outer1 = 5



Outer1 = 50

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Example: A Bézier Surface

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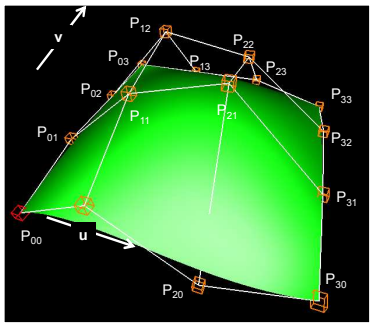

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Bézier Surface Parametric Equations

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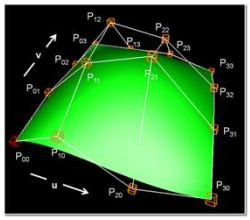

$$P(u,v) = \begin{bmatrix} (1-u)^3 & 3u(1-u)^2 & 3u^2(1-u) & u^3 \end{bmatrix} \begin{bmatrix} P_{00} & P_{01} & P_{02} & P_{03} \\ P_{10} & P_{11} & P_{12} & P_{13} \\ P_{20} & P_{21} & P_{22} & P_{23} \\ P_{30} & P_{31} & P_{32} & P_{33} \end{bmatrix} \begin{Bmatrix} (1-v)^3 \\ 3v(1-v)^2 \\ 3v^2(1-v) \\ v^3 \end{Bmatrix}$$

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In an OpenGL Program

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```
glPatchParameteri( GL_PATCH_VERTICES, 16 );

glBegin( GL_PATCHES );
        glVertex3f( x00, y00, z00 );
        glVertex3f( x10, y10, z10 );
        glVertex3f( x20, y20, z20 );
        glVertex3f( x30, y30, z30 );
        glVertex3f( x01, y01, z01 );
        glVertex3f( x11, y11, z11 );
        glVertex3f( x21, y21, z21 );
        glVertex3f( x31, y31, z31 );
        glVertex3f( x02, y02, z02 );
        glVertex3f( x12, y12, z12 );
        glVertex3f( x22, y22, z22 );
        glVertex3f( x32, y32, z32 );
        glVertex3f( x03, y03, z03 );
        glVertex3f( x13, y13, z13 );
        glVertex3f( x23, y23, z23 );
        glVertex3f( x33, y33, z33 );
glEnd( );
```

This order is not set by OpenGL. It is set by ***you***. Pick a convention yourself and stick to it!

GLSL doesn't care as long as you are consistent.

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In the .glib File

29

```
##OpenGL GLIB
Perspective 70

Vertex          beziersurface.vert
Fragment        beziersurface.frag
TessControl     beziersurface.tcs
TessEvaluation  beziersurface.tes
Geometry        beziersurface.geom
Program BezierSurface  uOuter02 <1 10 50>  uOuter13 <1 10 50>  uInner0 <1 10 50>  uInner1 <1 10 50>   \
                       uShrink <0. 1. 1.>                                                            \
                       u LightX <-10. 0. 10.>  u LightY <-10. 10. 10.>   uLightZ <-10. 10. 10. >

Color  1. 1. 0. 1.

NumPatchVertices 16

glBegin gl_patches
    glVertex 0. 2. 0.
    glVertex 1. 1. 0.
    glVertex 2. 1. 0.
    glVertex 3. 2. 0.

    glVertex 0. 1. 1.
    glVertex 1. -2. 1.
    glVertex 2. 1. 1.
    glVertex 3. 0. 1.

    glVertex 0. 0. 2.
    glVertex 1. 1. 2.
    glVertex 2. 0. 2.
    glVertex 3. -1. 2.

    glVertex 0. 0. 3.
    glVertex 1. 1. 3.
    glVertex 2. -1. 3.
    glVertex 3. -1. 3.
glEnd
```

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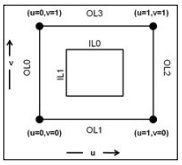
In the TCS Shader

30



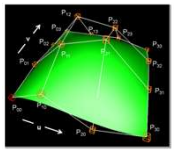

