

Machine Learning for Ecological Science and Environmental Policy

Tom Dietterich, Rebecca Hutchinson, Dan Sheldon Oregon State University

JCC 2012 Tutorial

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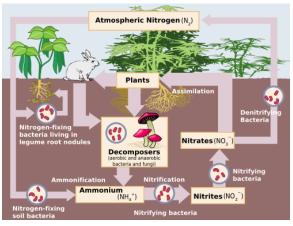
For additional information, please visit http://dsp.acm.org/

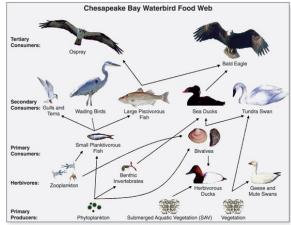
Introduction

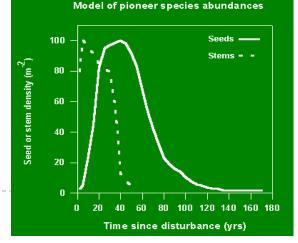
Ecological Science

- Processes governing the function and structure of ecosystems
 - Flows of energy and nutrients
 - Sunlight, water, carbon, nitrogen, phosphorus
 - Species distribution and interaction
 - Reproduction, Dispersal, Migration, Invasion
 - Competition, Food Webs, Mutualism
 - Non-equilibrium systems: Continual disturbance and system resilience
 - $\hfill\square$ Many species depend on disturbances

Wikipedia; http://www.plantbio.uga.edu/~chris/wind.html



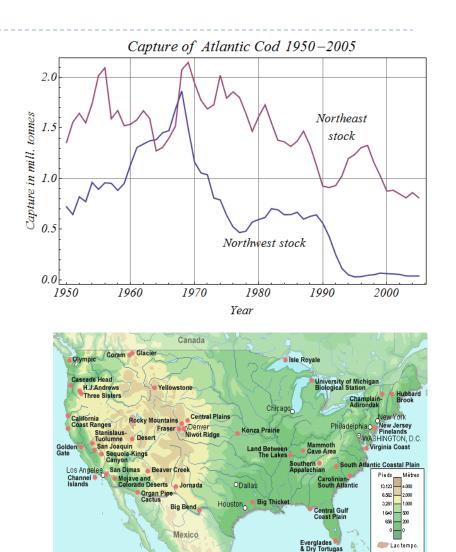


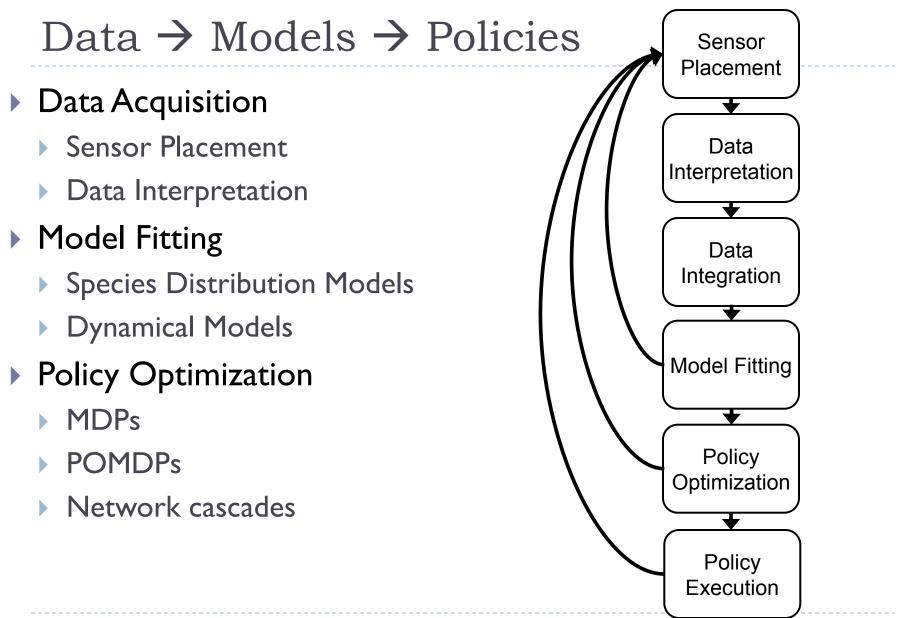


Introduction

Environmental Policy

- Natural resource management
 - Fisheries
 - Forestry
 - Water resources (rivers, aquifers, estuaries)
- Conservation biology
 - Reserves and conservation easements
 - Endangered species
 - Endangered ecosystems
 - Invasive species management





Unique Aspects

- Heterogeneity
 - Physical quantities (nutrients, temperature, wind)
 - Organisms and species (viruses, bacteria, fungi, plants, animals)
 - Spatial Scale (inside a single organism, watershed, continent, planet)

Hidden dynamics

- Virtually all interactions are not directly observed
- Observations are noisy and incomplete
- Most movement (dispersal, migration) is not directly observed
- Non-stationary dynamics: climate change, land-use change, evolution
- Optimization wrt learned dynamic models
 - Large spatio-temporal MDPs
 - Essential POMDPs
 - Need for robust solutions
 - poorly-modeled dynamics
 - politics

Goals for the Tutorial

- Review the primary data sources, model types, and machine learning and optimization problems that arise in ecological science and environmental policy
- Provide examples of current optimization and machine learning work in each of these areas
- Point out open problems and opportunities for additional research
- Provide pointers to data sets and relevant literature

Outline

Data Acquisition

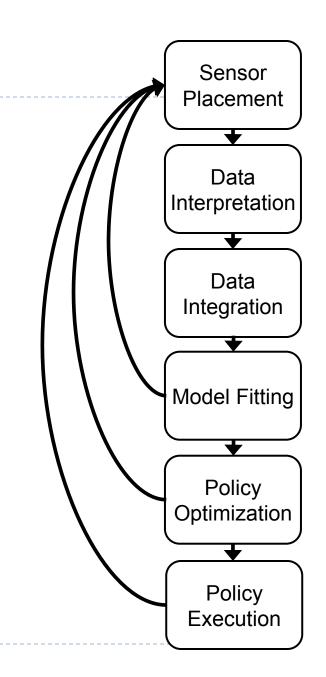
- Sensors: Physical sensors, human observers, repurposing data from other sources
- Data interpretation: Extracting signals from data

Ecological Models

- Species Distribution Models
- Dynamical Models: Dispersal, Migration, Invasion, Climate Change

Policy Optimization

- Conservation: Reserve design, Network design
- Invasive species: Eradication, restoration, monitoring
- Fisheries: Managing harvest levels



Part 1: Data Acquisition

Data Sources

- Instruments placed in the environment:
 - Weather stations: temperature, wind direction, wind speed, solar radiation, relative humidity, snow depth, precipitation
 - Stream gauging stations: water flow rate, temperature, height
 - Isotope and dye studies: Carbon, Nitrogen, Phosphorous
 - RFID tags: Fish
 - Radio collars: mammals and birds
 - Acoustic monitoring
 - □ Birds, insects, bats, whales



wildlifeacoustics.com



biomark.com



SensorScope

atstrack.com

Data Acquisition: Human Observation

Trapping and identification

- Insect traps: emergence, malaise, UV light
- Electro-fishing
- Kick nets

Volunteers

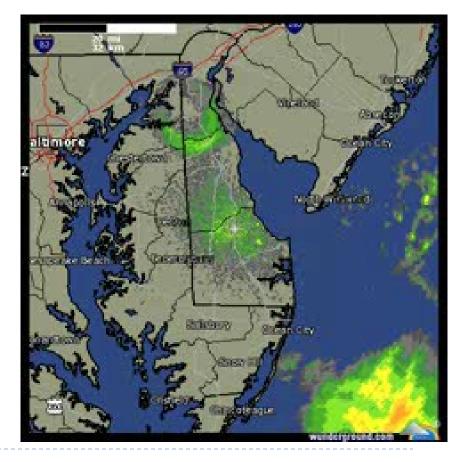
- Bird sightings
- Whale observations





Data Acquisition: Repurposing Data Gathered for Other Purposes

- Repurposing information gathered for other purposes
 - Fish catch data
 - Doppler weather radar

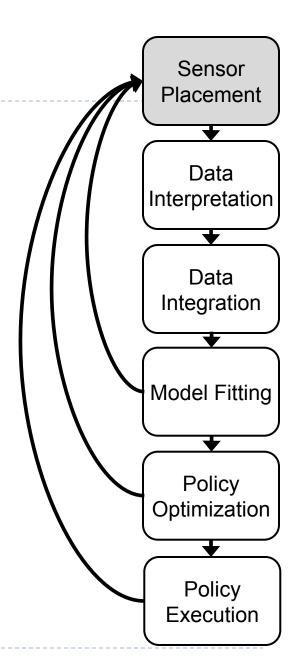


Data Acquisition: Remote Sensing

- Satellite-borne Sensors
 - Landsat 7
 - I 5m resolution; whole planet coverage every I6 days
 - MODIS
 - > 250m-1km resolution; whole planet coverage every 1-2 days

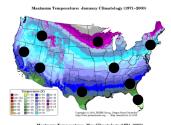
Sensor Placement

- Where should we place sensors to gain the best information for...
 - improving our models
 - improving our policies
 - guiding policy execution
- Related questions in ML
 - Active Learning
 - Exploration in Reinforcement Learning
 - Optimal POMDP policies



Basic Case: Spatial Sensor Placement for Real-Valued Function f [Krause, et al., 2008]

- Examples: Temperature, Rainfall, Nutrient Density, Pollutant Density
 - Goal: At each time t, we will observe the sensor readings (at the chosen locations) and estimate the complete spatial map of the target function f

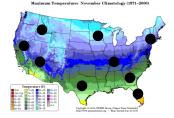




• Given:

- Initial model or initial set of observations
- Budget: # of sensors k
- Find:
 - Locations at which to put the sensors in order to best estimate the function at future times

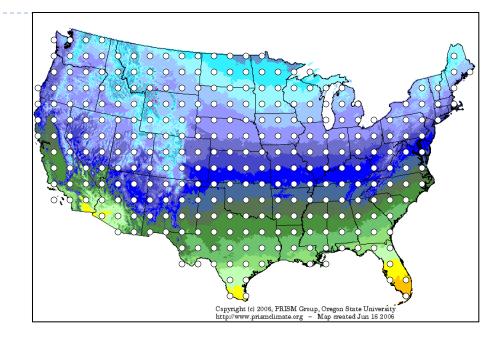




Approach

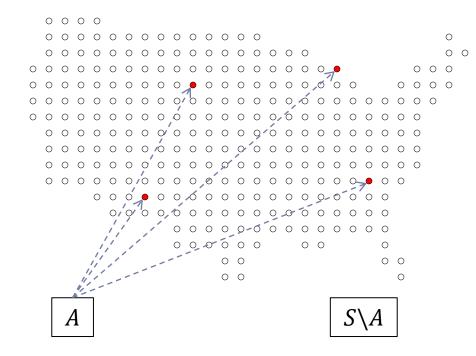
Discretize space:

- Let S be a set of points (s_1, \dots, s_N)
 - where sensors can be placed
 - where we will make predictions
- Assume joint Gaussian
 - $(f(s_1), \dots, f(s_N)) \sim \operatorname{Norm}(\boldsymbol{\mu}, \boldsymbol{\Sigma})$
 - where μ has dimension N and
 - Σ has dimension $N \times N$
- Use the initial observations to estimate Σ
- Choose an objective function J(A) for evaluating the quality of a set of sensor locations A
- Formulate an optimization problem to choose a set $A \subset S$ of size k that optimizes J(A).
- Place sensors at points A



What Criterion to Optimize?

- Estimate the amount of information that the chosen points tell us about the notchosen points
- $I(X_A; X_{S \setminus A}) =$ "mutual information"
- $J(A) = I(X_A; X_{S \setminus A})$ will be our "objective function"
 - Choose A to maximize J(A)



What Criterion to Optimize?

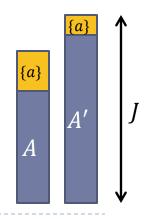
• Rationale:

- empirical: gives good results
- computational: easy to compute for Gaussian distributions
- analytical: objective is sub-modular
 - Greedy Algorithm with provable bounds

Submodularity:

▶ J is submodular if for all $A \subseteq A'$ and all $a \in S \setminus A'$, $J(A \cup \{a\}) - J(A) \ge J(A' \cup \{a\}) - J(A')$

"diminishing returns of adding a"



Greedy Algorithm

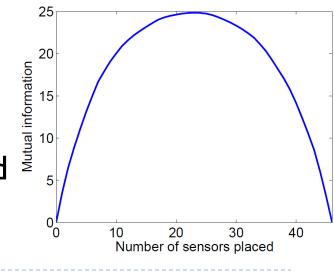
- Input:
 - Sites: S
 - Number of sensors: k
 - \blacktriangleright Estimated covariance matrix of joint Gaussian: Σ
- Output: sensor locations $A \subset S$, |A| = k
- begin
 - $\blacktriangleright A \leftarrow \emptyset$
 - for j = 1 to k do
 a^{*} ← argmax J(A ∪ {a}) a∈S\A
 A ← A ∪ {a^{*}}
- end

Analytical Bound

- Monotonicity assumption: $\forall a \in S \setminus A \quad J(A \cup \{a\}) > J(A) + \epsilon$
- Let be the greedy solution and A* be the optimal solution

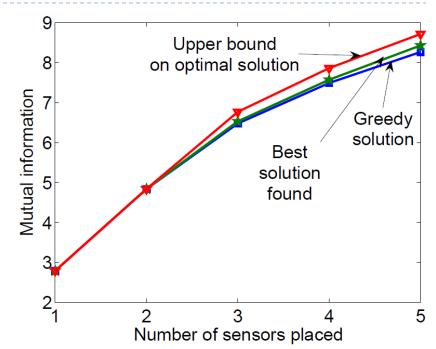
$$J(\hat{A}) \ge \left(1 - \frac{1}{e}\right) J(A^*) - k\epsilon$$
$$\left(1 - \frac{1}{e}\right) \approx 0.632$$

