# Local Invariant Features: What? Why? When? How?

Tinne Tuytelaars
Tutorial ECCV 2006
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#### Overview

#### Local Invariant Features: What? Why?

- Introduction
- Overview of existing detectors
- Quantitative and qualitative comparison

#### Local Invariant Features: When? How?

- Feature descriptors
- Applications
- Conclusions

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## Introduction

#### Wide baseline matching





#### Introduction

#### Recognition of specific objects







Rothganger et al. '03

Lowe et al. '02

Ferrari et al. '04

## Introduction

Object class recognition



# So what's the novelty?

Local character

# History

History of interest point detectors goes a long way back...

- Corner detectors
- Blob detectors
- Edgel detectors

# So what's the novelty?

Local character

Level of invariance

Local invariant features: a new paradigm

- Not just a method to select interesting locations in the image, or to speed up analysis
- But rather a new image representation, that allows to describe the objects / parts without the need for segmentation

# Properties of the ideal feature

Local: features are local, so robust to occlusion and clutter (no prior segmentation)

**Invariant** (or covariant)

Robust: noise, blur, discretization, compression, etc. do not have a big impact on the feature

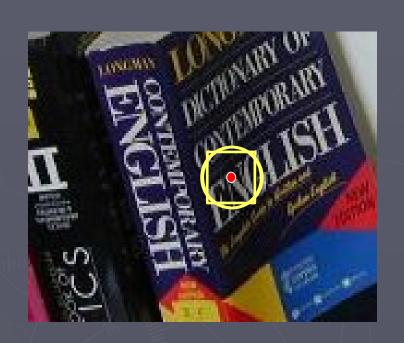
Distinctive: individual features can be matched to a large database of objects

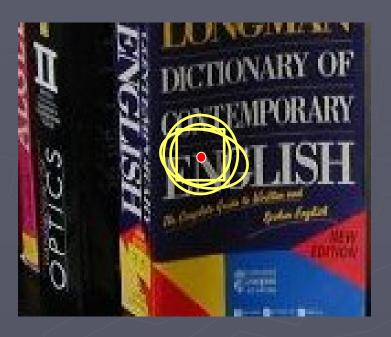
Quantity: many features can be generated for even small objects

**Accurate**: precise localization

Efficient: close to real-time performance

## The need for invariance





## Terminology: Invariant or Covariant?

When a transformation is applied to an image, an invariant measure remains unchanged. a covariant measure changes in a way consistent with the image transformation.

Terminology: 'detector' or 'extractor'

#### Geometric transformations

**Translation** 

Euclidean (translation + rotation)

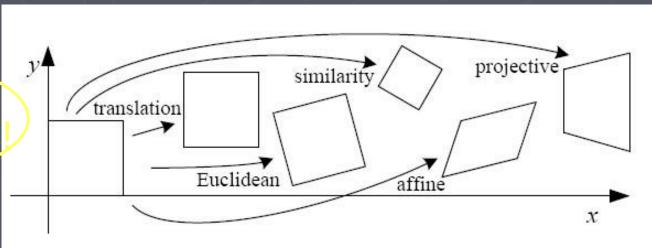
Similarity (transl. + rotation + scale)

Affine transformations

Projective transformations

Only holds

for planar patches



#### Photometric transformations



scaling + offset

#### Disturbances

Noise Image blur Discretizati

Discretization errors

Compression artefacts

Deviations from the mathematical model (non-linearities, non-planarities, etc.)

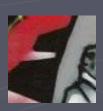
Intra-class variations

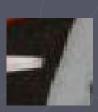
## How to cope with transformations?

Exhaustive search Invariance Robustness

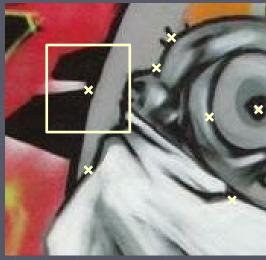


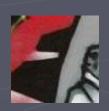


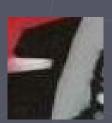




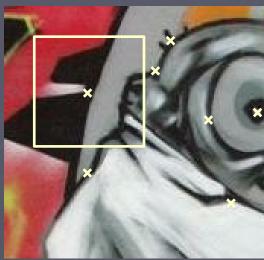


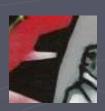


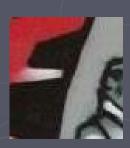




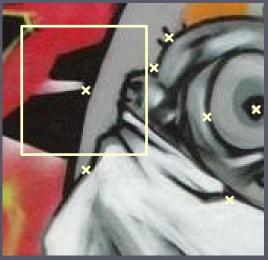


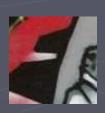


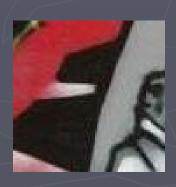










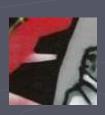


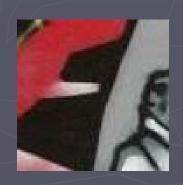
#### Invariance

Extract patch from each image individually









#### Invariance

#### Integration, e.g.

moment invariants, ...



#### Heuristics, e.g.

- Difference of intensity values for photom. offset
- Ratio of intensity values for photom. scalefactor

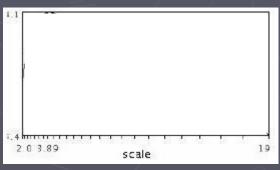
#### Selection and normalization, e.g.

- Automatic scale selection (Lindeberg et al., 1996)
- Orientation assignment
- Affine normalization ('deskewing')