```
#version 400
#extension GL_ARB_tessellation_shader : enable

uniform float uOuter02, uOuter13, uInner0, uInner1;

layout( vertices = 16 ) out;

void
main( )
{
        gl_out[ gl_InvocationID ].gl_Position = gl_in[ gl_InvocationID ].gl_Position;

        gl_TessLevelOuter[0] = gl_TessLevelOuter[2] = uOuter02;
        gl_TessLevelOuter[1] = gl_TesslevelOuter[3]  = uOuter13;
        gl_TessLevelInner[0]  = uInner0;
        gl_TessLevelInner[1]  = uInner1;
}
```



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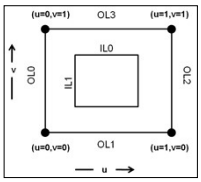
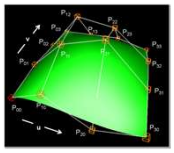
Computer Graphics

In the TES Shader

31

```
#version 400 compatibility
#extension GL_ARB_tessellation_shader : enable

layout( quads, equal_spacing, ccw)  in;

out vec3 teNormal;

void main( )
{
        vec4 p00 = gl_in[ 0].gl_Position;
        vec4 p10 = gl_in[ 1].gl_Position;
        vec4 p20 = gl_in[ 2].gl_Position;
        vec4 p30 = gl_in[ 3].gl_Position;
        vec4 p01 = gl_in[ 4].gl_Position;
        vec4 p11 = gl_in[ 5].gl_Position;
        vec4 p21 = gl_in[ 6].gl_Position;
        vec4 p31 = gl_in[ 7].gl_Position;
        vec4 p02 = gl_in[ 8].gl_Position;
        vec4 p12 = gl_in[ 9].gl_Position;
        vec4 p22 = gl_in[10].gl_Position;
        vec4 p32 = gl_in[11].gl_Position;
        vec4 p03 = gl_in[12].gl_Position;
        vec4 p13 = gl_in[13].gl_Position;
        vec4 p23 = gl_in[14].gl_Position;
        vec4 p33 = gl_in[15].gl_Position;

        float u = gl_TessCoord.x;
        float v = gl_TessCoord.y;
```



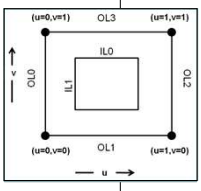


Assigning the intermediate pij's is here to make the code more readable. From what I've seen, the compiler will optimize this away.

In the TES Shader –

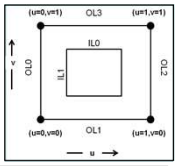
32

```
// the basis functions:

float bu0 = (1.-u) * (1.-u) * (1.-u);
float bu1 = 3. * u * (1.-u) * (1.-u);
float bu2 = 3. * u * u * (1.-u);
float bu3 = u * u * u;

float dbu0 = -3. * (1.-u) * (1.-u);
float dbu1 =  3. * (1.-u) * (1.-3.*u);
float dbu2 =  3. * u *      (2.-3.*u);
float dbu3 =  3. * u *      u;

float bv0 = (1.-v) * (1.-v) * (1.-v);
float bv1 = 3. * v * (1.-v) * (1.-v);
float bv2 = 3. * v * v * (1.-v);
float bv3 = v * v * v;

float dbv0 = -3. * (1.-v) * (1.-v);
float dbv1 =  3. * (1.-v) * (1.-3.*v);
float dbv2 =  3. * v *      (2.-3.*v);
float dbv3 =  3. * v *      v;

// finally, we get to compute something:

gl_Position =          bu0 * ( bv0*p00 + bv1*p01 + bv2*p02 + bv3*p03 )
                     + bu1 * ( bv0*p10 + bv1*p11 + bv2*p12 + bv3*p13 )
                     + bu2 * ( bv0*p20 + bv1*p21 + bv2*p22 + bv3*p23 )
                     + bu3 * ( bv0*p30 + bv1*p31 + bv2*p32 + bv3*p33
```



In the TES Shader – Computing the Normal, given a u and v

33



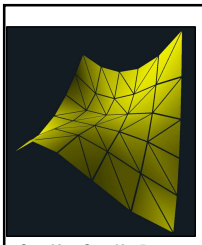
Tangent Vectors obtained by differentiating the position equation with respect to *u* and *v*:

```
vec4 dpdu =          dbu0 *  ( bv0*p00 + bv1*p01 + bv2*p02 + bv3*p03 )
                   + dbu1 * ( bv0*p10 + bv1*p11 + bv2*p12 + bv3*p13 )
                   + dbu2 * ( bv0*p20 + bv1*p21 + bv2*p22 + bv3*p23 )
                   + dbu3 * ( bv0*p30 + bv1*p31 + bv2*p32 + bv3*p33 );

vec4 dpdv =          bu0 *  ( dbv0*p00 + dbv1*p01 + dbv2*p02 + dbv3*p03 )
                   + bu1 * ( dbv0*p10 + dbv1*p11 + dbv2*p12 + dbv3*p13 )
                   + bu2 * ( dbv0*p20 + dbv1*p21 + dbv2*p22 + dbv3*p23 )
                   + bu3 * ( dbv0*p30 + dbv1*p31 + dbv2*p32 + dbv3*p33 );

teNormal = normalize( cross( dpdu.xyz, dpdv.xyz ) );
}
```

Vector cross product to get the perpendicular normal to the two tangent vectors.

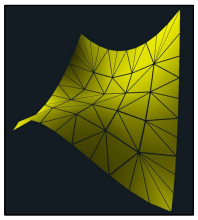
Example: A Bézier Surface

34

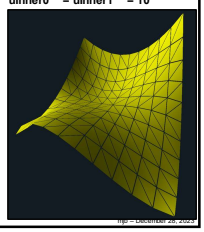


uOuter02 = uOuter13 = 5
uInner0 = uInner1 = 5

uOuter02 = uOuter13 = 10
uInner0 = uInner1 = 5

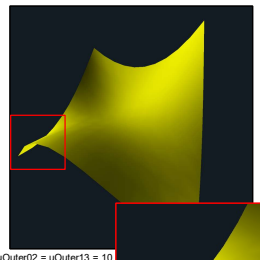


uOuter02 = uOuter13 = 10
uInner0 = uInner1 = 10

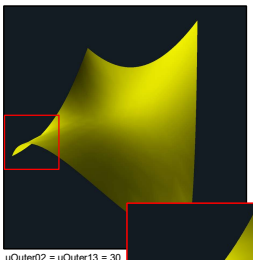


Tessellation Levels and Smooth Shading

35



uOuter02 = uOuter13 = 10
uInner0 = uInner1 = 10



uOuter02 = uOuter13 = 30
uInner0 = uInner1 = 10

Smoothing the edge boundaries is one of the reasons that you can set Outer and Inner tessellation levels separately

Example: Whole-Sphere Subdivision

36

spheresubd.glib

```
##OpenGL GLIB

Vertex          spheresubd.vert
Fragment        spheresubd.frag
TessControl     spheresubd.tcs
TessEvaluation  spheresubd.tes
Geometry        spheresubd.geom
Program SphereSubd                          \
        uDetail <1 30 200>                  \
        uScale <0.1 1. 10.>                 \
        uShrink <0. 1. 1.>                  \
        uFlat <false>                               \
        uColor {1. 1. 0. 0.}                \
        uLightX <-10. 5. 10.>  uLightY <-10. 10. 10.>  uLightZ <-10. 10. 10.>

Color 1. 1. 0.

NumPatchVertices 1

glBegin gl_patches
        glVertex 0. 0. 0. .2
        glVertex 0. 1. 0. .3
        glVertex 0. 0. 1. .4
glEnd
```

Using the x, y, z, and w to specify the center and radius of the sphere

Example: Whole-Sphere Subdivision

37

spheresubd.vert

```
#version 400 compatibility

out vec3  vCenter;
out float  vRadius;

void
main( )
{
        vCenter = gl_Vertex.xyz;
        vRadius = gl_Vertex.w;

        gl_Position = vec4( 0., 0., 0., 1. );
                // doesn't matter now – we will fill in the coords later
}
```

Using the x, y, z, and w to specify the center and radius of the sphere

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Example: Whole-Sphere Subdivision

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spheresubd.tcs

```
#version 400 compatibility
#extension GL_ARB_tessellation_shader : enable

in float   vRadius[  ];
in vec3  vCenter[  ];

patch out float   tcRadius;
patch out vec3  tcCenter;

uniform float uDetail;
uniform float uScale;

layout( vertices = 1 )  out;

void
main( )
{
        gl_out[ gl_InvocationID ].gl_Position = gl_in[ 0 ].gl_Position;     // (0.0.0.1)

        tcCenter = vCenter[ 0 ];
        tcRadius = vRadius[ 0 ];

        gl_TessLevelOuter[0]  = 2.;
        gl_TessLevelOuter[1]  = uScale * tcRadius * uDetail;
        gl_TessLevelOuter[2]  = 2.;
        gl_TessLevelOuter[3]  = uScale * tcRadius * uDetail;
        gl_TessLevelInner[0]  = uScale * tcRadius * uDetail;
        gl_TessLevelInner[1]  = uScale * tcRadius * uDetail;
}
```

Using the scale and the radius to help set the tessellation detail

Outer[0] and Outer[2] are the number of divisions at the poles. Outer[1] and Outer[3] are the number of divisions at the vertical seams. Inner[0] and Inner[1] are the inside sphere detail.

Example: Whole-Sphere Subdivision

39

spheresubd.tes