Assumption will hold if S is discretized sufficiently finely



Experimental Accuracy

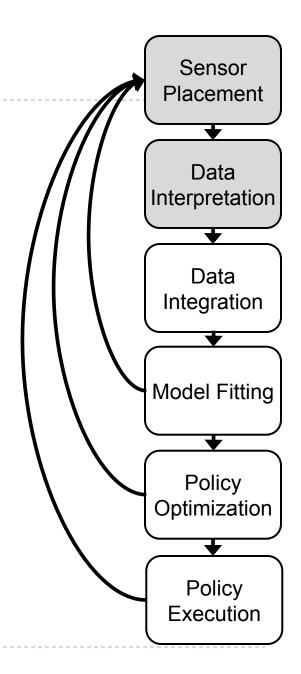
- Theoretical bound is 63.2% of optimal
- Greedy algorithm is closer to 95% of optimal in this case



Intel Berkeley Temperature Sensors

Data Interpretation

- Extracting high level interpretation from low-level sensor data
 - Example I: Arthropod Population Counting
 - Example 2: Finding Swallow Roosts in Doppler Weather Radar



Arthropod Population Surveys

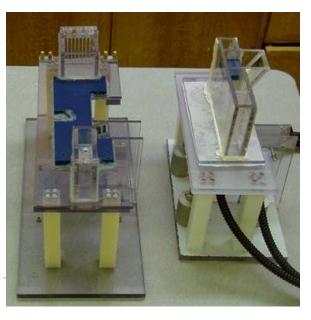
- Arthropods are a powerful data source
 - Found in virtually all environments
 - streams, lakes, oceans, soils, birds, mammals
 - Provide valuable information on ecosystem function
 - Standard tool for evaluating stream health in EPA biomonitoring and stream restoration efforts
- Problem: Identification is timeconsuming and requires hard-to-find expertise
- Solution: Combine robotics, computer vision, and machine learning to automate classification and population counting



OSU BugID Project

- Human technician gathers field sample
- Semi-automated image capture
- Automated classification

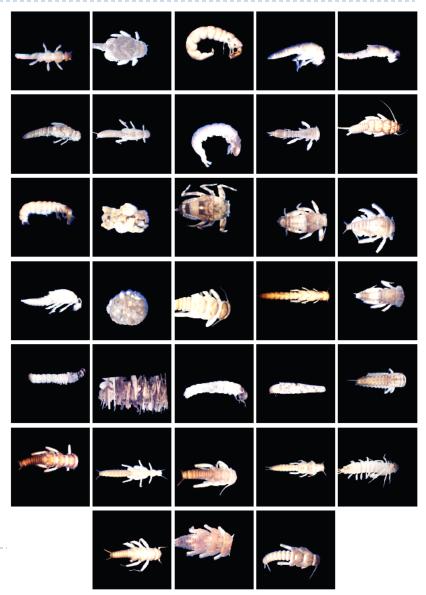




Computer Vision Challenge: Fine-Grained Classification

Challenges:

- Many classes
- Subtle differences between classes
- Wide variety of poses
- Substantial size and appearance variation within class



Hypotheses

Fine-grained classification requires

- High-resolution images
- Non-uniform extraction of information from the image

Existing object recognition methods

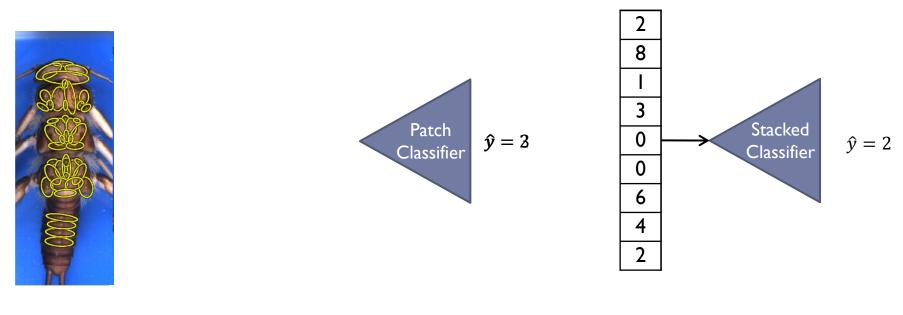
- Break image into set of patches
- Extract a fixed number of bits from each patch
 - e.g., via vector quantization, filter banks, PCA, etc.
- Classify image using extracted information

A "Variable Resolution" Method for Object Recognition

Stacked Patch Classifiers

[Martinez, et al, 2009]

- Learn a classifier that <u>tries</u> to classify the whole image using detailed information from a single patch
- Combine the single-patch classifications into a classification for the whole image



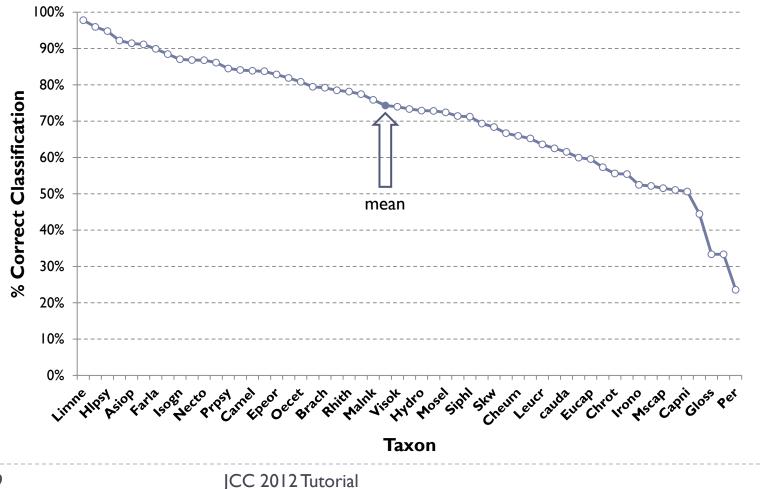
Results on STONEFLY9 Dataset

Configuration	Error Rate
Fixed resolution method	16.1%
Stacked Patch Classifier	5.6%

Variable resolution method is much more accurate

EPT54: 54 Species of Freshwater Macroinvertebrates

Stacked Patch Classifier: 74.3% Correct



Open Problems

- Rejection:
 - Maximize recall subject to high precision
- Detect and reject novel (i.e., unknown to the classifier) species
- Scale to thousands of species
- Hierarchical loss functions
 - Order, Family, Genus, Species
 - Classify as finely as possible while bounding error rate



Tracking Tree Swallow Roosts Using NEXRAD Radar



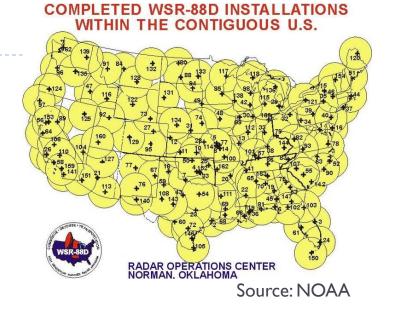


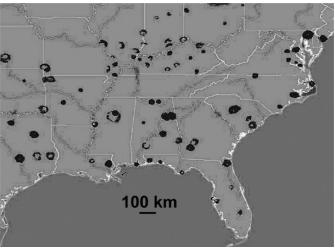


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The Dream

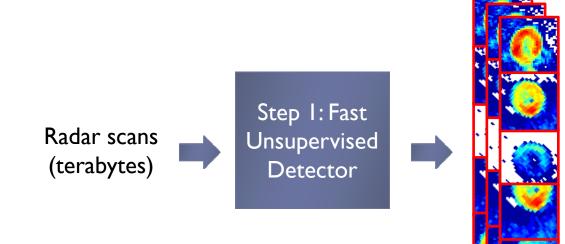
- Automatic detection of roosts at continent-scale on daily basis
 - Data gathering and repurposing
- Unprecedented view of species distribution
 - Spatial coverage
 - Temporal resolution
- Analyze results to learn about
 - Roost biology
 - Migration patterns
 - Climate change
 - Data archived since 1991





[Winkler, 2006]

Machine Learning Pipeline (1)

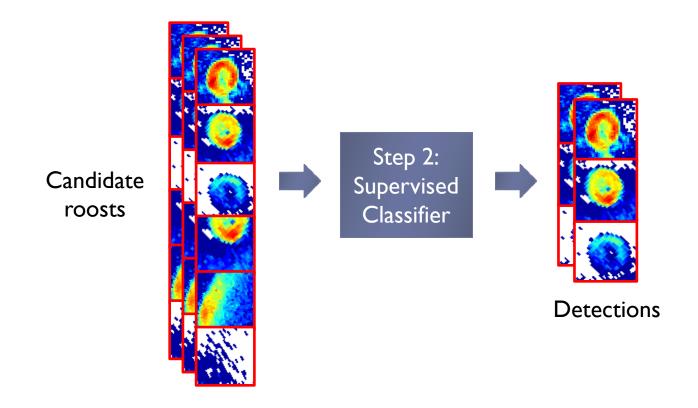


Primary goal: data reduction

- High recall
- Many false positives

Candidate roosts

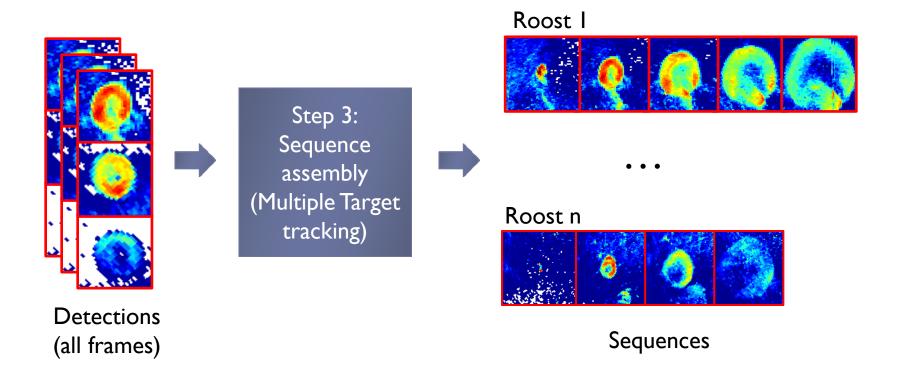
Machine Learning Pipeline (2)



Shape features

Biology features (velocity, habitat, weather, etc.)

Machine Learning Pipeline (3)

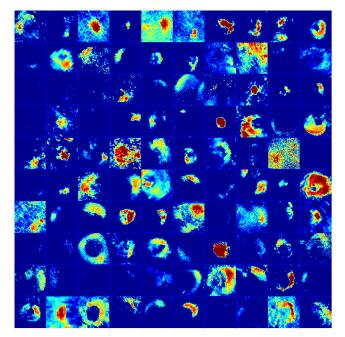


Motivation:

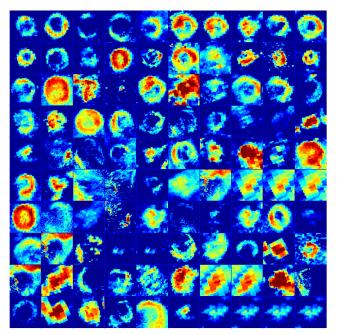
- Improve detection by using temporal context
- Extract high-level information such as duration, maximum size, etc.

Progress: Machine Learning

- Steps I and 2
 - Primarily shape features to-date
 - High precision for roosts with "perfect appearance"
 - \blacktriangleright Variability in appearance is challenging \rightarrow low recall



100 positive examples

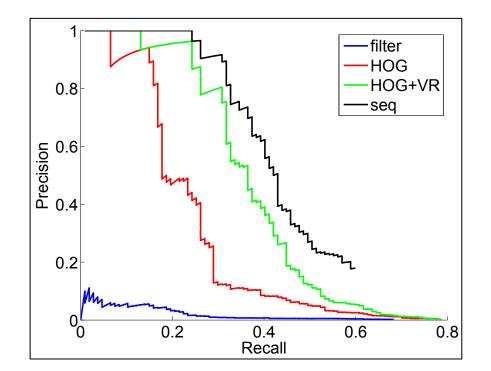


Top 100 predicted roosts (shape features + SVM)

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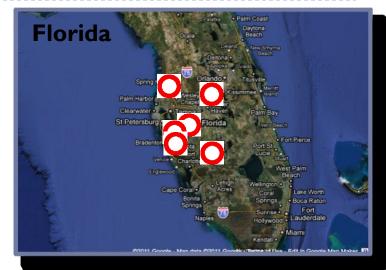
Initial Results

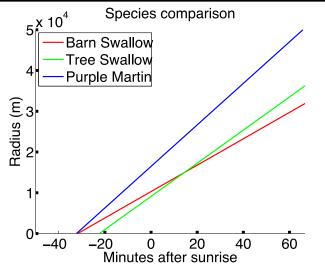
- <u>filter</u>: simple "matched filter" based on average appearance
- HOG and HOG+VR: learned classifier for single images
- <u>seq</u>: combining a sequence of images



Progress: Ecology

- Locating roosts
 - Identifying roosts in radar images
 - Labeling efforts
 - Estimate ground location within a few km
 - Previously difficult task
 - I5+ roosts located in 2010-2011
 - 🗆 Oregon, Florida, Louisiana
- Analysis of labeled data
 - Understand regional patterns
 - Roost growth dynamics
 - Very predictable
 - Potential species ID from radar!





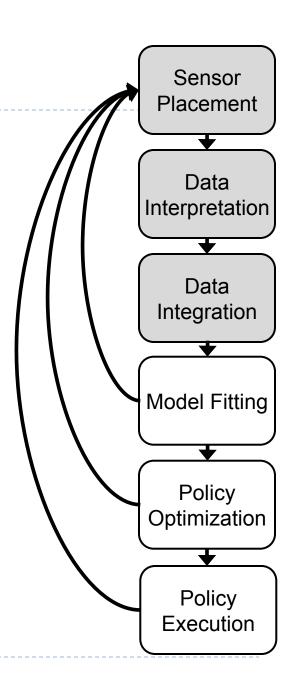
Summary

Ongoing project

- A lot of work remains to reach "the dream"
- Significant opportunity for ML and ecology to develop in parallel

Data Integration

- Integrating heterogeneous data sources to predict when migrating birds will arrive:
 - Landsat (30m; monthly)
 - land cover type
 - MODIS (500m; daily/weekly)
 - land cover type
 - "greening" index
 - Census (every 10 years)
 - human population density
 - housing density and occupation
 - Interpolated weather data (15 mins)
 - rain, snow, solar radiation, wind speed & direction, humidity
 - Integrated weather data (daily)
 - warming degree days
 - Digital elevation model (rarely changes)
 - elevation, slope, aspect



Questions on Part 1?