4 4 5

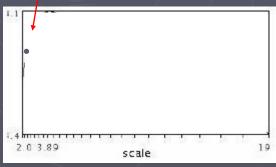
Lindeberg et al., 1996





 $f(I_{i_1...i_m}(x,\sigma))$ 

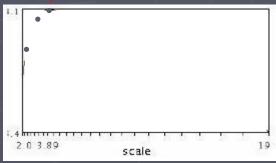




 $f(I_{i_1...i_m}(x,\sigma))$ 



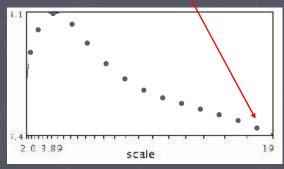




 $f(I_{i_1...i_m}(x,\sigma))$ 

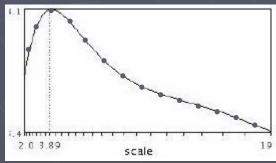






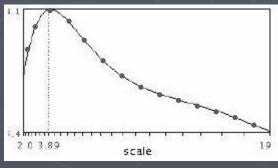
 $f(I_{i_1...i_m}(x,\sigma))$ 

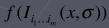




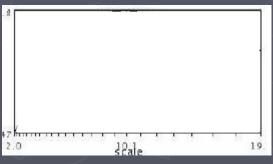
 $f(I_{i_1...i_m}(x,\sigma))$ 





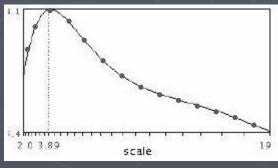






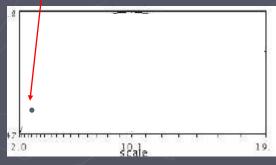
$$f(I_{i_1...i_m}(x',\sigma))$$



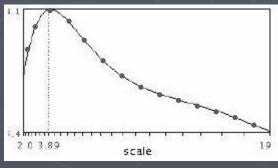






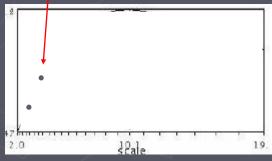






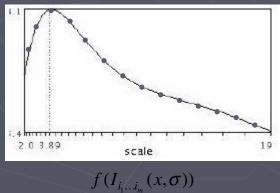






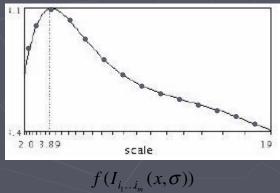
$$f(I_{i_1...i_m}(x',\sigma))$$

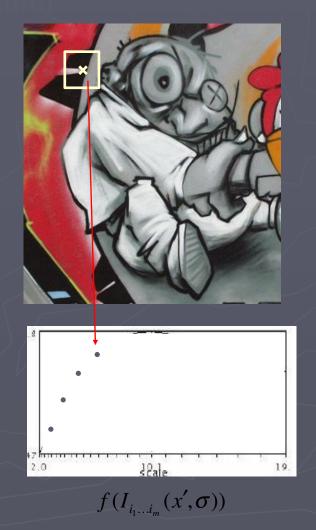




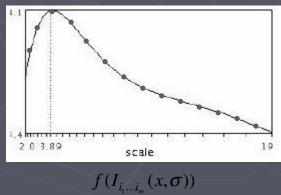








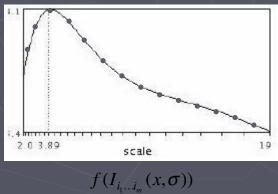




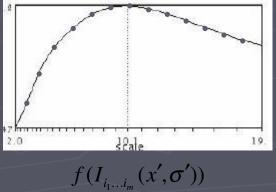


 $f(I_{i_1...i_m}(x',\sigma))$ 





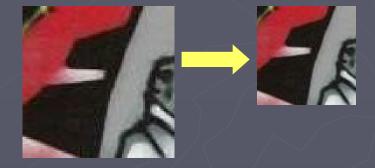




#### Automatic scale selection

Normalize: rescale to fixed size





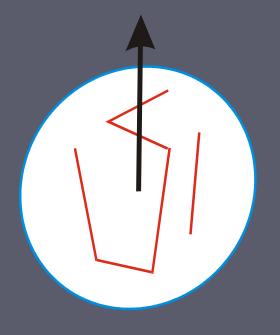
#### Orientation assignment

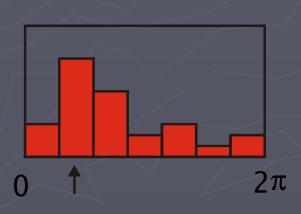
Lowe, SIFT, 1999

Compute orientation histogram

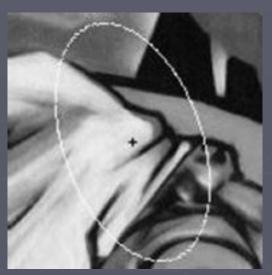
Select dominant orientation

Normalize: rotate to fixed orientation





# Affine normalization ('deskewing')



rotate





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#### Overview of existing detectors

Hessian & Harris

Lowe: DoG

Mikolajczyk & Schmid:

Hessian/Harris-Laplacian/Affine

Tuytelaars & Van Gool: EBR and IBR

Matas: MSER

Kadir & Brady: Salient Regions

Others

#### Overview of existing detectors

#### Hessian & Harris

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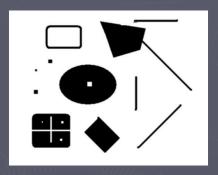
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Others

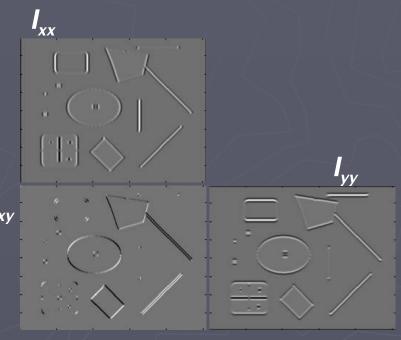
#### Hessian detector (Beaudet, 1978)

#### Hessian determinant



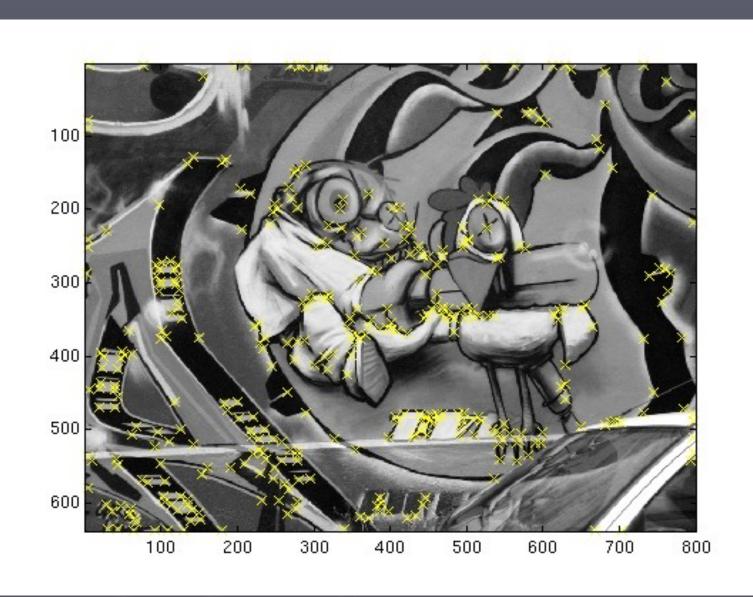
$$Hessian(I) = \begin{bmatrix} I_{xx} & I_{xy} \\ I_{xy} & I_{yy} \end{bmatrix}^{xy}$$

$$\det(Hessian(I)) = I_{xx}I_{yy} - I_{xy}^{2}$$





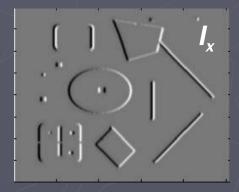
### Hessian (Beaudet, 1978)



Second moment matrix / autocorrelation matrix

$$\mu(\sigma_I, \sigma_D) = g(\sigma_I) * \begin{bmatrix} I_x^2(\sigma_D) & I_x I_y(\sigma_D) \\ I_x I_y(\sigma_D) & I_y^2(\sigma_D) \end{bmatrix}$$

1. Image derivatives  $g_{x}(\sigma_{D}), g_{y}(\sigma_{D}),$ 

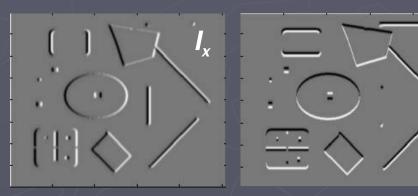




Second moment matrix / autocorrelation matrix

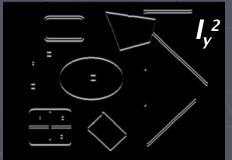
$$\mu(\sigma_I, \sigma_D) = g(\sigma_I) * \begin{bmatrix} I_x^2(\sigma_D) & I_x I_y(\sigma_D) \\ I_x I_y(\sigma_D) & I_y^2(\sigma_D) \end{bmatrix}$$

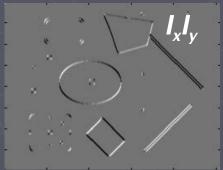
1. Image derivatives  $g_x(\sigma_D)$ ,  $g_y(\sigma_D)$ ,



2. Square of derivatives







Second moment matrix / autocorrelation matrix

Second Moment Matrix / autocorrelation 
$$\mu(\sigma_I, \sigma_D) = g(\sigma_I) * \begin{bmatrix} I_x^2(\sigma_D) & I_xI_y(\sigma_D) \\ I_xI_y(\sigma_D) & I_y^2(\sigma_D) \end{bmatrix}$$
1. Image derivatives