```
#version 400 compatibility
#extension GL_ARB_tessellation_shader : enable

uniform float  uScale;

layout( quads, equal_spacing, ccw)  in;

patch in float   tcRadius;
patch in vec3  tcCenter;

out vec3        teNormal;

const float PI = 3.14159265;

void main( )
{
        vec3 p = gl_in[0].gl_Position.xyz;

        float u  = gl_TessCoord.x;
        float v  = gl_TessCoord.y;

        float phi   =       PI * ( u - .5 );
        float theta = 2. * PI * ( v - .5 );

        float cosphi = cos(phi);
        vec3 xyz = vec3( cosphi*cos(theta), sin(phi), cosphi*sin(theta) );
        teNormal = xyz;

        xyz *= ( uScale * tcRadius );
        xyz += tcCenter;

        gl_Position = gl_ModelViewMatrix * vec4( xyz,1. );
}
```

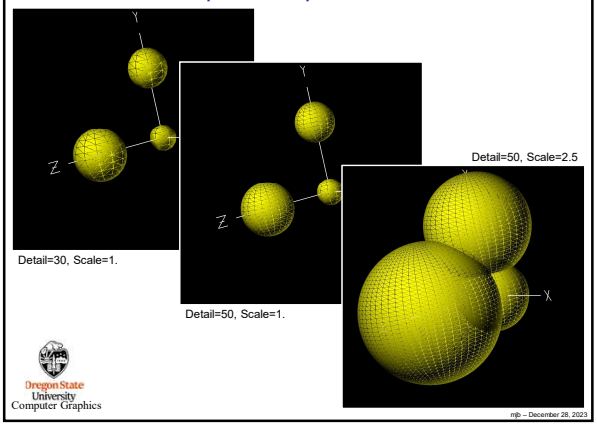
$$-\frac{\pi}{2} \le \phi \le +\frac{\pi}{2}$$

$$-\pi \le \theta \le +\pi$$

Turning u and v into spherical coordinates

Example: Whole-Sphere Subdivision

40



Detail=30, Scale=1.

Detail=50, Scale=1.

Detail=50, Scale=2.5

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Making the Whole-Sphere Subdivision *Adapt* to Screen Coverage, I

41

sphereadapt.tcs, I

```
#version 400 compatibility
#extension GL_ARB_tessellation_shader : enable

in float   vRadius[  ];
in vec3  vCenter[  ];

patch out float   tcRadius;
patch out vec3  tcCenter;

uniform float uDetail;

layout( vertices = 1 )  out;

void main( )
{
        gl_out[ gl_InvocationID ].gl_Position = gl_in[ 0 ].gl_Position;          // (0,0,0,1)

        tcCenter = vCenter[ 0 ];
        tcRadius = vRadius[ 0 ];

        vec4 mx = vec4( vCenter[0] - vec3( vRadius[0], 0., 0. ),  1. );
        vec4 px  = vec4( vCenter[0] + vec3( vRadius[0], 0., 0. ),  1. );
        vec4 my = vec4( vCenter[0] - vec3( 0., vRadius[0], 0. ),  1. );
        vec4 py  = vec4( vCenter[0] + vec3( 0., vRadius[0], 0. ),  1. );
        vec4 mz = vec4( vCenter[0] - vec3( 0., 0., vRadius[0] ),  1. );
        vec4 pz  = vec4( vCenter[0] + vec3( 0., 0., vRadius[0] ),  1. );
```

Extreme points of the sphere

Making the Whole-Sphere Subdivision *Adapt* to Screen Coverage, II

42

sphereadapt.tcs, II