Part 2: Ecological Models

Outline

Data Acquisition

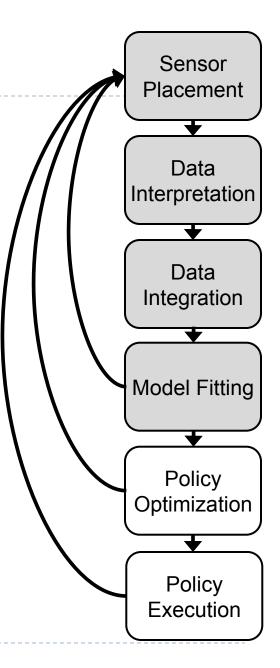
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- Data interpretation: Extracting signals from data

Ecological Models

- Species Distribution Models
- Dynamical Models: Dispersal, Migration, Invasion, Climate Change

Policy Optimization

- Conservation: Reserve design, Network design
- Invasive species: Eradication, restoration, monitoring
- Fisheries: Managing harvest levels



Ecological Models

Species Distribution Models

- > Static descriptions of the geographic distribution of a species.
- Address the fundamental ecological question of why species are found where they are.

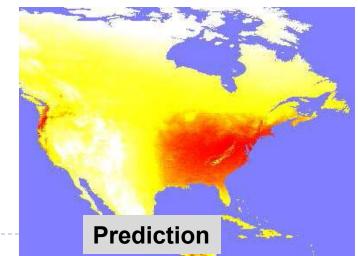
Dynamical Models

• Account for dynamic ecological processes like dispersal, migration, population growth, etc.

Example

Yellow-throated vireo





Images are from Figure 1 in Phillips, et al., 2004.

Species Distribution Models (SDM)

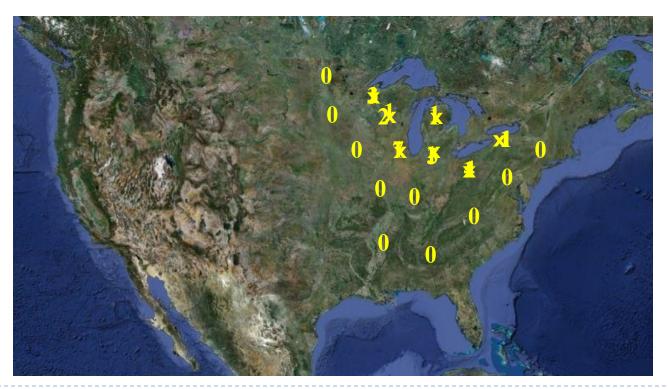
Prediction Task:

- Given a feature vector x describing a site, predict whether the species occurs there $y \in \{0,1\}$
- Standard Supervised Learning
 - Given training examples $\{(x_1, y_1), \dots, (x_N, y_N)\}$
 - Learn a predictive model f such that y = f(x)
- Purposes:
 - Mapping the current distribution of a species
 - Understanding habitat requirements for the species
 - Predicting distribution in places where there is no data available

SDM: Data

• Types of y

- Presence-only
- Presence/absence
- Abundance









eBird Data

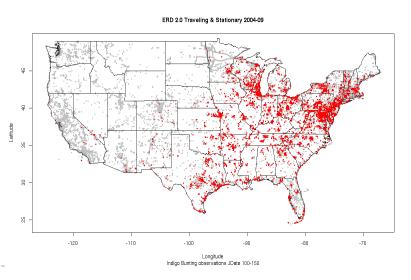
- Bird watchers record their observations in a database through eBird.org.
 - "Citizen Science"
- Dataset available for analysis. (see references)

Features

- > 38,599 observers; 336,088 locations
- 2.4M checklists; 41.7M observations
- All bird species (~3,000)
- Year-round
- World wide

Challenges

- Variable quality observations
- No systematic sampling plan



SDM: Methods

Envelope Models

Bioclim

Statistical and Machine Learning Models

- Maxent
- Generalized Linear Models
- Generalized Additive Models
- Multivariate Adaptive Regression Splines
- Hierarchical Bayesian modeling
- Boosted regression trees
- Random forests
- Genetic algorithms

...and more!

ML is already having an impact in SDM

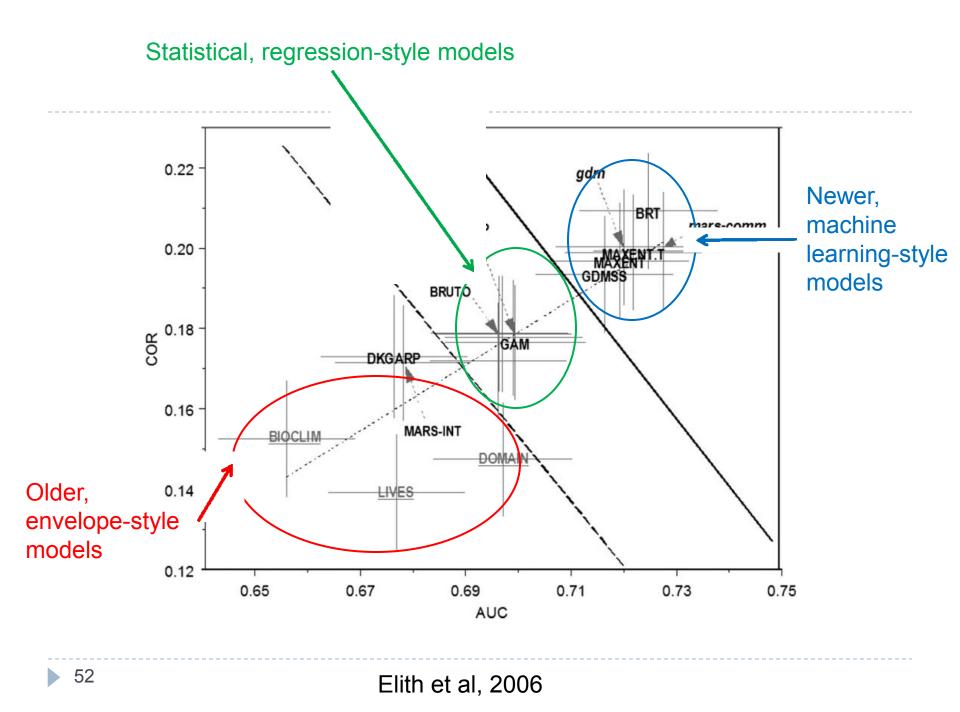
ECOGRAPHY 29: 129-151, 2006

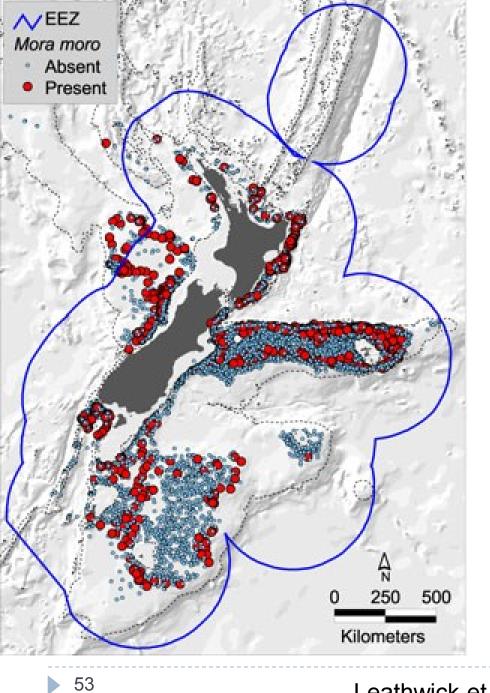
- I6 methods
- > 226 species
- 6 regions

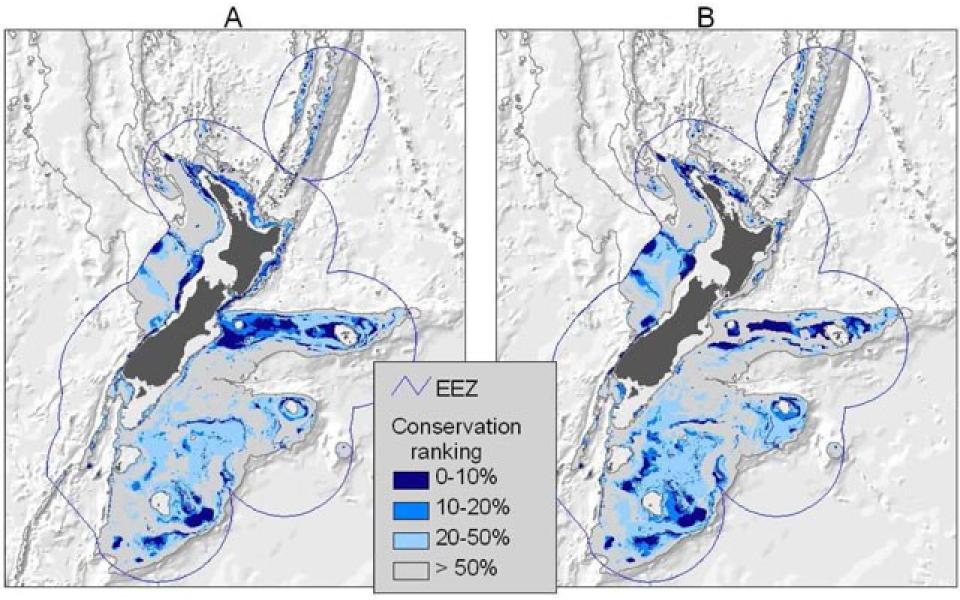
Novel methods improve prediction of species' distributions from occurrence data

Jane Elith^{*}, Catherine H. Graham^{*}, Robert P. Anderson, Miroslav Dudík, Simon Ferrier, Antoine Guisan, Robert J. Hijmans, Falk Huettmann, John R. Leathwick, Anthony Lehmann, Jin Li, Lucia G. Lohmann, Bette A. Loiselle, Glenn Manion, Craig Moritz, Miguel Nakamura, Yoshinori Nakazawa, Jacob McC. Overton, A. Townsend Peterson, Steven J. Phillips, Karen Richardson, Ricardo Scachetti-Pereira, Robert E. Schapire, Jorge Soberón, Stephen Williams, Mary S. Wisz and Niklaus E. Zimmermann

 General result: new(er) statistical and/or machine learning methods outperformed older envelope/distance style models.







Disregarding costs to fishing industry

Full consideration of costs to fishing industry

Leathwick et al, 2008

Three SDM Challenges

- Presence-only data
- Extrapolation beyond the training data
- Imperfect detection of the species on surveys
 - Often lack prior knowledge of the system for model building
 - Observers have variable expertise/biases

Challenge #1: Presence-only data

- Problem: some data sources only contain records of presence (e.g., museum collections)
- Solution: Maximum entropy modeling (Maxent)

Positive-Only Learning Problem

• Given:

- Training examples x_1, \dots, x_N where the species is present
- These are assumed to be drawn from an unknown probability distribution: $\pi(x) = P(x|y = 1)$
- A set of feature functions φ₁, ..., φ_j such that φ_j(x) computes the value of the *j*th feature of x. Let Φ(x) = (φ₁(x), ..., φ_j(x)).

Find:

• A good approximation $\hat{\pi}$ to π

Method: The Maximum Entropy Principle

- Maximum entropy principle: Among all distributions consistent with the data, prefer the distribution of maximum entropy
- Find the maximum entropy distribution subject to expectation constraints:

 $\hat{\pi} = \underset{q}{\operatorname{argmax}} H(q) \text{ subject to } \operatorname{E}_{q}[\phi_{j}(x)] = \frac{1}{N} \sum_{i} \phi_{j}(x_{i}) \forall j$

- Intuition:
 - The average value of temperature according to the model should match the average value of temperature in the data
 - The average value of elevation according to the model should match the average value of elevation in the data
 - While making as few additional assumptions as possible

Solving the Maxent Optimization

Step I: Relax the constraints:

$$\hat{\pi} = \underset{q}{\operatorname{argmax}} H(q) \text{ subject to}$$
$$E_{q}[\phi_{j}(x)] - \frac{1}{N} \sum_{i} \phi_{j}(x_{i}) \leq \beta_{j} \forall j$$

- Step 2: Assume a parametric form for $\hat{\pi}$: $\hat{\pi}(x) = \frac{1}{Z(w)} \exp[w \cdot \Phi(x)]$
- Step 3: Apply duality methods to show this is equivalent to an L₁-regularized linear optimization

$$\widehat{\boldsymbol{w}} = \underset{\boldsymbol{w}}{\operatorname{argmax}} \sum_{i} \boldsymbol{w} \cdot \Phi(x_i) - \sum_{j} \beta_j |w_j|$$

Obtaining an SDM

- Problem: We have a model $\hat{\pi}$ of P(x|y=1) but we want a model of P(y=1|x).
- Solution: Apply Bayes' Rule

$$P(y = 1|x) = \frac{P(x|y = 1)P(y = 1)}{P(x)}$$

- P(y = 1) is the "abundance". It is a constant that is *not* identifiable from presence-only data.
- P(x) is the "background distribution" of the study area (often assumed uniform).
- Therefore,

$$P(y=1|x) \propto \hat{\pi}(x)$$

Creating a Usable Tool

Free software package for SDM

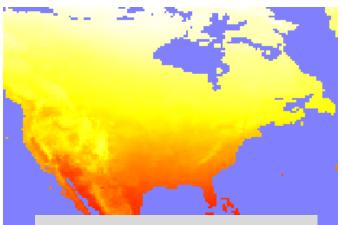
- http://www.cs.princeton.edu/~schapire/maxent/
- Has had a huge impact in the ecology literature
- Provides a rich set of feature types ϕ^t
 - linear
 - quadratic
 - thresholds
 - ramps
 - pairwise products of these
- Provides default settings for the β s
 - The method requires tuning a separate β_j for each feature, which is hard to do via cross-validation.
 - Defaults are based on tuning for 6 datasets from Elith, et al. [2006]

Example

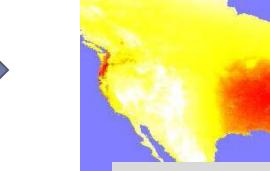
Yellow-throated vireo







Avg. ann. temperature



Maxent prediction

Images are from Figure 1 in Phillips, et al., 2004.