2. Square of derivatives

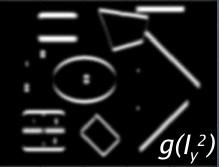


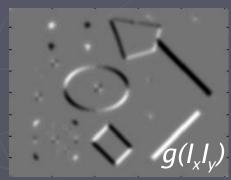




3. Gaussian filter  $g(\sigma_i)$ 



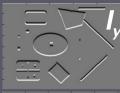




# Second moment matrix autocorrelation matrix

1. Image derivatives





2. Square of derivatives







3. Gaussian filter  $g(\sigma_i)$ 



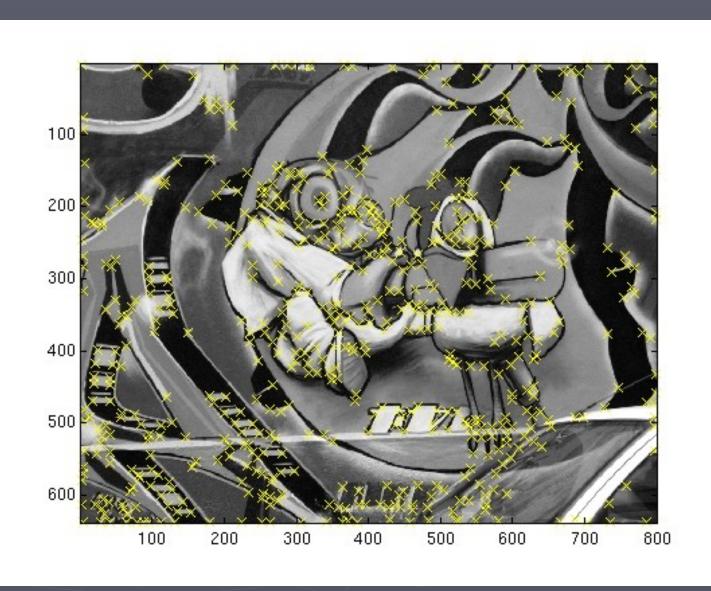




4. Cornerness function – both eigenvalues are  $\frac{\text{strong}_{har}}{\text{strong}_{har}} = \det[\mu(\sigma_I, \sigma_D)] - \alpha[\operatorname{trace}(\mu(\sigma_I, \sigma_D))] = g(I_x^2)g(I_y^2) - [g(I_xI_y)]^2 - \alpha[g(I_x^2) + g(I_y^2)]^2$ 

5. Non-maxima suppression





#### Overview of existing detectors

Hessian & Harris

Lowe: DoG

Mikolajczyk & Schmid: Hessian/Harris-Laplacian/Affine

Tuytelaars & Van Gool: EBR and IBR

Matas: MSER

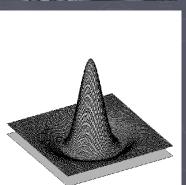
Kadir & Brady: Salient Regions

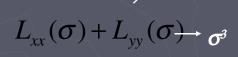
Others

# Scale invariant detectors Laplacian of Gaussian

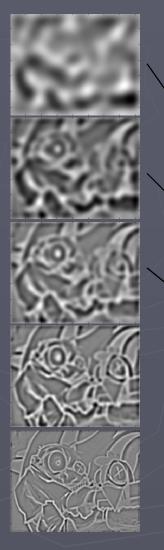
Local maxima in scale space of Laplacian of Gaussian LoG

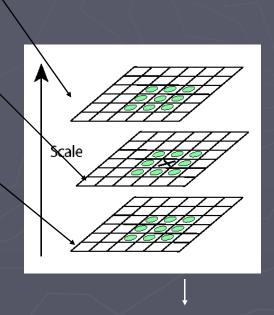






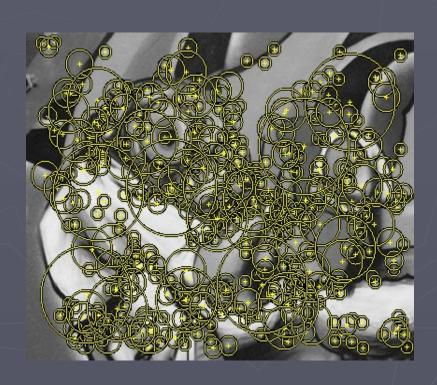






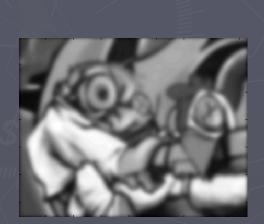
list of ( x, y, σ)

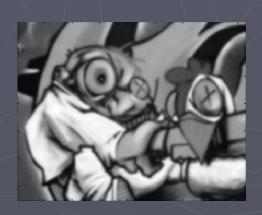
# Scale invariant detectors Laplacean of Gaussian



#### Lowe's DoG

Difference of Gaussians as approximation of the Laplacian of Gaussian

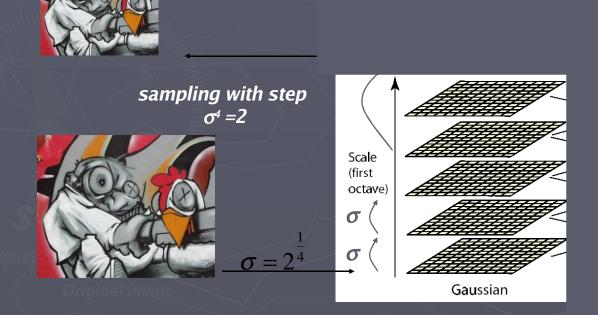


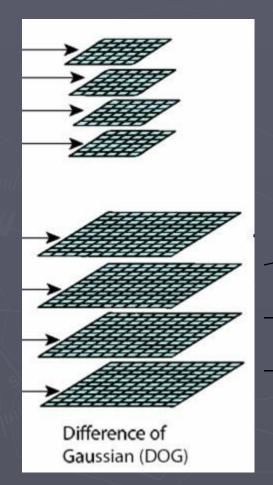


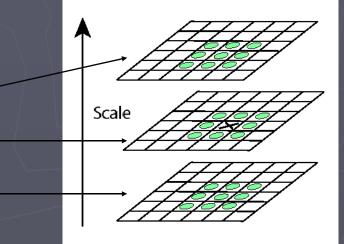


#### Lowe's DoG

Difference of Gaussians as approximation of the Laplacian of Gaussian







list of ( x, y, σ)

# Lowe's DoG



## Appreciation

#### scale-invariant

- simple, efficient scheme
- laplacian fires more on edges than determinant of hessian

#### Overview of existing detectors

Hessian & Harris

Lowe: DoG

Mikolajczyk & Schmid: Hessian/Harris-Laplacian/Affine

Tuytelaars & Van Gool: EBR and IBR

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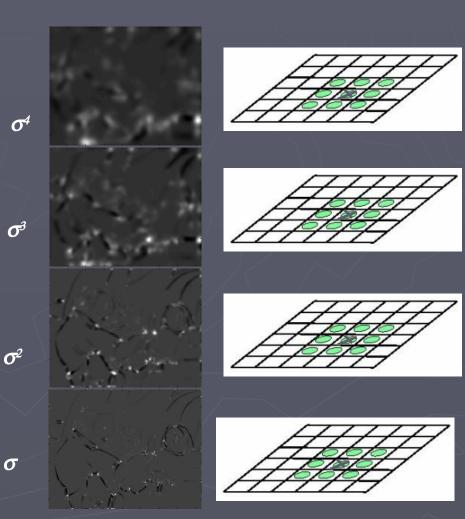
# Mikolajczyk & Schmid