```
        mx = gl_ModelViewProjectionMatrix * mx;
        px  = gl_ModelViewProjectionMatrix * px;
        my = gl_ModelViewProjectionMatrix * my;
        py  = gl_ModelViewProjectionMatrix * py;
        mz = gl_ModelViewProjectionMatrix * mz;
        pz  = gl_ModelViewProjectionMatrix * pz;

        mx.xy /= mx.w;
        px.xy  /= px.w;
        my.xy /= my.w;
        py.xy  /= py.w;
        mz.xy /= mz.w;
        pz.xy  /= pz.w;

        float dx = distance( mx.xy,  px.xy );
        float dy = distance( my.xy,  py.xy );
        float dz = distance( mz.xy,  pz.xy );
        float dmax = sqrt( dx*dx + dy*dy + dz*dz );

        gl_TessLevelOuter[0] = 2.;
        gl_TessLevelOuter[1] = dmax * uDetail;
        gl_TessLevelOuter[2] = 2.;
        gl_TessLevelOuter[3] = dmax * uDetail;
        gl_TessLevelInner[0]  = dmax * uDetail;
        gl_TessLevelInner[1]  = dmax * uDetail;
}
```

Extreme points of the sphere in Clip space

Extreme points of the sphere in NDC space

How long are the lines between the extreme points?

We no longer use uScale or tcRadius. But, we do use uDetail to provide a way to convert from NDC to Screen Space or to indicate the quality you'd like

(I.e., uDetail depends on how good you want the spheres to look and on how large the window is in pixels.)

Making the Whole-Sphere Subdivision *Adapt* to Screen Coverage, III

43

sphereadapt.tes

```
#version 400 compatibility
#extension GL_ARB_tessellation_shader : enable

layout( quads, equal_spacing, ccw) in;

patch in float   tcRadius;
patch in vec3  tcCenter;

out vec3         teNormal;

const float PI = 3.14159265;

void main( )
{
        vec3 p = gl_in[0].gl_Position.xyz;

        float u = gl_TessCoord.x;
        float v = gl_TessCoord.y;
        float w = gl_TessCoord.z;

        float phi    = PI *      ( u - .5 );
        float theta = 2. * PI * ( v - .5 );

        float cosphi = cos(phi);
        vec3 xyz = vec3( cosphi*cos(theta), sin(phi), cosphi*sin(theta) );
        teNormal = xyz;

        xyz *=  tcRadius;
        xyz += tcCenter;

        gl_Position = gl_ModelViewMatrix * vec4( xyz,1. );
}
```

$$-\frac{\pi}{2} \le \phi \le +\frac{\pi}{2}$$

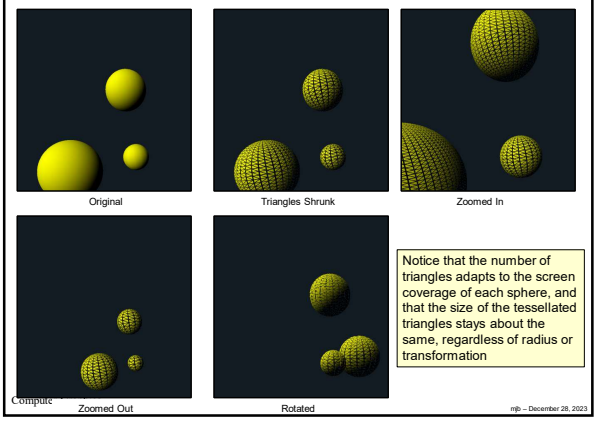
$$-\pi \le \theta \le +\pi$$

Spherical coordinates

No longer uses uScale

Making the Whole-Sphere Subdivision *Adapt* to Screen Coverage, IV

44

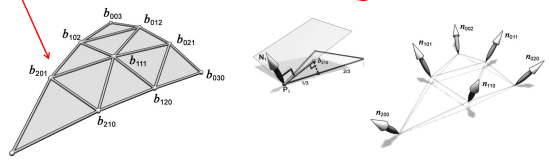


Notice that the number of triangles adapts to the screen coverage of each sphere, and that the size of the tessellated triangles stays about the same, regardless of radius or transformation

Example: PN Triangles

45

General idea: turn each triangle into a triangular Bézier patch. Create the Bézier control points by using the surface normals at the corner vertices. The Bézier patch equation can then be interpolated to any level of tessellation.



Alex Vlachos, Jörg Peters, Chas Boyd, and Jason Mitchell, "Curved PN Triangles", *Proceedings of the 2001 Symposium on Interactive 3D Graphics*, pp.159 – 166.

Observation: triangles are usually passed in with points (P) and normals (N). Using this method, those triangles can be broken into a series of smoother triangles internally. AMD actually had this in their firmware before tessellation shaders made it unnecessary.

Example: PN Triangles

46

pntriangles.vert