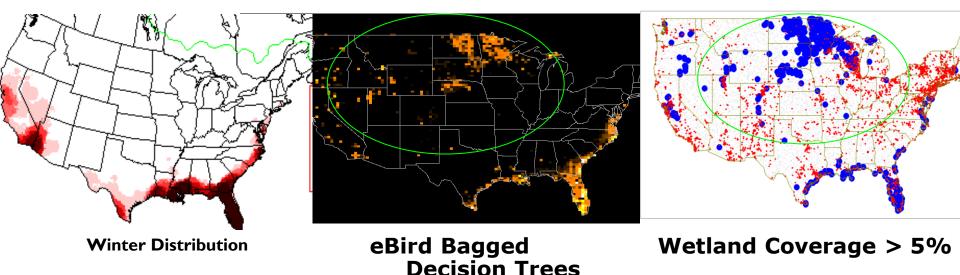
Challenge #2: Extrapolation

- Problem: at continental scale, learned models may extrapolate too far and make mistakes
- Fink, et al., 2010: "Spatiotemporal exploratory models for broad-scale survey data"



Tree Swallow Winter Distribution Analysis

(Tachycineta bicolor)

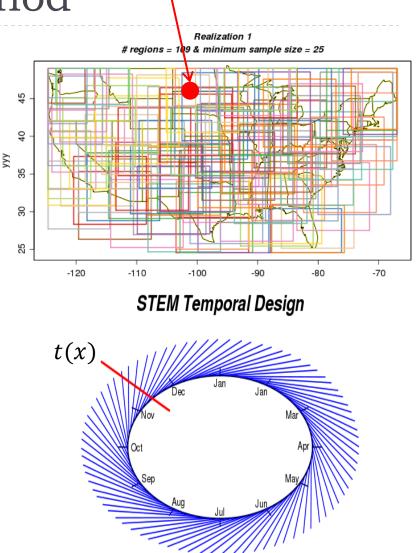


- "Wetland" should really be "Wetland at time t"
- Lack of data for northern US in winter time (people don't go bird watching in the snow)

STEM: Ensemble Method

Idea:

- Slice space and time into hyperrectangles:
 - latitude x longitude x time called "stixels"
- Train a classifier on the data inside each stixel
- To predict at a new point x at a given place loc(x) and time t(x), vote the predictions of all classifiers whose stixel contains (loc(x), t(x))



loc(x)



Because each classifier is only asked to predict within its stixel, it will never extrapolate beyond the stixel

STEM SDM: Solitary Sandpiper







slide courtesy of Daniel Fink

STEM SDM: Indigo Bunting

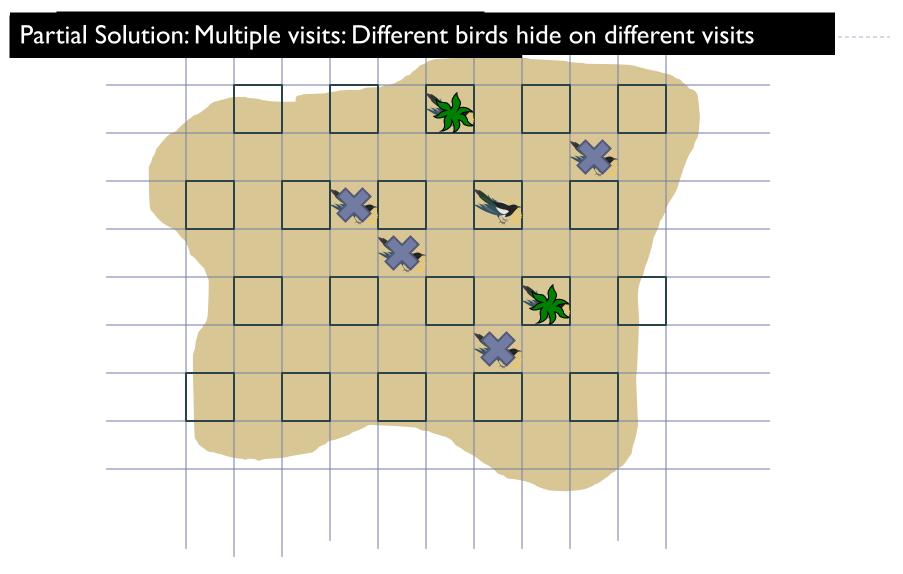


slide courtesy of Daniel Fink

Challenge #3: Imperfect Detection

- Problem: many species are hard to detect even when present, so their data contain false negatives
- Solution:
 - visit each site several times
 - use a hierarchical model to describe the data collection process explicitly and correct for false zeros

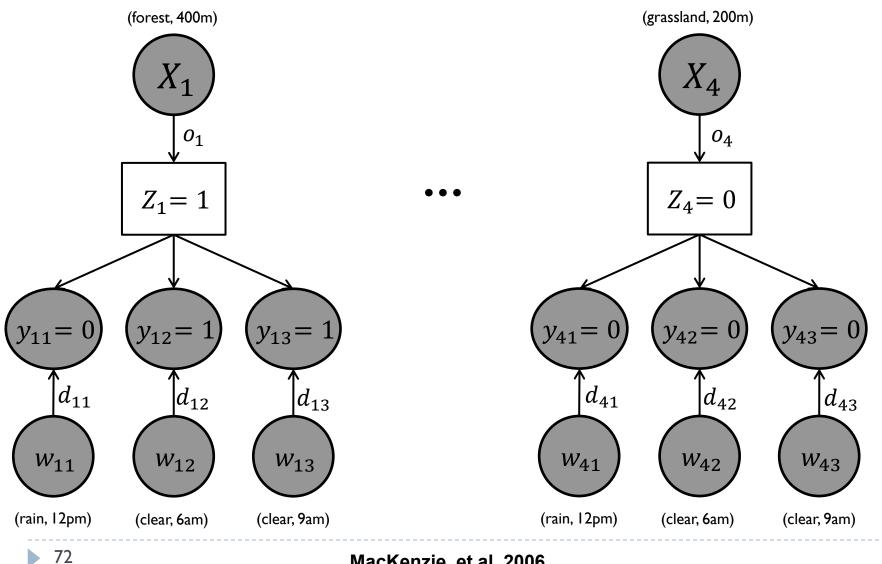
Wildlife Surveys with Imperfect Detection



Multiple Visit Data

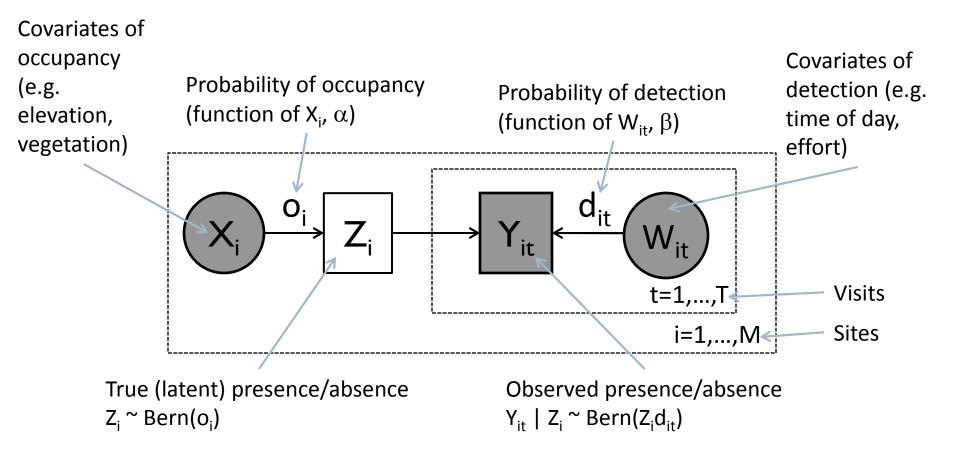
		Detection History		
Site	True occupancy (latent)	Visit I (rainy day, I2pm)	Visit 2 (clear day, 6am)	Visit 3 (clear day, 9am)
A (forest, elev=400m)	Ι	0	I	I
B (forest, elev=500m)	Ι	0	I	0
C (forest, elev=300m)	Ι	0	0	0
D (grassland, elev=200m)	0	0	0	0

Probabilistic Model with Latent Variable Z



MacKenzie, et al, 2006

Occupancy Model



Typical Parameterization

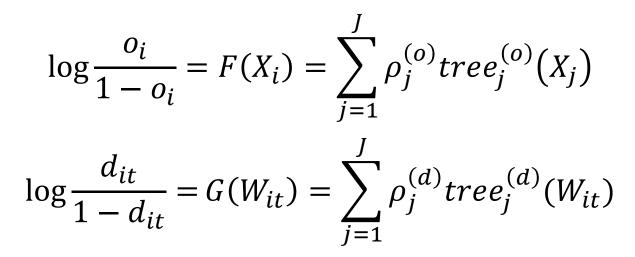
$$\log \frac{o_i}{1 - o_i} = F(X_i) = \alpha \cdot X_i$$
$$\log \frac{d_{it}}{1 - d_{it}} = G(W_{it}) = \beta \cdot W_{it}$$

- Model selection:
 - construct models including different sets of occupancy and detection covariates
 - evaluate fit with AIC
 - hypothesis tests/confidence intervals

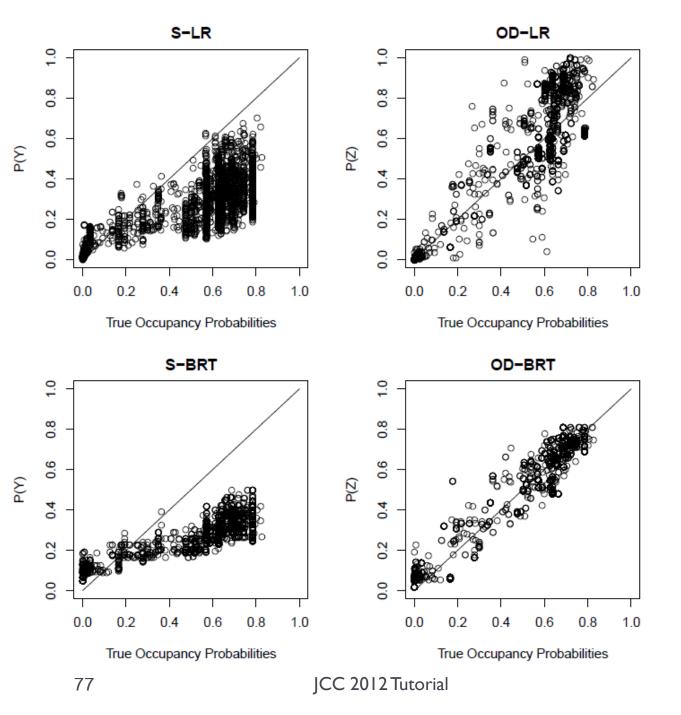
Imperfect Detection + Lack of Prior Knowledge

- Problem: occupancy models require parametric assumptions too rigid for exploratory modeling of big data sets
- Solution: incorporate flexible models into the model while maintaining hierarchical structure to account for imperfect detection

Integrating regression trees



- Fit with functional gradient descent [Friedman, 2001]
 - On each iteration:
 - compute pseudo-targets (gradient of loss at each data point)
 - grow another tree to predict pseudo-targets
 - compute a weight for the tree and add to ensemble
 - Maximizes log-likelihood of occupancy model



Synthetic Species built from eBird covariates (with non-linearities)

S = supervised, with no latent structure (left column)

OD = occupancy model structure (right column)

LR = linear (top row)

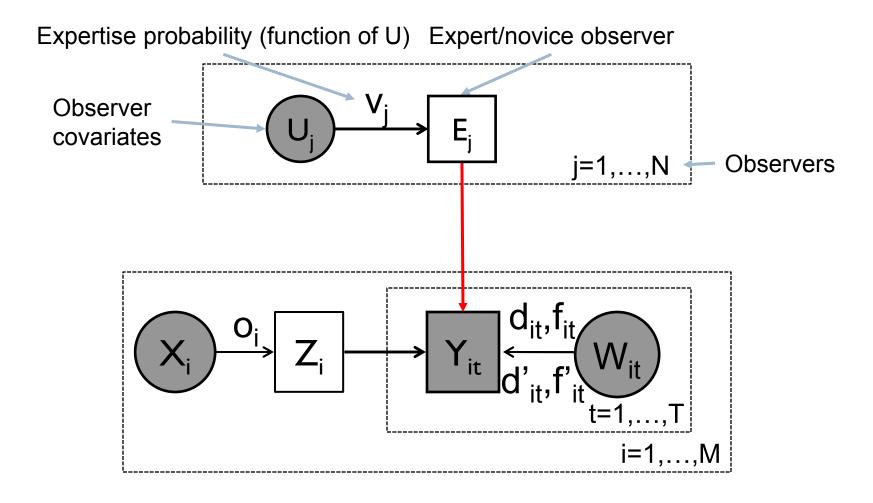
BRT = tree-based (bottom row)

Hutchinson, et al, 2011

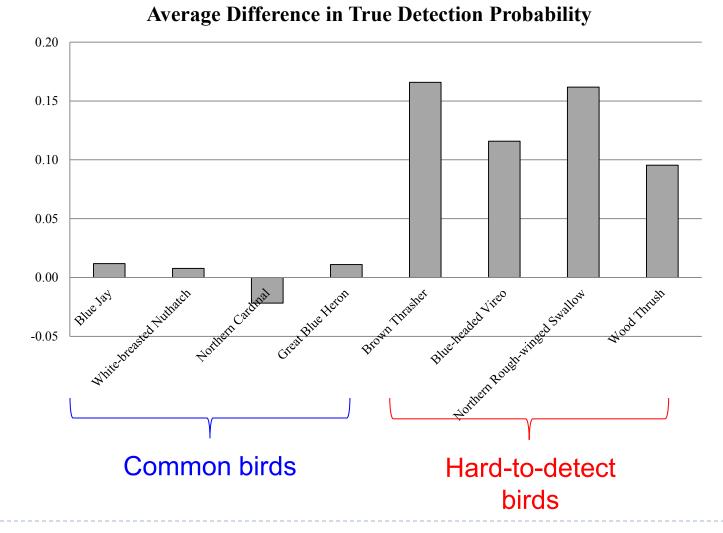
Imperfect Detection + Variable Expertise

- Problem: expert and novice observers contributing observations to citizen science data generate different mistakes/biases
- Solution: extend occupancy models so that observer expertise affects the detection model