Harris Laplace
Hessian Laplace
Harris Affine
Hessian Affine

# Mikolajczyk: Harris Laplace

Initialization:
 Multiscale Harris
 corner detection





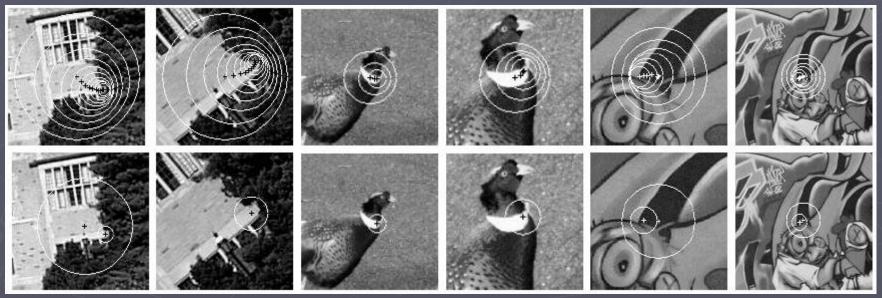
**Computing Harris function** 

**Detecting local maxima** 

### Mikolajczyk: Harris Laplace

- 1. Initialization: Multiscale Harris corner detection
- 2. Scale selection based on Laplacian

#### **Harris** points

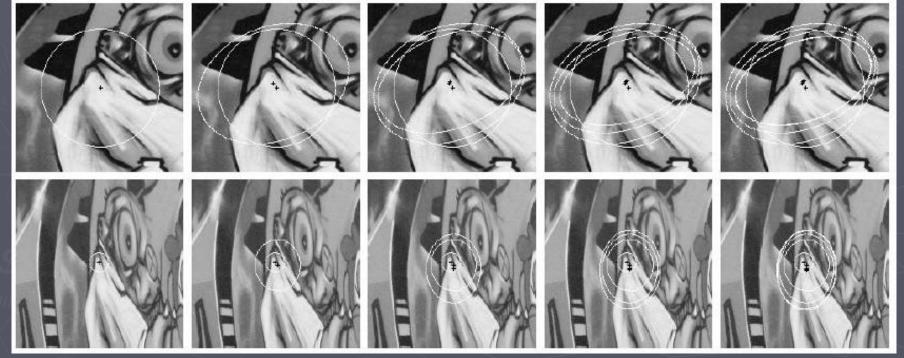


**Harris-Laplace points** 

# Mikolajczyk: Harris Affine

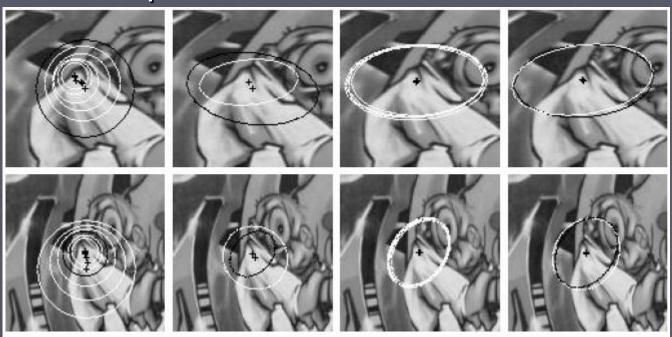
Initialization with Harris Laplace Estimate shape based on second moment matrix Using normalization / deskewing

Iterative algorithm

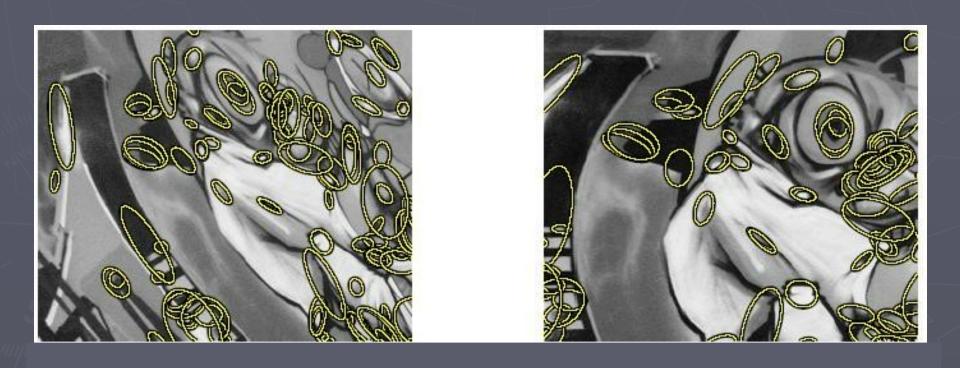


### Mikolajczyk: Harris Affine

- Detect multi-scale Harris points
- 2. Automatically select the scales
- 3. Adapt affine shape based on second order moment matrix
- 4. Refine point location

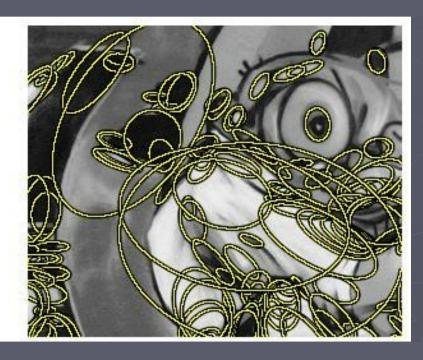


# Harris Affine



#### Hessian Affine





## Appreciation

- Scale or affine invariant

  Detects blob- and corner-like structures
- large number of regions
- well suited for object class recognition
- less accurate than some competitors

#### Overview of existing detectors

Lowe: DoG

Lindeberg: scale selection

Mikolajczyk & Schmid:

Hessian/Harris-Laplacian/Affine

Tuytelaars & Van Gool: EBR and IBR

Matas: MSER

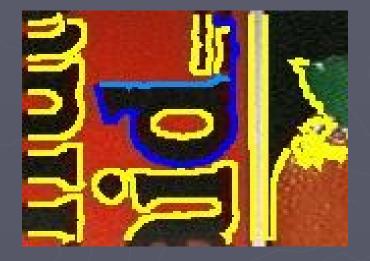
Kadir & Brady: Salient Regions

Others

**1.** Select Harris corners



- Select Harris corners
- 2. Find Canny edges



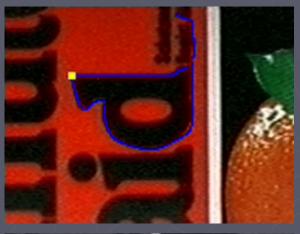


- Select Harris corners
- Find Canny edges
- Evaluate relative affine invariant parameter along edges



$$l_i = \int abs(|p_i^{(1)}(s_i)| p - p_i(s_i)|)ds_i$$

- 1. Select Harris corners
- Find Canny edges
- Evaluate relative affine invariant parameter along edges
- 4. Construct 1-dimensional family of parallelograms





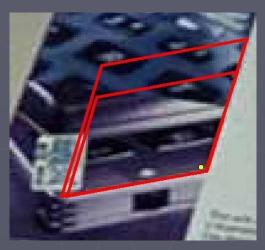
- Select Harris corners
- Find Canny edges
- 3. Evaluate relative affine invariant parameter along edges
- Construct 1-dimensional family of parallelograms
- 5. Select parallelogram based on local extrema of invariant function

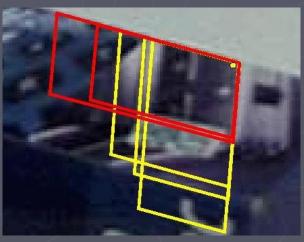


$$M_{pq}^{a} = \int [I(x, y)]^{a} x^{p} y^{q} dx dy$$

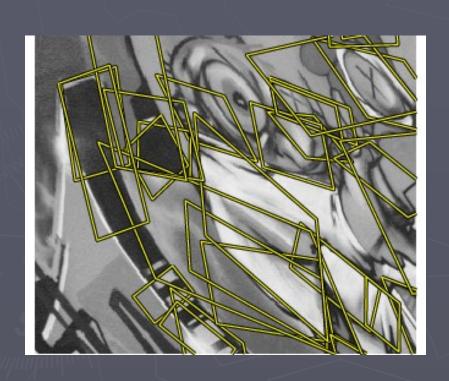
## Tuytelaars: edge-based regions

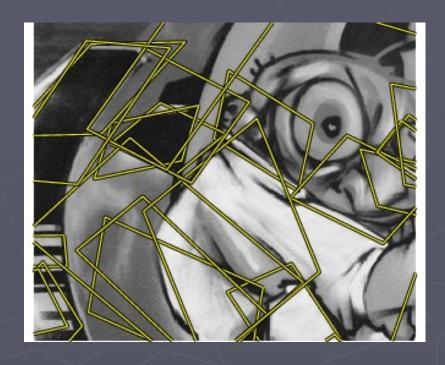
Variant for straight lines...