```
#version 400 compatibility
uniform float  uScale;
out vec3        vNormal;
void  main( )
{
        vec3 xyz = gl_Vertex.xyz;
        xyz *= uScale;
        gl_Position = gl_ModelViewMatrix * vec4( xyz,  1. );
        vNormal = normalize( gl_NormalMatrix * gl_Normal );
}
```

pntriangles.tcs

```
#version 400 compatibility
#ension GL_ARB_tessellation_shader : enable
uniform int      uOuter, uInner;
uniform float    uScale;
layout( vertices = 3 )  out;
in vec3    vNormal[ ];
out vec3  tcNormals[ ];

void main( )
{
        teNormals[ gl_InvocationID  ] = vNormal[ gl_InvocationID  ];
        gl_out[ gl_InvocationID ].gl_Position = gl_in[ gl_InvocationID ].gl_Position;

        gl_TessLevelOuter[0] = uScale * float(uOuter);
        gl_TessLevelOuter[1] = uScale * float(uOuter);
        gl_TessLevelOuter[2] = uScale * float(uOuter);
        gl_TessLevelInner[0]  = uScale * float(uInner);
}
```


Example: PN Triangles

47

pntriangles.tes, I

```
#version 400 compatibility
#ension  GL_ARB_tessellation_shader  : enable
in vec3     tcNormals[  ];
out vec3  teNormal;
layout(  triangles,  equal_spacing,  ccw)  in;

void  main( )
{
        vec3 p1 = gl_in[0].gl_Position.xyz;
        vec3 p2 = gl_in[1].gl_Position.xyz;
        vec3 p3 = gl_in[2].gl_Position.xyz;

        vec3 n1 = tcNormals[0];
        vec3 n2 = tcNormals[1];
        vec3 n3 = tcNormals[2];

        float u = gl_TessCoord.x;
        float v = gl_TessCoord.y;
        float w = gl_TessCoord.z;

        vec3 b300 = p1;
        vec3 b030 = p2;
        vec3 b003 = p3;

        float w12 = dot( p2 - p1, n1 );
        float w21 = dot( p1 - p2, n2 );
        float w13 = dot( p3 - p1, n1 );
        float w31 = dot( p1 - p3, n3 );
        float w23 = dot( p3 - p2, n2 );
        float w32 = dot( p2 - p3, n3 );
```


Example: PN Triangles

48

pntriangles.tes, II

```
        vec3 b210 = ( 2.*p1 + p2 - w12*n1 ) / 3.;
        vec3 b120 = ( 2.*p2 + p1 - w21*n2 ) / 3.;
        vec3 b021 = ( 2.*p2 + p3 - w23*n2 ) / 3.;
        vec3 b012 = ( 2.*p3 + p2 - w32*n3 ) / 3.;
        vec3 b102 = ( 2.*p3 + p1 - w31*n3 ) / 3.;
        vec3 b201 = ( 2.*p1 + p3 - w13*n1 ) / 3.;

        vec3 ee = ( b210 + b120 + b021 + b012 + b102 + b201 ) / 6.;
        vec3 vv = ( p1 + p2 + p3 ) / 3.;
        vec3 b111 = ee + ( ee - vv ) / 2.;

        vec3 xyz =   1.*b300*w*w*w + 1.*b030*u*u*u   + 1.*b003*v*v*v  +
                     3.*b210*u*w*w  + 3.*b120*u*u*w + 3.*b201*v*w*w +
                     3.*b021*u*u*v   + 3.*b102*v*v*w  + 3.*b012*u*v*v  +
                     6.*b111*u*v*w;

        float v12 = 2. * dot( p2-p1, n1+n2 ) / dot( p2-p1, p2-p1 );
        float v23 = 2. * dot( p3-p2, n2+n3 ) / dot( p3-p2, p3-p2 );
        float v31 = 2. * dot( p1-p3, n3+n1 ) / dot( p1-p3, p1-p3 );

        vec3 n200 = n1;
        vec3 n020 = n2;
        vec3 n002 = n3;
        vec3 n110 = normalize( n1 + n2 - v12*(p2-p1) );
        vec3 n011 = normalize( n2 + n3 - v23*(p3-p2) );
        vec3 n101 = normalize( n3 + n1 - v31*(p1-p3) );
        Normal =     n200*w*w + n020*u*u + n002*v*v +
                     n110*w*u + n011*u*v + n101*w*v;

        gl_Position = vec4( xyz,  1. );
}
```

Example: PN Triangles

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pntriangles.geom