Extending Occupancy Models



Expert vs Novice Differences

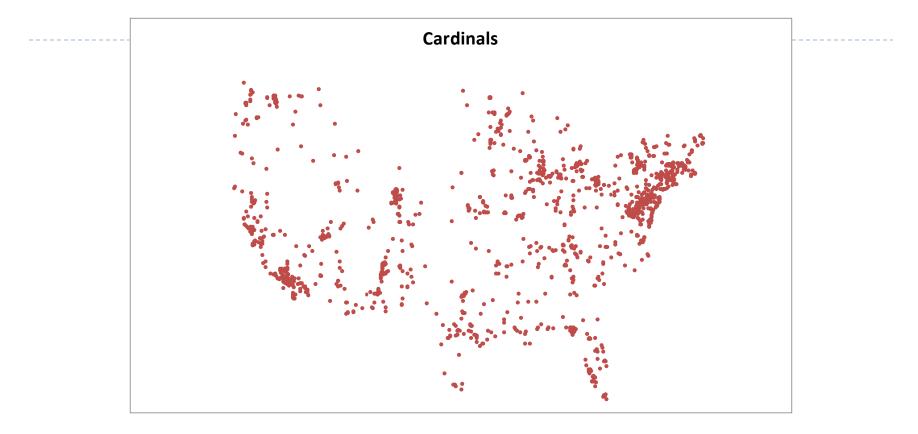


D

A few SDM Challenges

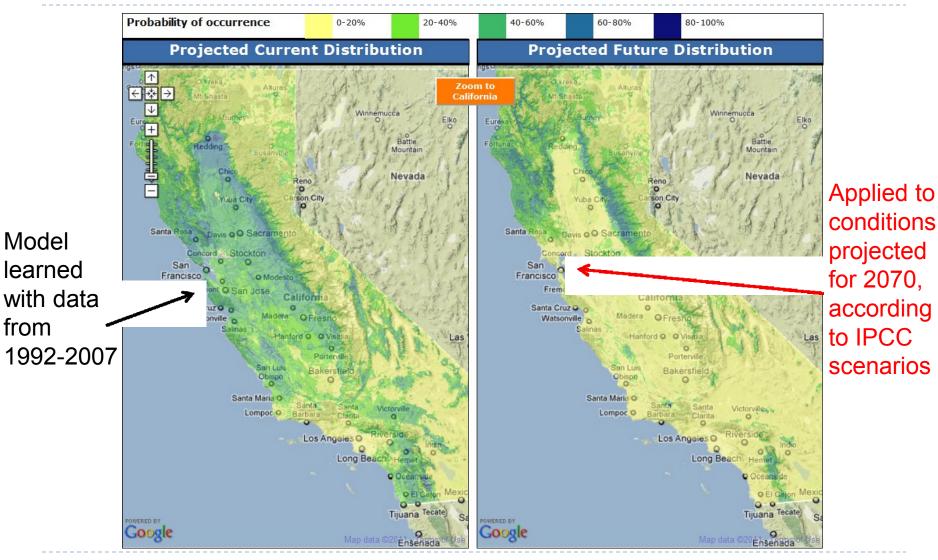
- Presence-only data
- Predictor-response relationships are non-stationary
- Imperfect detection of the species on surveys
 - Often lack prior knowledge of the system for model building
 - Observers have variable expertise/biases
- Sampling bias
- Extrapolation (e.g. under climate change)
- Evaluation strategies
- Estimating temporal trends directly
- More biologically-realistic models
- Multi-species models
- Models of abundance (instead of presence/absence)

Sampling Bias



- eBird participants tend to stay close to home.
- How can we make good predictions uniformly across the U.S.?

Inappropriate Extrapolation



⁸³ http://data.prbo.org/cadc2/index.php?page=climate-change-distribution

A few SDM Challenges

- Presence-only data
- Predictor-response relationships are non-stationary
- Imperfect detection of the species on surveys
 - Often lack prior knowledge of the system for model building
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- Evaluation strategies
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- Multi-species models
- Models of abundance (instead of presence/absence)

Ecological Models (part 2): Dynamical Models

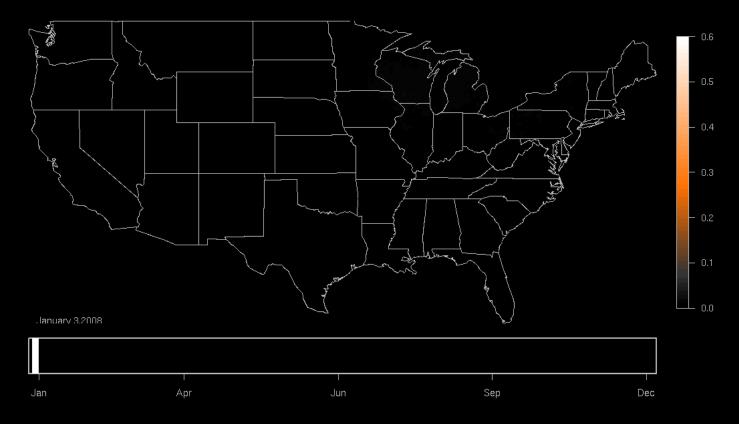
Dynamical Models

Dynamics are Central to Ecology

- Population growth, animal movement, predator/prey interaction, evolutionary game theory, etc.
- We will look at two particular models of broad-scale population dynamics
 - Bird migration
 - Metapopulations
- Primary motivation: treat species distributions explicitly as spatiotemporal processes
 - Foundation for prediction about future outcomes
 - In contrast with SDMs

Dynamical Model #1: Bird Migration

Motivation: eBird demonstrates clear migration patterns (but without a dynamical model)



Unique opportunity to extract quantitative knowledge about migration

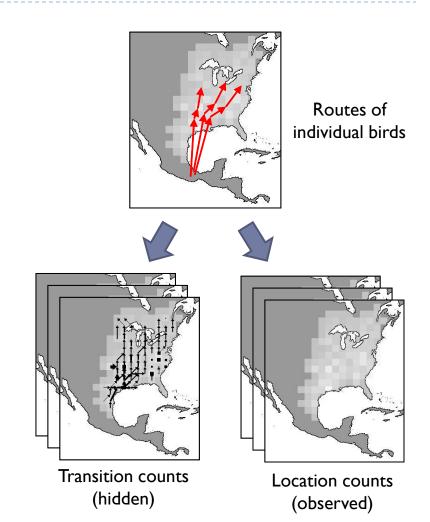
Challenges Extracting Migration Knowledge

Migration is a latent process

- eBird data and SDM predictions are static
 - Each observation/prediction for particular place and time
 - We see a sequence of snapshots
- Observations are noisy and incomplete
- Migration most naturally described at level of individual behavior, but we can only observe population-level statistics
 - Lack of modeling techniques to link the two

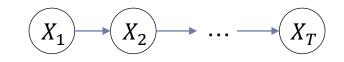
Overview: Collective Hidden Markov Models

- Generative model for population data from individual behavior
- 1. Define migration model for individual bird
 - Markov chain on grid cells
- 2. Generate routes for each individual in population
 - Assume birds are iid
- 3. Derive population statistics at each time step
 - Transition counts: # birds that fly between each pair of grid cells
 - Location counts: # birds in each grid cell

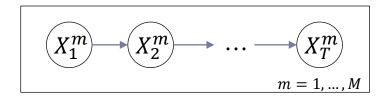


Overview: Collective Hidden Markov Models

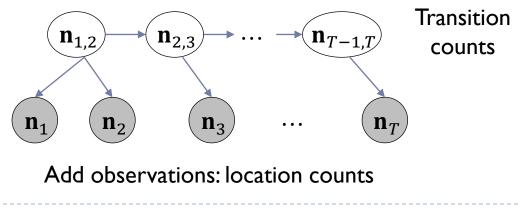
Individual model: Markov chain on grid cells



Population model: iid copies of individual model

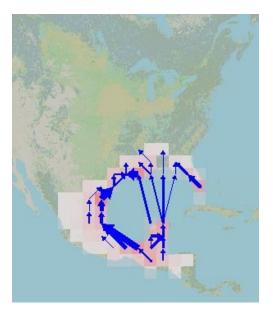


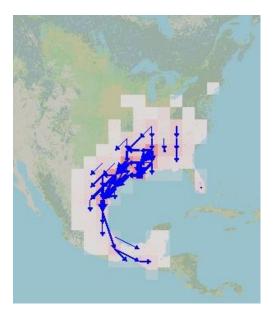
Marginalize out individuals: chain-structured model on sufficient statistics



Results

- Reconstruction by network flow techniques
- Use to visualize bird migration
 - E.g. Ruby-throated Hummingbird





Northbound March 5

Southbound October I

JCC 2012 Tutorial

Extensions

Collective Graphical Models [Sheldon & Dietterich, NIPS 2011]

- Substantial generalization of modeling ideas
- Parameter learning
- BirdCast Project (<u>http://birdcast.info</u>)
 - Joint project with Cornell Lab of Ornithology
 - Apply these ideas to forecast bird migration at continent-scale
 - Data: eBird + radar + acoustic + weather

Dynamical Model #2: Metapopulations

Dynamics of spatially disjoint populations

- Butterflies in alpine meadows
- Birds in a fragmented forest

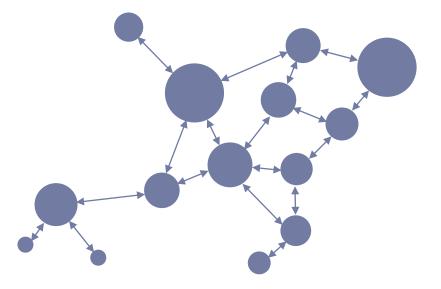


Metapopulation = population of populations

JCC 2012 Tutorial

Basic Components

- A network of habitat patches
- Dynamics models
 - Local population dynamics in each patch
 - Interaction between patches (dispersal/colonization)



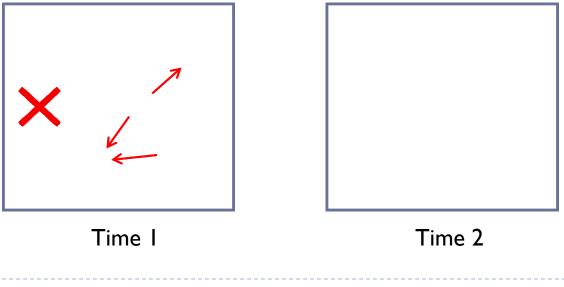
Metapopulation Background

Extremely important models in ecology

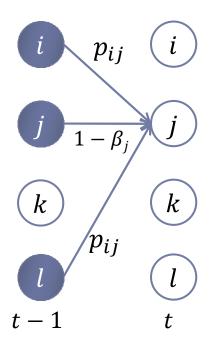
- Thousands of articles dating from 1960s with many modeling variations
 - Originally mathematical models for idealized landscapes
 - E.g. equidistant patches
 - Move to applied models, real landscapes
- Importance: formal basis for reasoning about the effects of habitat configuration on species persistence

SPOM: Stochastic Patch Occupancy Model

- Patches are occupied or unoccupied
- Two types of stochastic events:
 - Local extinction: occupied \rightarrow unoccupied
 - Colonization: unoccupied \rightarrow occupied (from neighbor)
- Independence among all events



SPOM Probability Model



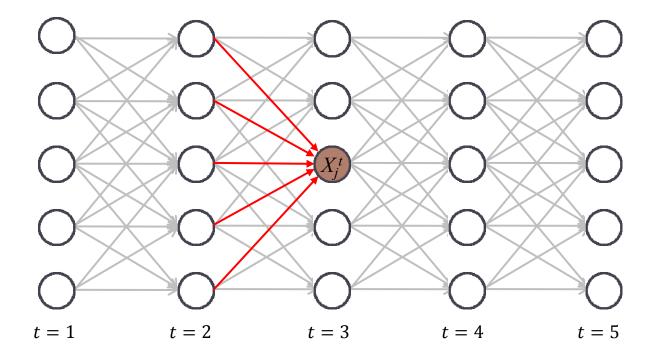
- To determine occupancy of patch j at time t
 - For each occupied patch $i \neq j$ from time t 1, flip coin with probability p_{ij} to see if *i* colonizes *j*
 - If j is occupied at time t 1, flip a coin with probability $1 - \beta_j$ to determine survival (non-extinction)
 - If any of these events occurs, *j* is occupied

Parameters:

- p_{ij} : colonization probability
- β_i : extinction probability
- functions of patch-size, inter-patch distance, etc.

SPOM as Dynamic Bayes Net (DBN)

• Let $X_j^t = 0$ or 1 be occupancy of patch j at time t



 $\Pr(X_j^t = 1 | \mathbf{X}^1, ..., \mathbf{X}^{t-1}) = \Pr(X_j^t = 1 | \mathbf{X}^{t-1})$

SPOM Fitting

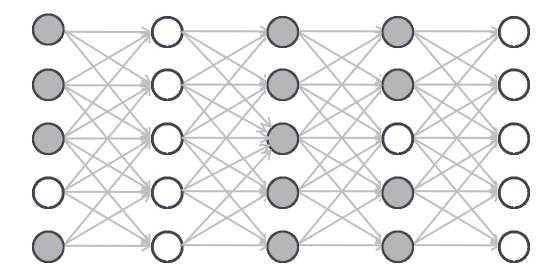
- Major advance in practical utility of SPOMs was ability to fit to survey data
 - Given: Occupancy vectors $\mathbf{X}^1, \mathbf{X}^2, \dots, \mathbf{X}^T$
 - Find: Parameters Θ for colonization and extinction models
- Hanski [1994] gave heuristic approach based on equilibrium properties of metapopulation
- Moilanen [1999]
 - Maximum likelihood approach

$$L(\Theta) = p(\mathbf{X}^{1}; \Theta) \prod_{t=2}^{T} p(\mathbf{X}^{t} | \mathbf{X}^{t-1}; \Theta)$$

- Easy in principle
 - Likelihood easy to evaluate
 - Small parameter space

Challenge: Missing Data

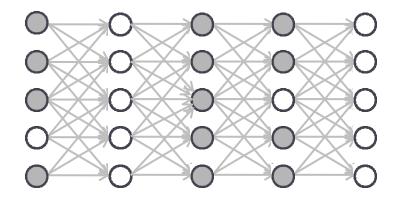
= observed values (either present or absent)



Field data is sparse and messy

- Surveys conducted in non-consecutive time steps
- Some patches are not surveyed

Fitting by Data Augmentation

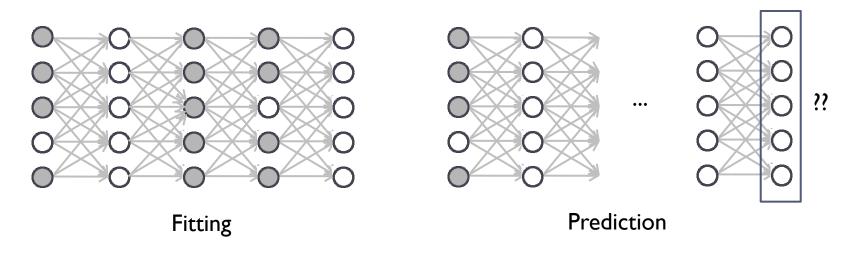


- Key step: fill in missing data by sampling from distribution of missing data given observed data
 - Maximum-likelihood approach of Moilanen [1999]
 - Bayesian approach of Ter Braak and Etienne [2003]

ML Opportunity

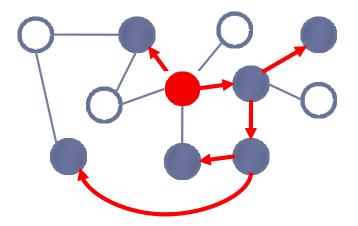
Improved methods for fitting?