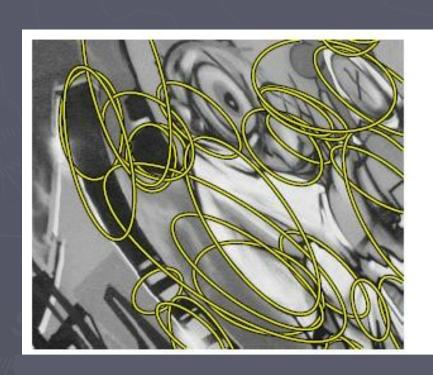


## Edge-based regions





## Edge-based regions





#### Appreciation

Affine invariant

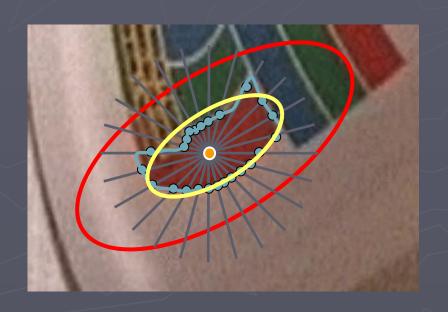
Detects corner-like structures

- Works well in structured scenes
- Doesn't cross edges/object contours
- Depends on presence of edges

# Tuytelaars: intensity-based regions

- 1. Select intensity extrema
- 2. Consider intensity profile along rays
- 3. Select maximum of invariant function f(t) along each ray
- 4. Connect all local maxima
- 5. Fit an ellipse

$$f(t) = \frac{abs(I_0 - I)}{\max(\frac{\int abs(I_0 - I)dt}{t}, d)}$$



## Intensity-based regions





#### Appreciation

Affine invariant

Detects 'blob'-like structures

- Accurate regions
- Especially good on printed material

#### Overview of existing detectors

Lowe: DoG

Lindeberg: scale selection

Mikolajczyk & Schmid:

Hessian/Harris-Laplacian/Affine

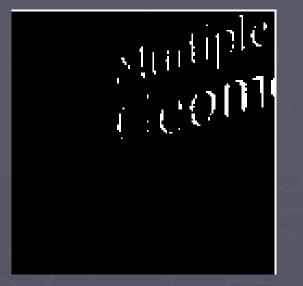
Tuytelaars & Van Gool: EBR and IBR

Matas: MSER

Kadir & Brady: Salient Regions

Others

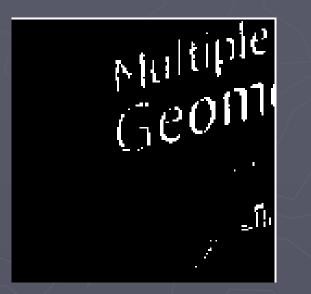






































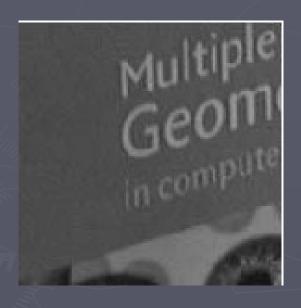














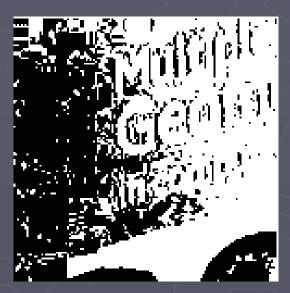












Extremal region: region such that

$$\forall p \in Q, \forall q \in \delta Q: \frac{I(p)>I(q)}{I(p)< I(q)}$$

Order regions

$$Q_1 \subset ... \subset Q_i \subset Q_{i+1} \subset ...Q_n$$

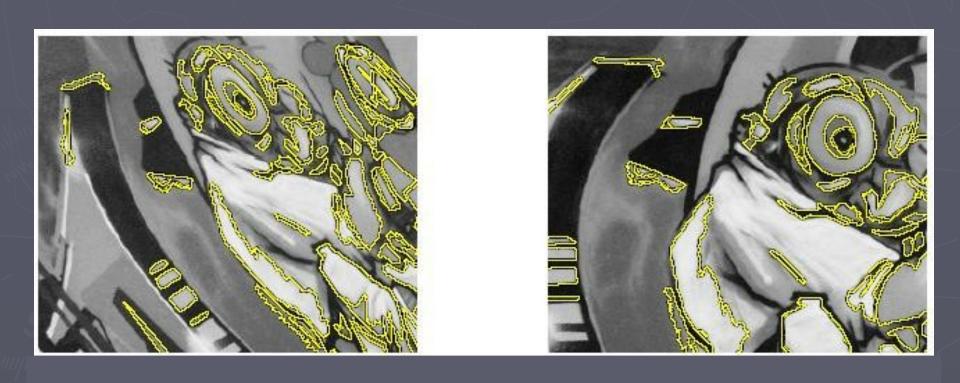
Maximally Stable Extremal Region: local minimum of

$$q(i) = Q_{i+\Delta} \setminus Q_{i-\Delta} \mid / Q_i$$





#### Maximally Stable Extremal Regions



#### Appreciation

- Affine invariant
  Detects blob-like structures
  - Simple, efficient scheme
  - High repeatability
  - Fires on similar features as IBR (regions need not be convex, but need to be closed)
  - Sensitive to image blur

#### Overview of existing detectors

Lowe: DoG

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Mikolajczyk & Schmid:

Hessian/Harris-Laplacian/Affine

Tuytelaars & Van Gool: EBR and IBR

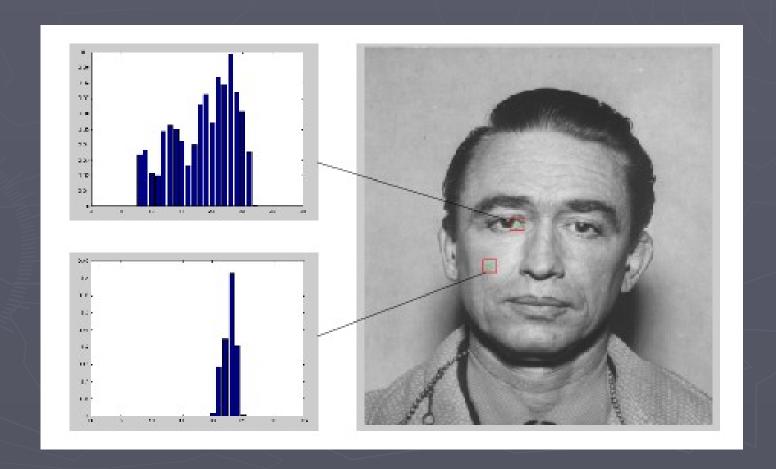
Matas: MSER

Kadir & Brady: Salient Regions

Others

### Kadir & Brady's salient regions

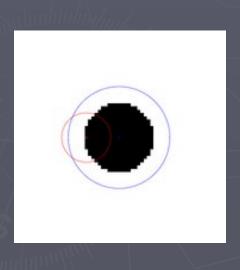
#### Based on entropy

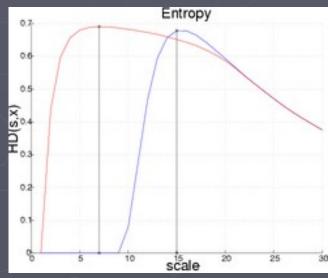


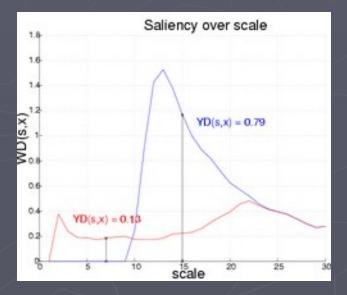
### Kadir & Brady's salient regions

Maxima in entropy, combined with interscale saliency

Extended to affine invariance

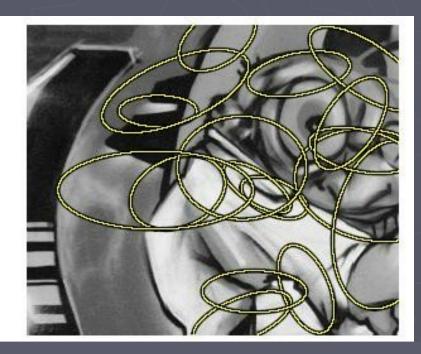






## Salient regions





#### Appreciation

Scale or affine invariant
Detects blob-like structures

- very good for object class recognition
- limited number of regions
- slow to extract













#### Overview of existing detectors

Lowe: DoG

Lindeberg: scale selection

Mikolajczyk & Schmid:

Hessian/Harris-Laplacian/Affine

Tuytelaars & Van Gool: EBR and IBR

Matas: MSER

Kadir & Brady: Salient Regions

Others

#### Other feature detectors

#### Edge-based detectors

Jurie et al., Mikolajczyk et al., ...

#### Combinations of small-scale features

Brown & Lowe

#### Vertical line segments

Goedeme et al.

#### Speeded-Up Robust Features (SURF)

Bay et al.

#### Overview

#### Local Invariant Features: What? Why?

- Introduction
- Overview of existing detectors
- Quantitative and qualitative comparison

#### Local Invariant Features: When? How?

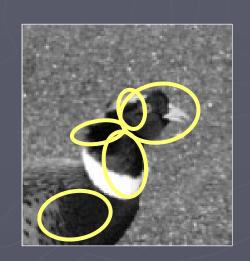
- Feature descriptors
- Applications
- Conclusions

#### Quantitative comparisons

Evaluation of interest points (Schmid & Mohr, ICCV98) Evaluation of descriptors (Mikolajczyk & Schmid, CVPR03) Evaluation of affine invariant features (Mikolajczyk et al., PAMI05)

Evaluation on 3D objects (Moreels & Perona, ICCV05) Evaluation on 3D objects (Fraundorfer & Bischof, ICCV05) Evaluation in the context of object class recognition (Mikolajczyk et al., ICCV05)

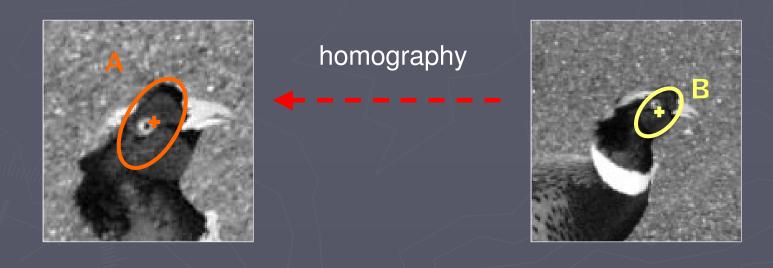


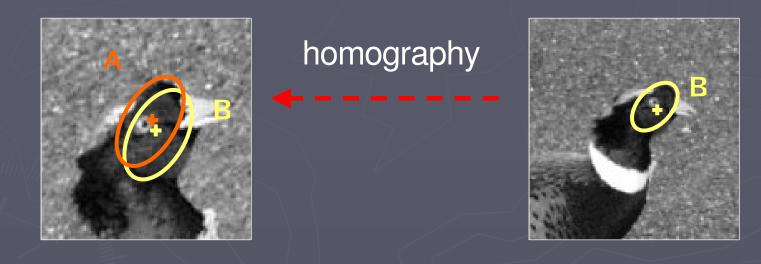


$$repeatability = \frac{\#correspondences}{\#detected} \cdot 100\%$$



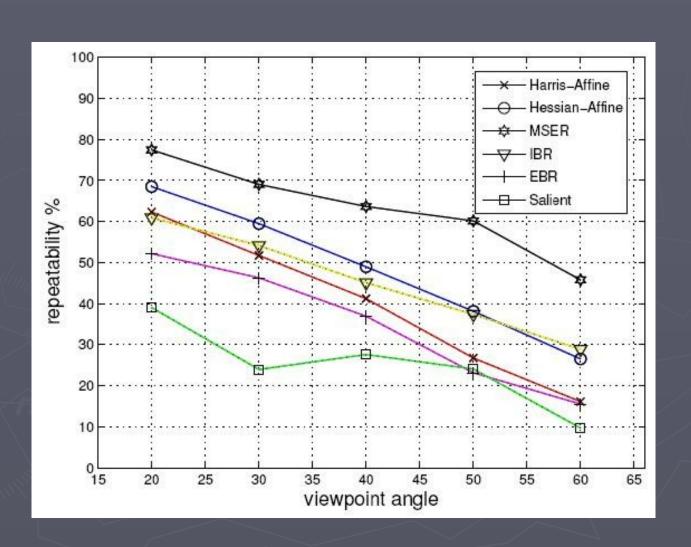
$$repeatability = \frac{\#correspondences}{\#detected} \cdot 100\%$$





•Two points are corresponding if 
$$\frac{A \cap B}{A \cup B} > T$$

# Repeatability



### Quantitative evaluation

Repeatability often lower than 50% Performance often depends on scene type, different detectors are complementary Number of detected features varies greatly Accuracy of detected features varies Performance depends on application Speed

## Qualitative Comparison

Difficult to declare a 'winner'
Different methods are complementary
'Best features' depends on application:

- Level of invariance needed
- Number/density of features wanted
- Typical scene types
- Accuracy of features
- Generalization power of features



### Overview

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## The ideal feature descriptor

Repeatable (invariant/robust)

Distinctive

Compact

**Efficient** 

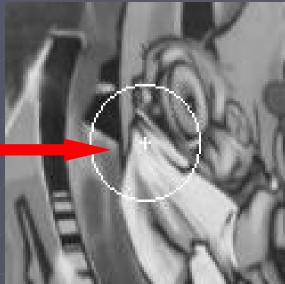
### Normalized crosscorrelation

$$NCC = \frac{\sum_{x=-N}^{N} \sum_{y=-N}^{N} (I_1(x, y) - \bar{I}_1)(I_2(x, y) - \bar{I}_2)}{\sqrt{\sum_{x=-N}^{N} \sum_{y=-N}^{N} (I_1(x, y) - \bar{I}_1)^2 \sum_{x=-N}^{N} \sum_{y=-N}^{N} (I_2(x, y) - \bar{I}_2)^2}}$$

After 'deskewing' the region:

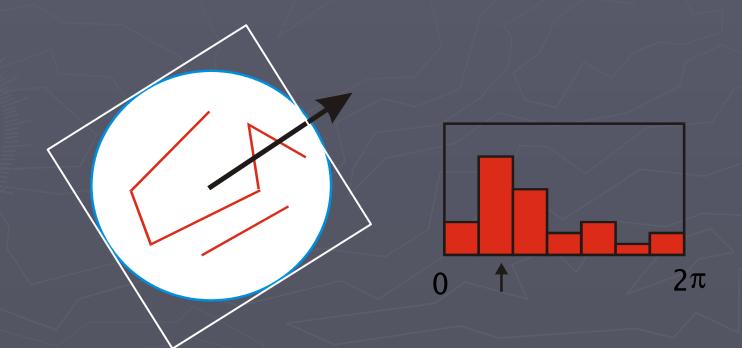




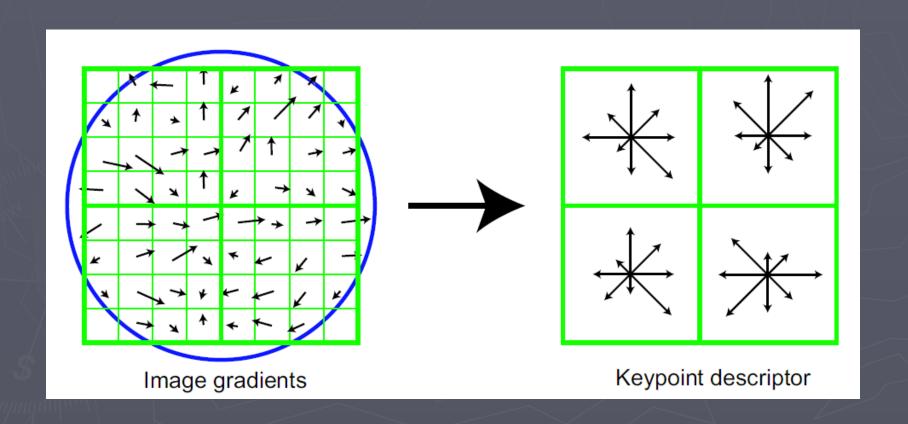


# SIFT descriptor

Orientation assignment
Distribution-based
Focusing on image gradients



# SIFT descriptor



### **Others**

Steerable filters, moment invariants, local jet, complex filters, shape contexts, PCA-SIFT, GLOH, HOG, SURF

### Distance measures

Euclidean distance Mahalanobis distance

$$d_M = \sqrt{(x - x')^T \mathbf{C}^{-1} (x - x')}$$

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### Applications

Wide baseline matching
Recognition of specific objects
Recognition of object classes

### Applications

Wide baseline matching
Recognition of specific objects
Recognition of object classes



Extract features in each image Compute feature descriptors Find correspondences

Matching strategy

Check consistency – filter out mismatches (Refined matching)

#### Which features to use?

- Affine invariant features if large viewpoint changes are expected (>30degrees)
- Accurate features
- Limited number of good matches > large number of medium quality matches
- Take into account typical image content (blobs/corners/prints/...)

MSER, IBR, EBR, ...

### Matching strategy

Match to nearest neighbour Match to nearest neighbour if distance

below a threshold

Match to nearest neighbour if much closer than second-best match (Lowe, 1999)

Possibly match in both directions

### Consistency checks

#### Global constraints

- Epipolar geometry (ransac)
- Homography (ransac)

#### Semi-local constraints

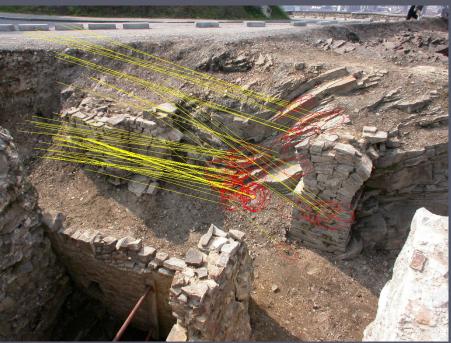
- (Same neighboring regions) (Schmid, 1998)
- Geometric constraints (Tuytelaars & Van Gool, 2000)
- (Topologic constraints) (Ferrari et al., 2004)
- Photometric constraints

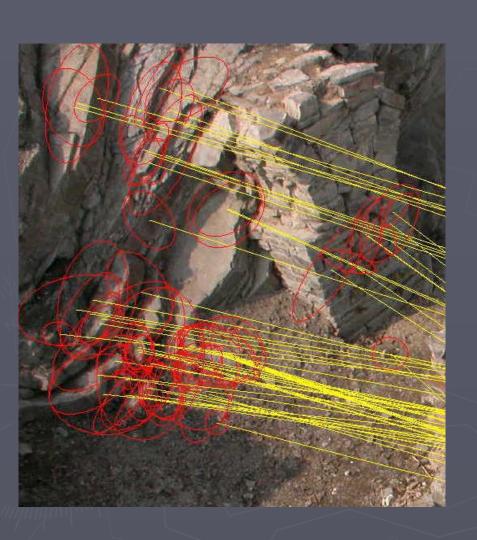
$$\det \begin{bmatrix} a_{23} - b_{23} & b_{13} - a_{13} \\ a_{22} - b_{22} & b_{12} - a_{12} \\ a_{21} - b_{21} & b_{11} - a_{11} \end{bmatrix}$$

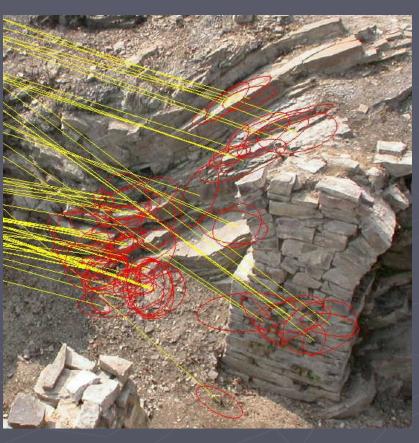
## Refined matching

Search only along epipolar lines Construct additional matches (Ferrari et al., 2004)





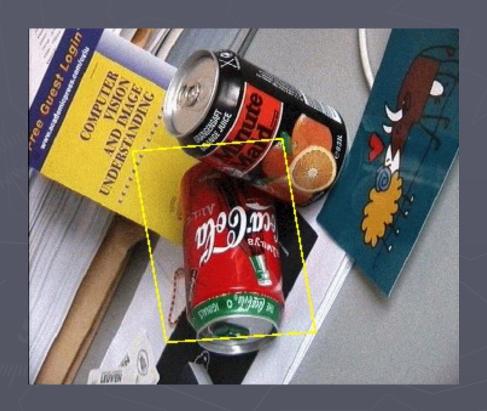




### **Applications**

Wide baseline matching
Recognition of specific objects
Recognition of object classes

Object recognition can be cast as feature matching problem

















#### Training:

Extract features in each model image Compute feature descriptors
Store in database

Efficient search structures

#### Testing:

Extract features
Compute feature descriptors
Match features to database
Count number of votes
Post-processing (Lowe, 1999; Rothganger & Ponce, 2003; Ferrari et al., 2004)

#### Which features to use?

- Affine invariant features if large viewpoint changes are expected (>30 degrees)
- Level of invariance needed depends on number of model images
- Features need to be distinctive: risk for false matches is much larger
- At least a few good matches (if time for post-processing is not an issue)
- Take into account typical image content (blobs/corners/prints/)..