```
#version 400 compatibility
#ension GL_gpu_shader4: enable
#ension GL_geometry_shader4: enable

uniform float   uShrink;
in vec3         teNormal[  ];
out float       gLightIntensity;
const vec3      LIGHTPOS = vec3( 5., 10., 10. );

vec3 V[3];
vec3 CG;

void
ProduceVertex(  int  v )
{
        gLightIntensity = abs( dot( normalize(LIGHTPOS - V[v]), normalize(teNormal[v]) )
);
        gl_Position = gl_ProjectionMatrix * vec4( CG + uShrink * ( V[v] - CG ), 1. );
        EmitVertex( );
}

void main( )
{
        V[0]  =  gl_PositionIn[0].xyz;
        V[1]  =  gl_PositionIn[1].xyz;
        V[2]  =  gl_PositionIn[2].xyz;

        CG = ( V[0] + V[1] + V[2] ) / 3.;

        ProduceVertex(  0 );
        ProduceVertex(  1 );
        ProduceVertex(  2 );
}
```

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Example: PN Triangles

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pntriangles.frag

```
#version 400 compatibility

in float    gLightIntensity;

const vec3 COLOR = vec3( 1., 1., 0. );

void
main( )
{
        gl_FragColor = vec4(  gLightIntensity*COLOR,  1. );
}
```

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The Cow's Tail is a Good Example of using PN Triangles

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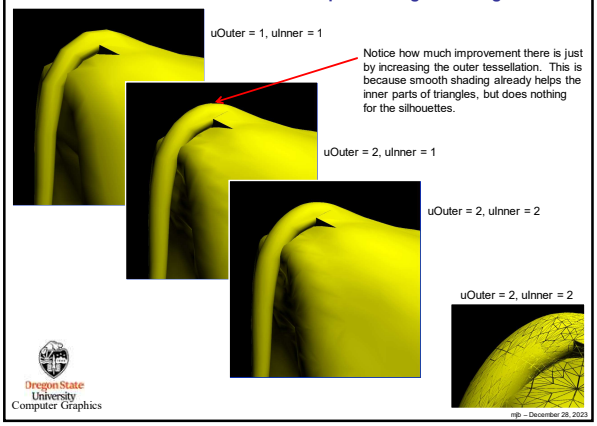

Notice how much improvement there is just by increasing the outer tessellation. This is because smooth shading already helps the inner parts of triangles, but does nothing for the silhouettes.

uOuter = 2, uInner = 2

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The Difference Between Tessellation Shaders and Geometry Shaders

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By now, you are probably confused about when to use a Geometry Shader and when to use a Tessellation Shader. Both are capable of creating new geometry from existing geometry. See if this helps.

Use a **Geometry Shader** when:

1. You need to convert an input topology into a *different output topology*, such as in the silhouette and hedgehog shaders (triangles→lines) or the explosion shader (triangles→points)
2. You need some sort of geometry processing to come after the Tessellation Shader (such as how the shrink shader was used).

Use a **Tessellation Shader** when:

1. One of the built-in tessellation patterns will suit your needs.
2. You need more than 6 input vertices to define the surface being tessellated.
3. You need more output vertices than a Geometry Shader can provide.

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Demonstrating the Limits of Tessellation Shaders

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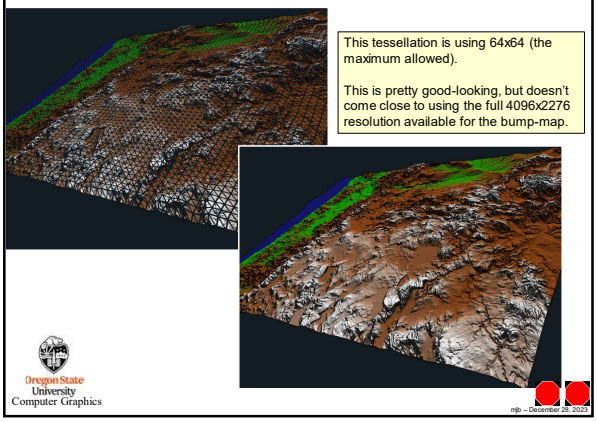

This tessellation is using 64x64 (the maximum allowed).

This is pretty good-looking, but doesn't come close to using the full 4096x2276 resolution available for the bump-map.

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