- Key step is inference in P(missing | observed)
 - I.e., inference in DBN with metapopulation structure
 - Approximate inference techniques
- Importance of inference:

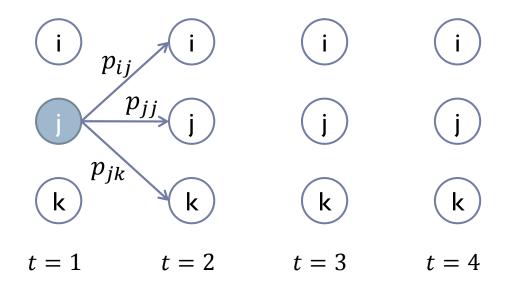


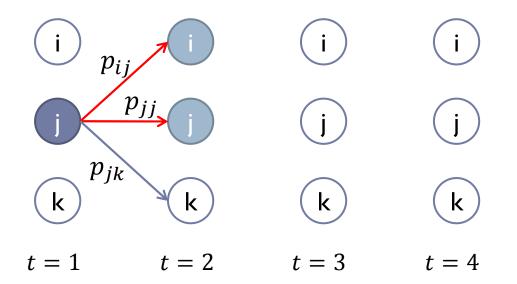
Connections to Network Cascades

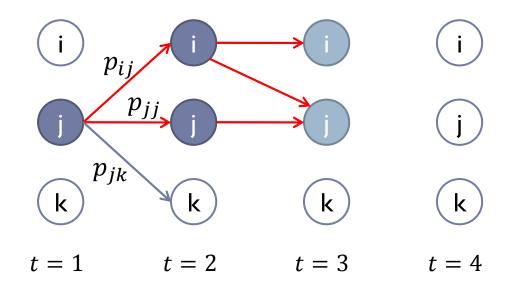
- Models for diffusion in (social) networks
 - Spread of information, behavior, disease, etc.
- Independent cascade model
 - Each individual passes information to friends independently with specified probability

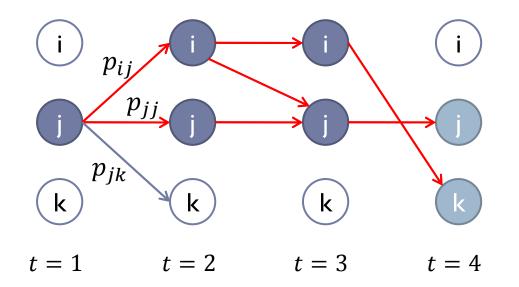


[Goldenberg, Libai, Muller 2001] [Kempe, Kleinberg, Tardos 2003]









ML connection: Social Network Inference

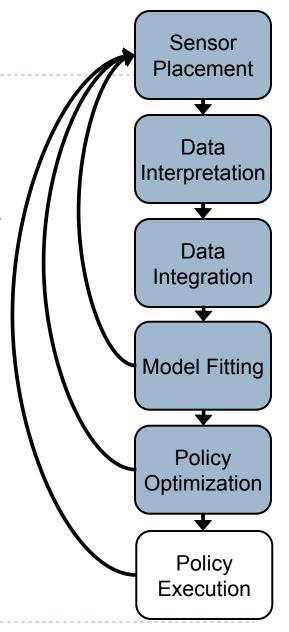
- Recent work in ML community to learn cascade models
 - Network is hidden
 - Observe infection times of nodes
- Maximum-likelihood estimation by convex optimization
 - [Myers and Leskovec, 2010]
 - [Gomez-Rodriguez et al., 2011]
- Applicability to SPOM fitting?
 - Model differences
 - Layered vs. non-layered graph
 - Time model
 - Much different parameterization

Coffee Break

Part 3: Policy Optimization

Outline

- Data Acquisition
 - Sensors: Physical sensors, human observers, repurposing data from other sources
 - Data interpretation: Extracting signals from data
- Ecological Models
 - Species Distribution Models
 - Dynamical Models: Dispersal, Migration, Invasion, Climate Change
- Policy Optimization
 - Conservation: Reserve design, Network design
 - Invasive species: Eradication, restoration, monitoring
 - Fisheries: Managing harvest levels



Optimal Policies for Environmental Management

One-shot problems

- Network design
- Reserve design
- Sequential decision-making problems (known as "Active Management")
 - Fisheries management
 - Fire management
 - Invasive species management
 - Reserve design and conservation easements over time
- Most problems are really sequential decision-making problems

Distinctive Aspects

- Optimizing an objective computed using a *learned* model of the system
 - Generalization of reinforcement learning
- Models are typically very bad
 - Doak, et al. 2008: Ecological Surprises
 - "Surprises are common and extreme"
 - Costs and benefits may be highly uncertain and non-stationary
 - Multiple objectives: Harvest + Species Viability
 - Need solutions that are robust to misspecified models

Large state and action spaces

Spatial models

Plan

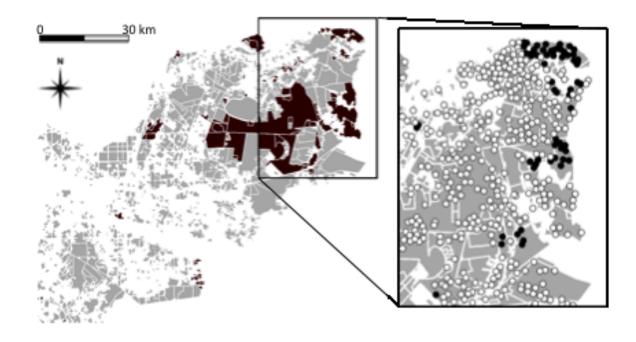
- Reserve Design for the Endangered Red Cockaded
 Woodpecker
 - One-shot design problem
- Optimal Policies for Managing Fisheries
 - Markov Decision Problem with analytical characterization of the optimal policy
- Managing Wildfire in Eastern Oregon
 - Large Spatial Markov Decision Problem (MDP)
- Optimal Management of Difficult-to-Observe Invasive Species
 - Small Partially-Observable MDP (POMDP)

SPOM Optimization: Reserve Design for Endangered Species

Given a limited budget to purchase additional patches, which should you buy?



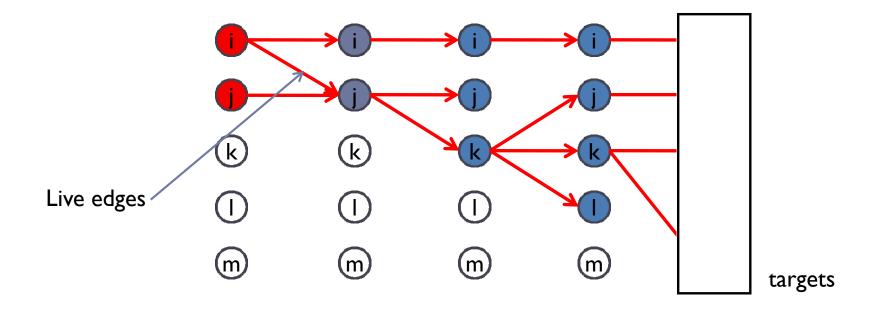
Red-cockaded woodpecker (endangered)



By viewing SPOM dynamics as a network cascade in the layered graph, we can formulate the conservation problem as a cascade optimization problem

Insight #1: Objective as Network Connectivity

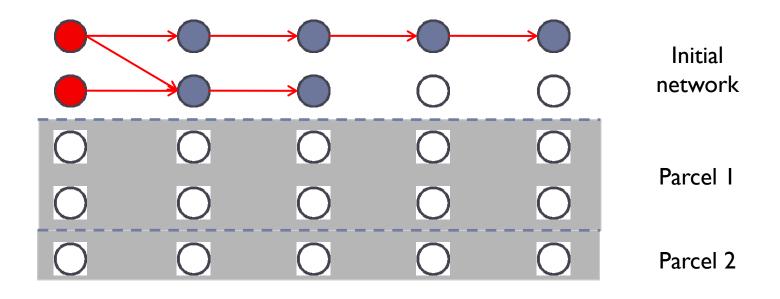
 Conservation objective: maximize expected # occupied patches at time T



Occupied patches = nodes reachable by live edges

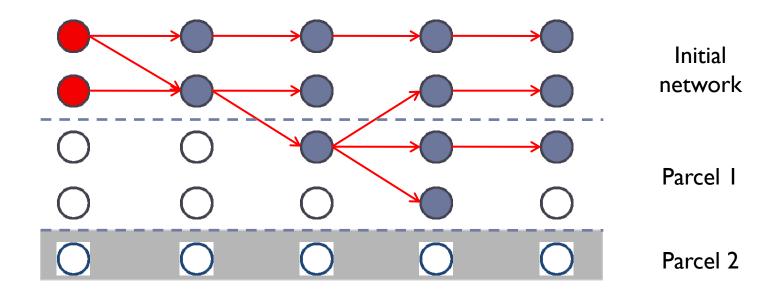
Insight #2: Management as Network Building

 Conserving parcels adds nodes and (stochastic) edges to the network



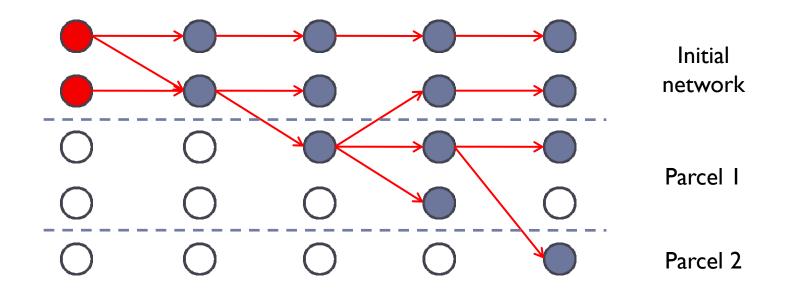
Insight #2: Management as Network Building

Conserving parcels adds nodes to the network



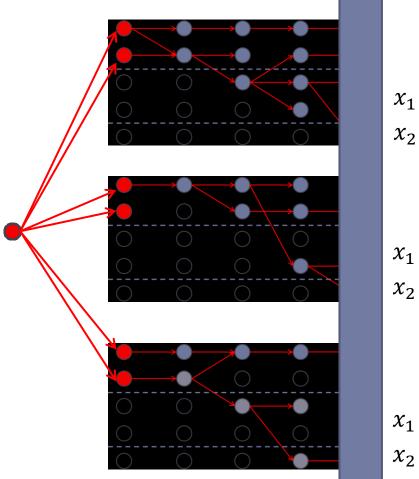
Insight #2: Management as Network Building

Conserving parcels adds nodes to the network



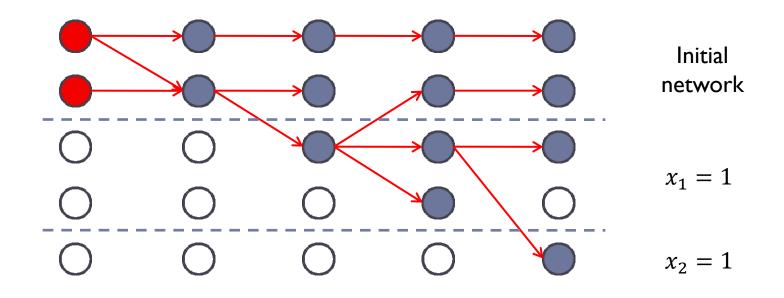
Solution Strategy

- Assume we own *all* parcels. Run multiple simulations of bird propagation
- 2. Join all of those simulations into a single giant graph
 - Goal of maximizing expected # of occupied patches at time T is approximated by # of reachable patches in the giant graph
- 3. Define a set of variables $\{x_1, x_2 \dots\}$, one for each parcel that we can buy
- Solve a mixed integer program to decide which x variables are 0 and which are 1



Why This Works

Using the simulation on the whole graph, it is easy to compute the results for any purchased subgraph



Sample Average Approximation (SAA)

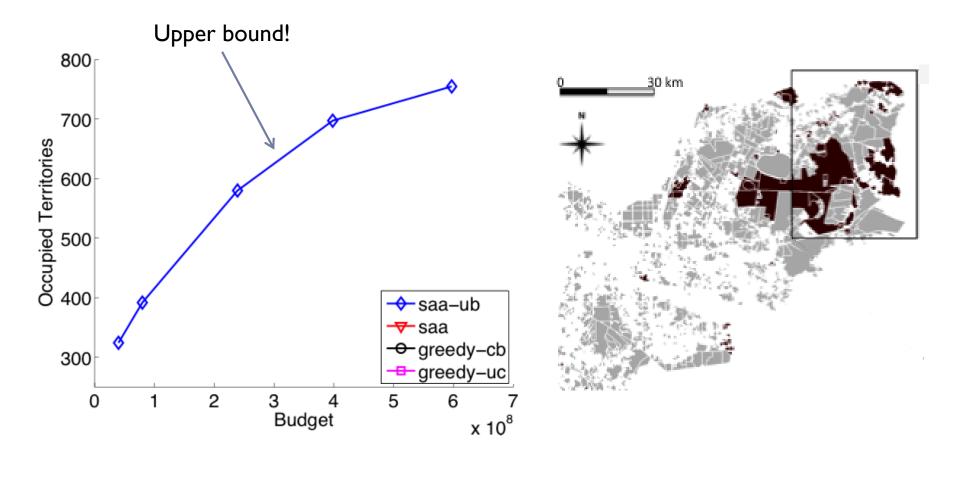
Generic approach to convert stochastic problem to deterministic problem:

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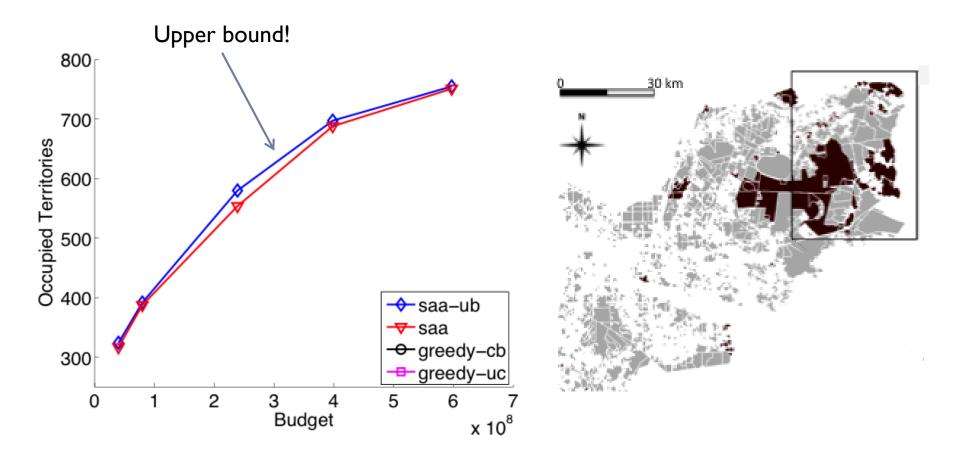
$$\max_{X} E_{Y}[f(X,Y)] \longrightarrow \max_{X} \frac{1}{N} \sum_{i=1}^{N} f(X,Y_{i})$$

- X: decision variable
- > Y: random variable
- Y_1, \ldots, Y_N : realizations of Y
- Nice properties
 - Converges to true optimum as $N \to \infty$
 - Error bounds
- Can we solve the sample average problem?