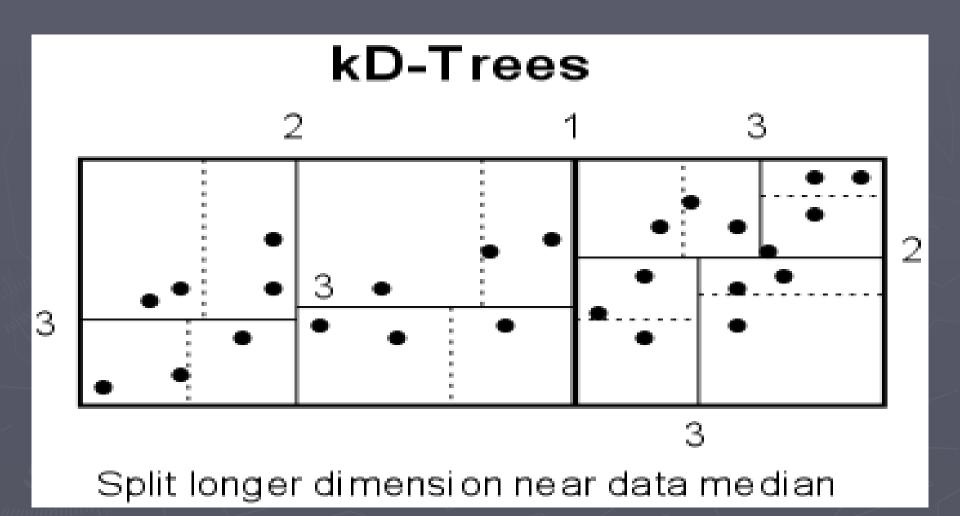
MSER, IBR, EBR, DoG, Harris/Hessian-

## Image Retrieval

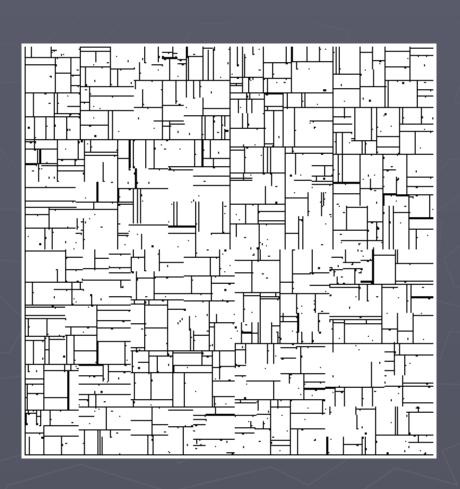
### Efficient matching to a database of images

- Kd-tree
- Best bin first (Lowe, 1999)
- Visual vocabulary & inverted files (Sivic & Zisserman, 2003)

### Kd-tree



## Kd-tree



### Best bin first

Kd-tree less effective in high-dimensional spaces.

Examine only the N closest bins of the kd-tree

#### Postprocessing:

- Hough-like scheme
- 3D model
- Image exploration



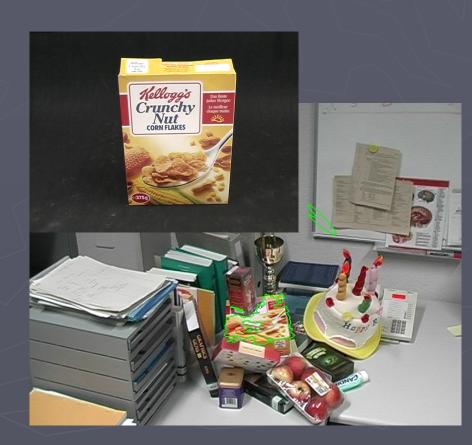
### Postprocessing:

- Hough-like scheme
- 3D model
- Image exploration



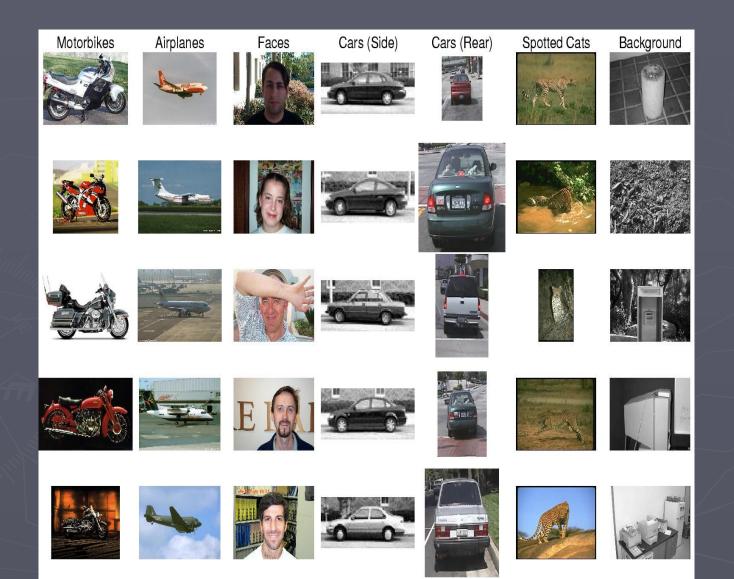
#### Postprocessing:

- Hough-like scheme
- 3D model
- Image exploration



### Applications

Wide baseline matching
Recognition of specific objects
Recognition of object classes



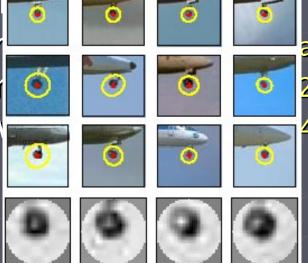
#### **Training**

- Extract local features
- Compute feature descriptors
- Cluster features in object parts / codebooks / visual words

Build model wit

- Constellation m
- Implicit shape
- Bag-of-visual-w

Train classifier





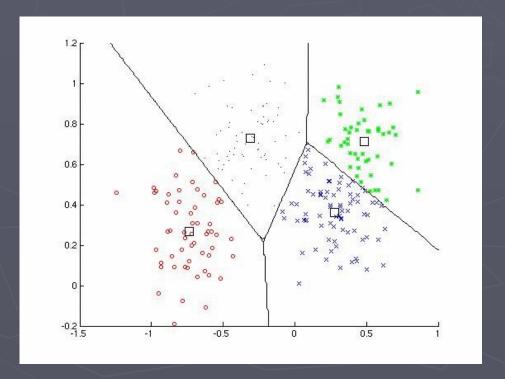
#### Which features to use?

- Scale invariant features
- Robust features
- Large number of features (depends on model used)
- Accuracy not important

Salient Regions, Harris/Hessian-Laplace

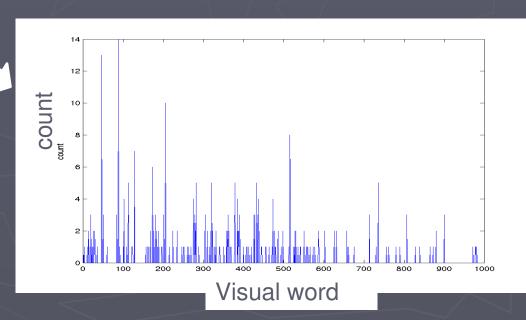
### Clustering features into 'visual words'

- K-means
- Jurie & Triggs, ICCV05



Bag-of-visual-words image representation:





### Other applications

Image mosaicking Mobile robot navigation Scene classification Texture classification Video data mining Object discovery 3D reconstruction

4 4 7

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### Do's and Don'ts

#### DO

- Think about the right level of invariance
- Rely on statistics

#### DO NOT

- Expect wonders
- Rely on a single local feature
- Evaluate methods based on a single image

### Questions?

Tinne.Tuytelaars@esat.kuleuven.be http://homes.esat.kuleuven.be/~tuytelaa/ECCV06tutorial.html

http://www.robots.ox.ac.uk/~vgg/research/affine