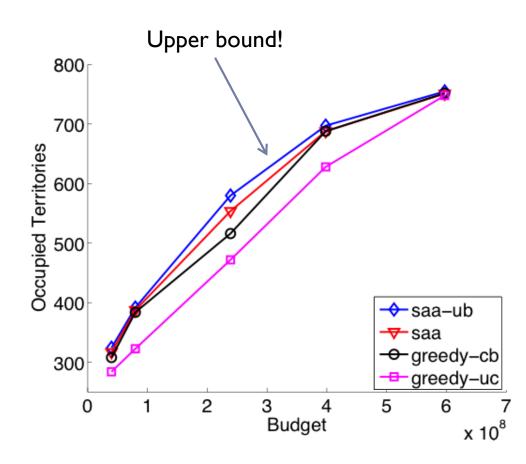
Results



Results



Results



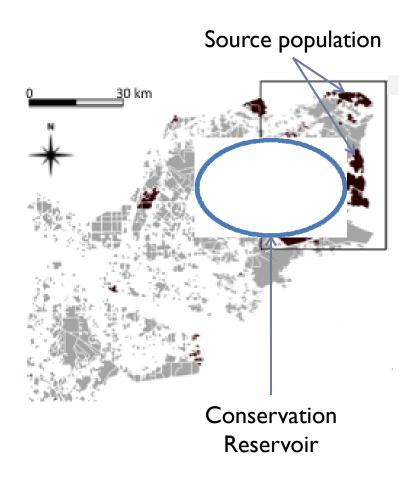
 Greedy baselines from related submodular cascade optimization problems

- [Kempe et al. 2003]
- [Leskovec et al. 2007]
- Our problem is not submodular
 - Why is greedy performing well?

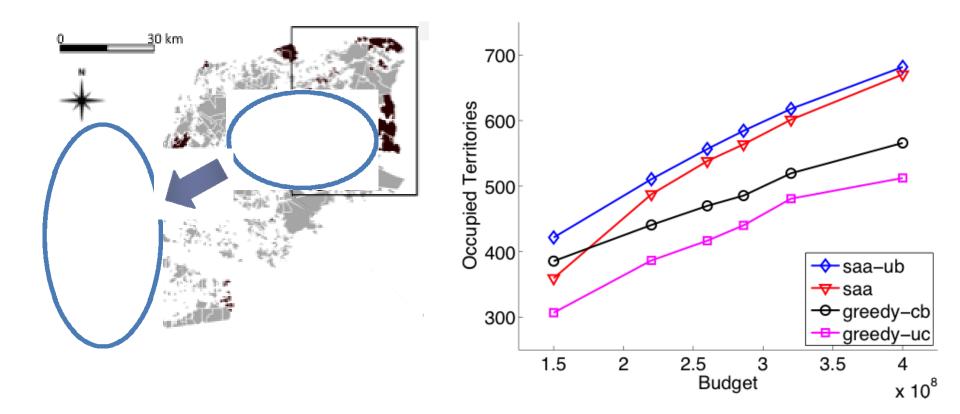
Conservation Strategies

Both approaches build outward from source

- Greedy buys best patches next to currently-owned patches
- Optimal solution builds toward areas of high conservation potential
- In this case, the two strategies are very similar

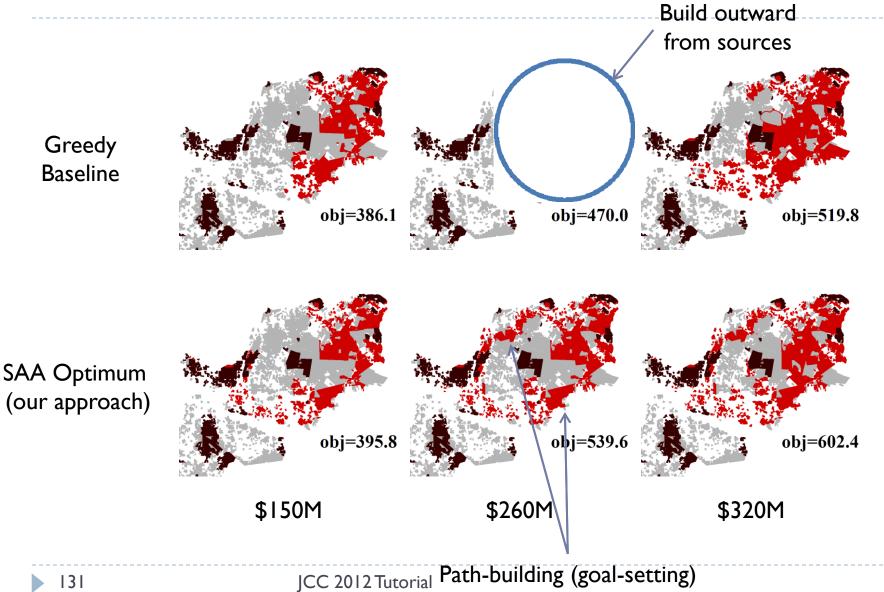


A Harder Instance



Move the conservation reservoir so it is more remote.

Conservation Strategies



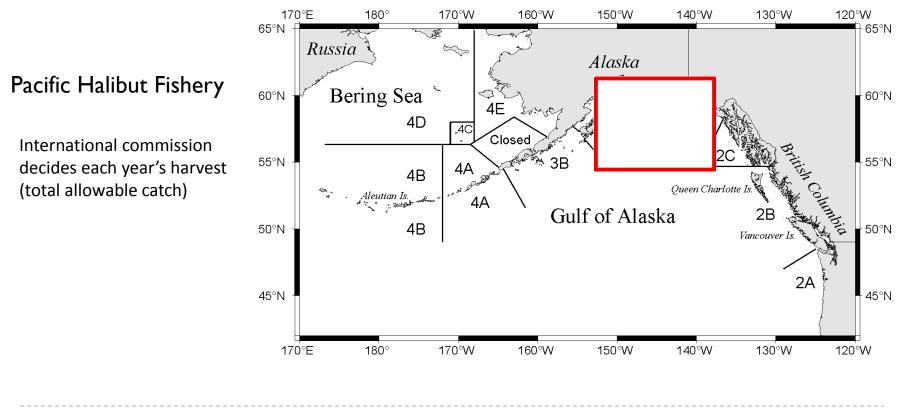
Future Challenges

The real world is complex

- Competing objectives
 - Multiple species
 - Competing uses of the land
- Model dynamics
 - Learn the SPOM
 - Include interactions among multiple species
 - $\hfill\square$ competition for nesting sites
 - \Box predation
- Markov Decision Processes (MDPs)
 - Buy some patches each year based on annual budgets
 - Make future purchases depending on where the birds actually go

Fishery Management [Ermon et al. 2010]

How to sustainably exploit a renewable and economically valuable resource such as forest or fishery?

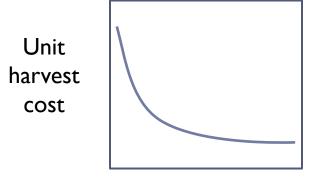


MDP Formulation

- State variable
 - x:stock (population size)

Actions

- Harvest amount h in each year
- Reward model
 - Fixed cost K when h > 0
 - Per-unit harvest cost
 - More \$\$ when fish are scarce
 - Per-unit market price p
 - Discount rate for future reward

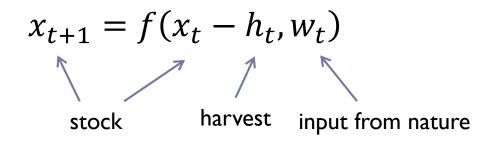


x (stock)

MDP Formulation (2)

Dynamics

Growth function f (post-harvest)

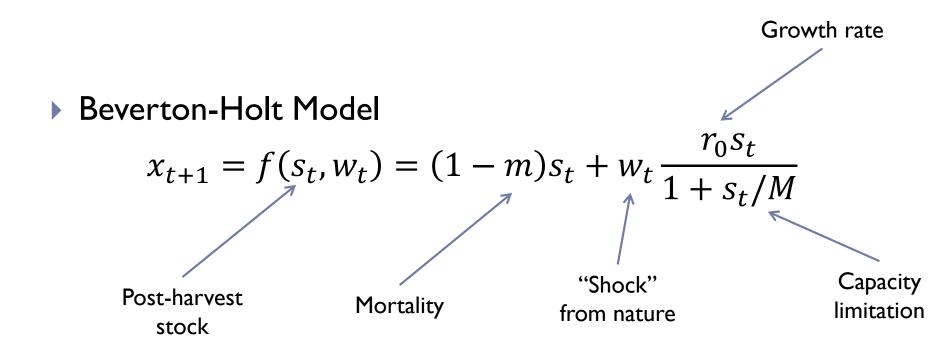


• Idea: w_t captures stochasticity or modeling uncertainty

State transition model

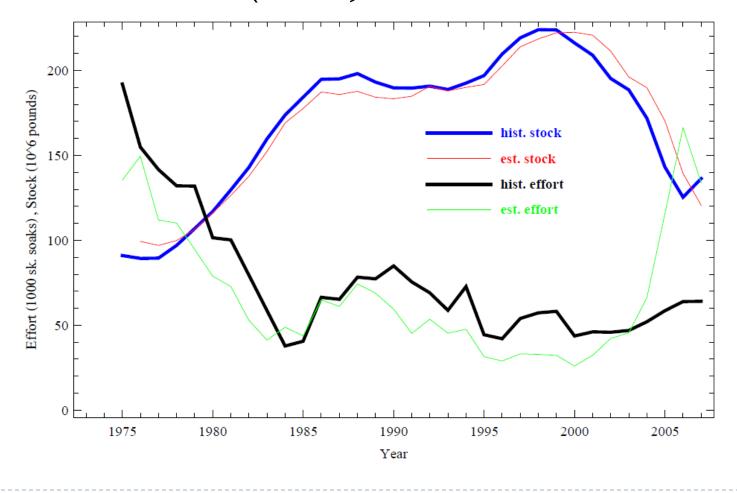
•
$$x \to f(x - h, w)$$
 with probability $p(w)$

Population Dynamics



Population Dynamics

Fit to historical data (w = 1)



Robust Optimization

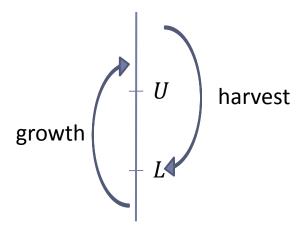
- Traditional MDP approach
 - Maximize expected total discounted reward
- Their approach: "Game against Nature"
 - Nature chooses w adversarially
 - Maximize worst-case total discounted reward

Advantages:

- Avoid catastrophic outcomes such as collapse of fishery
- Don't need fine-grained model for p(w)
 - Only specify allowable range of w

Main Result

- Analytical characterization of optimal policy
 - For a general class of growth and economic models, optimal policy is of S-s type



Stock > $U \rightarrow$ Harvest down to L

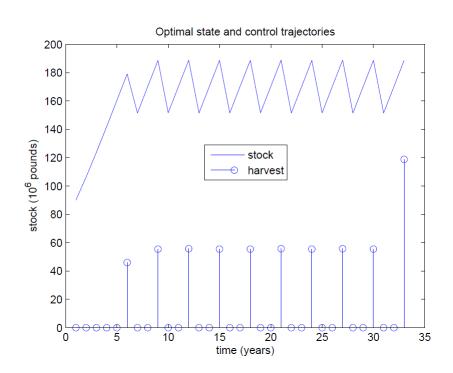
Stock $\leq U \rightarrow$ Let grow until U

- Proof based on mathematical notion of K-concavity [Scarf 1960]
 - From inventory control problems in economics and operations research

Pacific Halibut Results

Reanalysis of 1975-2007 data

- Fitted growth model
- Worst-case environmental inputs
- Optimal policy involves periodic closures of fishery
 - Maintain supply by rotating closures
- More revenue than baselines
 - Historical revenue
 - Current IPHC policy (Constant Proportional Policy; CPP)



Policy	Disc. revenue (\$)	Loss (\$)
Optimal $S - s$	9.05141×10^{8}	—
Historical rates	7.06866×10^8	1.98275×10^{8}
Average CPP	6.51849×10^{8}	2.53292×10^{8}

Important Themes for Environmental Policy

Synergy between economic reward and ecosystem stability

- Why no over-exploitation?
 - Protect future value of fishery
 - Cost to harvest scarce stock
- Cautionary notes
 - Barriers to over-exploitation are not intrinsic
 - \square High discount rate ightarrow prioritize present reward too much
 - \Box Technology improvements \rightarrow cheaper to harvest
 - Models often wrong or missing important side-effects

Robust optimization

141

- Prevents catastrophic outcomes (within modeling framework)
- Is worst-case too severe?
 - Extension to broader class of risk-sensitive objectives [Ermon et al. IJCAI, 2011]

Managing Wildfire in Eastern Oregon

Natural state (hypothesized):

- Large Ponderosa Pine trees with open understory
- Frequent "ground fires" that remove understory plants (grasses, shrubs) but do not damage trees

Fires have been suppressed since 1920s

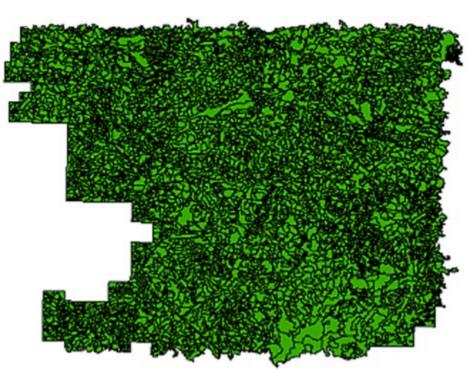
- Large stands of Lodgepole Pine
- Heavy accumulation of fuels in under-story
- Large catastrophic fires that kill all trees and damage soils
- Huge firefighting costs and lives lost





Formulation as an MDP

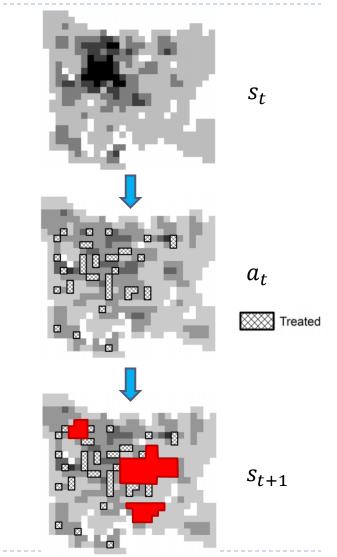
- Divide landscape into 4000 Management Units
- I0-Year time step
- State of each MU:
 - Age of trees
 - **{0-9, 10-19, 20-29, 30-39, 40-49}**
 - Amount of fuel
 - {none, low, medium, high, very high}
 - 25 possible combinations
 - > 25^{4000} possible states for the landscape
- Actions in each MU each decade
 - Do nothing
 - Fuel treatment (costs money)
 - Harvest trees (makes money, but increases fuel)
 - Harvest + Fuel
 - ▶ 4⁴⁰⁰⁰ possible actions over landscape



Study area in Deschutes National Forest

Game Against "Neutral" Nature

- For each time step t
 - Our turn:
 - Observe current state s_t (i.e., state of all MUs)
 - Choose action vector a_t
 - Execute the actions in the MUs
 - Nature's turn:
 - Stochastically ignite and burn fires on the landscape (Implemented by ignition model + fire spread model)
 - Grow trees and fuel (Implemented by forest growth model)



Open Problem: Solving This MDP

- One-shot Method [Wei, et al., 2008]
 - Run 1000s of simulated fires to generate fire risk map and fire propagation graph
 - Formulate and solve Mixed Integer Program to compute optimal one-shot solution
- Challenge:
 - Develop methods that can solve the MDP over long time horizons

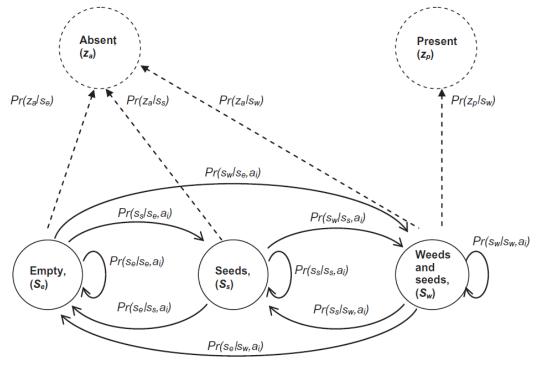
Optimal Management of Difficult-to-Observe Invasive Species [Regan et al., 2011]

- Branched Broomrape (Orobanche ramosa)
 - Annual parasitic plant
 - Attaches to root system of host plant
 - Results in 75-90% reduction in host biomass
 - Each plant makes ~50,000 seeds
 - Viable for 12 years
- Quarantine Area in S.Australia
 - > 375 farms; 70km x 70km area
 - Transition from eradication to management



Formulation as a POMDP: Single Farm

- States:
 - {Empty, Seeds, Plants & Seeds}
- Actions:
 - {Nothing, Host Denial, Fumigation}
- Observations:
 - Absent, Present}
 - Detection probability d
- Rewards:
 - Cost(Nothing) < Cost(Host Denial) « Cost(Fumigation)
- Objective:
 - 20-year discounted reward (discount = 0.96)



State Diagram

Optimal MDP Policy

If plant is detected, Fumigate; Else Do Nothing

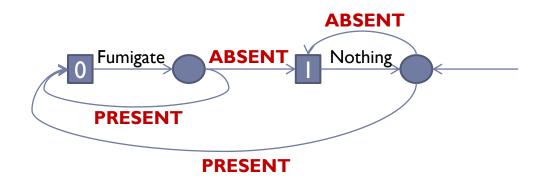
Assumes perfect detection



www.grdc.com.au

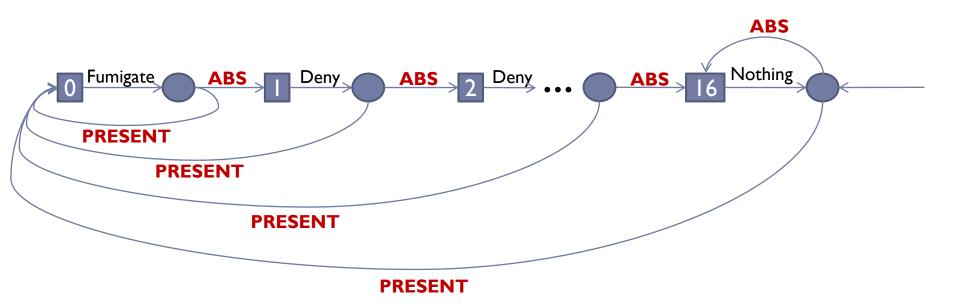
Optimal Policy for $d \ge 0.5$





Same as the Optimal MDP Policy

Optimal Policy for d = 0.3



- Deny Host for 15 years before switching to Nothing
- For d = 0.1, Deny Host for 17 years before switching to Nothing

Discussion

- POMDP is exactly solvable because the state space is very small
- Real problem is a spatial meta-population at two scales
 - Within a single farm
 - Among the 375 farms in the quarantine area
 3³⁷⁵ states
 - Exact solution of large POMDPs is beyond the state of the art

Outline

Data Acquisition

- Sensors: Physical sensors, human observers, repurposing data from other sources
- Data interpretation: Extracting signals from data

Ecological Models

- Species Distribution Models
- Dynamical Models: Dispersal, Migration, Invasion, Climate Change

Policy Optimization

- Conservation: Reserve design, Network design
- Invasive species: Eradication, restoration, monitoring
- Fisheries: Managing harvest levels

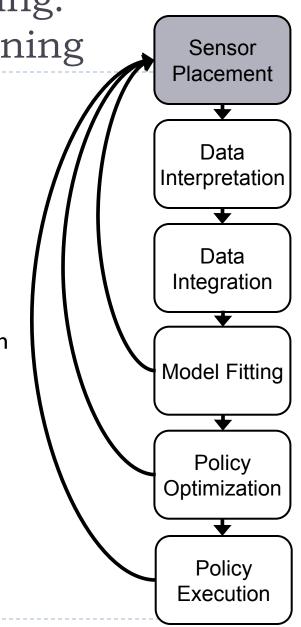
Challenges for Machine Learning: Sensor Placement/Active Learning

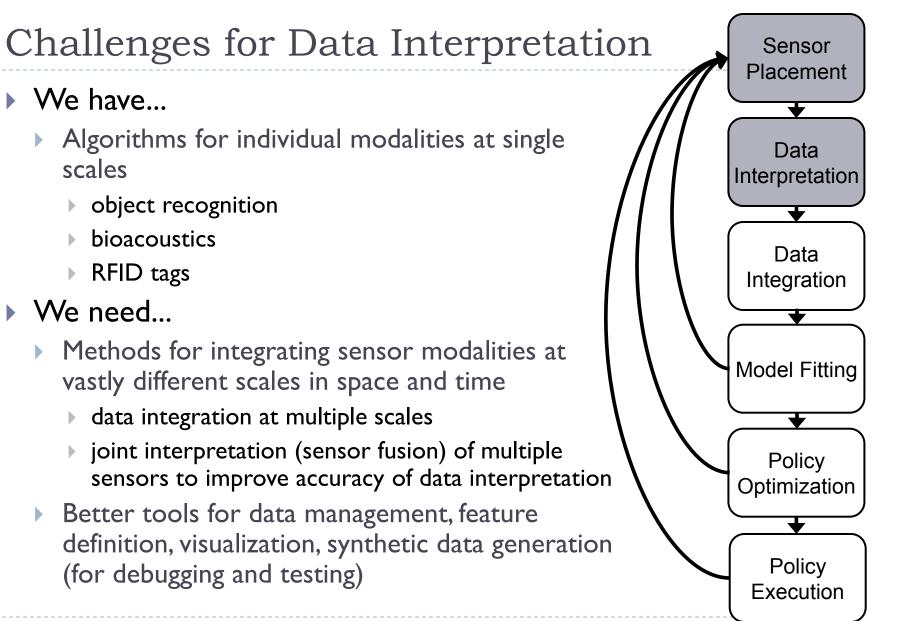
• We have...

- Algorithms for one real-valued quantity
 - assuming stationary correlations, perfect observations

• We need...

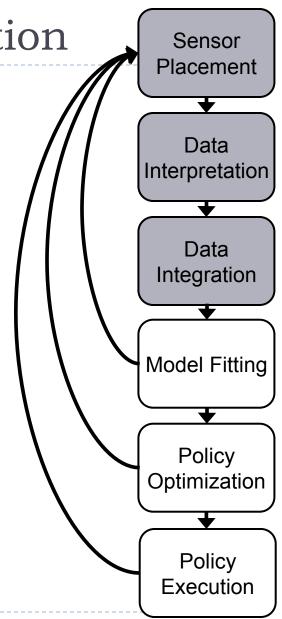
- Algorithms for multiple quantities
 - real-valued: nutrients, temperature, precipitation
 - counts: species abundance for multiple species
 - discrete: species presence/absence for multiple species
- Algorithms that consider dynamics, detectability, patchiness (meta-populations)





Challenges for Data Integration

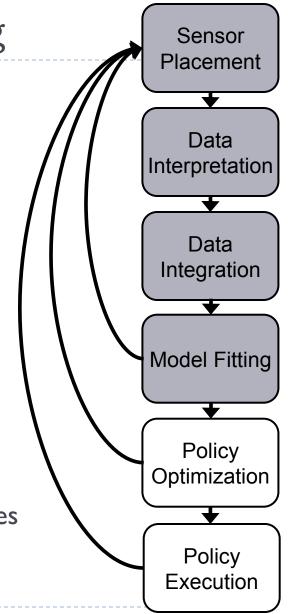
- How do we integrate data from multiple temporal and spatial scales while retaining all of the detail?
 - Joint modeling of the ecological process and the data collection process?
 - Integrate at a small number of scales?
 - Are there general-purpose strategies? Can there be general tools?



Challenges for Model Fitting

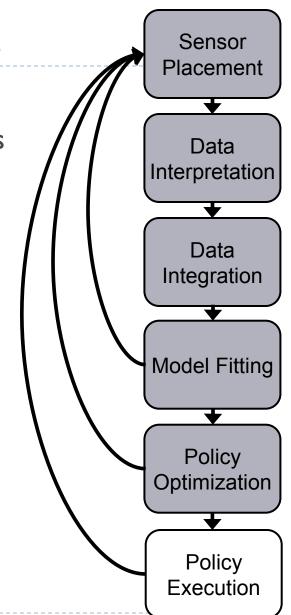
• We have...

- Species Distribution Models for single species with partial detectability
 - stationary, non-spatial
- We need...
 - Species Distribution Models for thousands of species
 - model competition, predation, dispersal
 - explicitly spatial
 - Meta-Population Models for multiple species
 - Models that link abiotic quantities (nutrients, temperature, precipitation) and biotic quantities (species, populations)



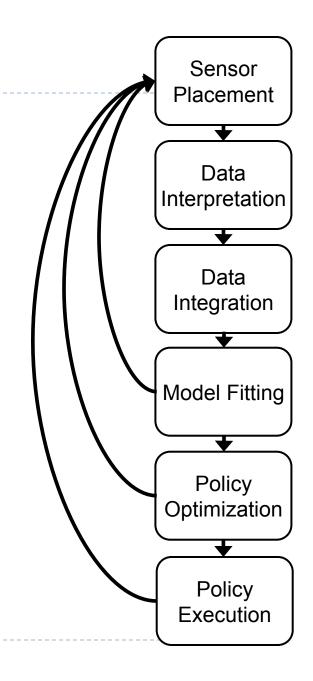
Challenges for Optimization

- We have...
 - One-shot algorithms for meta-populations and fires
 - Exact algorithms for modest-sized MDPs
 - Exact algorithms for tiny POMDPs
 - Algorithms that optimize a scalar reward in expectation
- We need...
 - Algorithms for MDP/POMDP planning for meta-populations and spatial processes
 - That consider multiple criteria
 - That are robust to mis-specified dynamics and rewards



Data → Models → Policies: Overall Challenges

- It isn't a pipeline
 - We need algorithms that integrate/couple all parts of the process
 - Learning algorithms should be integrated with policy optimization
 - Sensor placement should be sensitive to all goals



Closing

- Links to data, software, and papers available in the electronic version of these slides
- Thank-you's
 - Dan Sheldon and Rebecca Hutchinson
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 - David Winkler
 - Jane Elith and Steven Phillips
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 - ACM Distinguished Lecturers Program

Questions?

Data Resources

- Species Distribution Models
 - eBird Reference Dataset 3.0
 - http://www.avianknowledge.net/content/features/archive/ebird-referencedataset-3-0-released
 - eBird checklist data along with an excellent set of covariates
 - set of suggested analysis problems
- Fine-Grained Image Classification
 - Oregon State STONEFLY9 dataset
 - http://web.engr.oregonstate.edu/~tgd/bugid/stonefly9/
 - Oregon State EPT29 dataset
 - http://web.engr.oregonstate.edu/~tgd/bugid/ept29/
 - Caltech/UCSD CUB-200 bird dataset
 - http://www.vision.caltech.edu/visipedia/CUB-200.html
 - Oxford Flower dataset (102 classes)
 - http://www.robots.ox.ac.uk/~vgg/data/flowers/102/index.html

Model Resources

- Meta-Population Models
 - SPOMSIM
 - http://www.helsinki.fi/bioscience/consplan/software/SPOMSIM.html
 - Synthetic Red-Cockaded Woodpecker instances
 - http://www.cs.cornell.edu/~kiyan/rcw/generator.htm

Machine Learning Algorithms

- Phillips' Maxent Package
 - http://www.cs.princeton.edu/~schapire/maxent/

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