

SECTION 4: ALGORITHMIC THINKING

ENGR 112 – Introduction to Engineering Computing

2

Algorithmic Thinking

Algorithmic Thinking

3

- ***Algorithmic thinking:***

- The ability to identify and analyze problems, and to develop and refine algorithms for the solution of those problems

- ***Algorithm:***

- Detailed step-by-step procedure for the performance of a task

- Learning to program is about developing algorithmic thinking skills, *not* about learning a programming language

Algorithms

4

- Ultimately, algorithms will be implemented by writing code in a particular programming language
- Algorithm design is (mostly) language-independent
 - A procedure that can be implemented in any language
- Universal algorithm representations:
 - Flowcharts
 - Graphical representation
 - Pseudocode
 - Natural language
 - Not necessarily language-independent

5

Flowcharts

Flow Charts

6

- **Flowcharts** are graphical representations of algorithms
- Interconnection of different types of blocks
 - ▣ Start/End
 - ▣ Process
 - ▣ Conditional
 - ▣ Input/Output
- Connection paths indicate flow from one step in the procedure to the next
- Well-constructed flowcharts are easily translated into code later

Flowchart Blocks

7

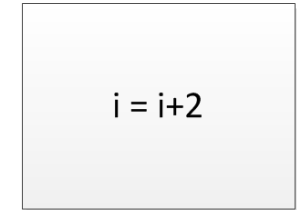
□ Start/End

- Always indicate the start and end of any flowchart



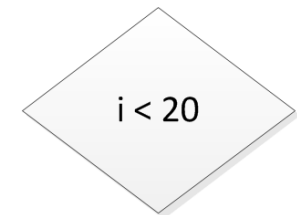
□ Process

- Indicates the performance of some action



□ Conditional

- Performs a check and makes a decision
- Binary result: True/False, Yes/No, 1/0
- Algorithm flow branches depending on result



□ Input/Output

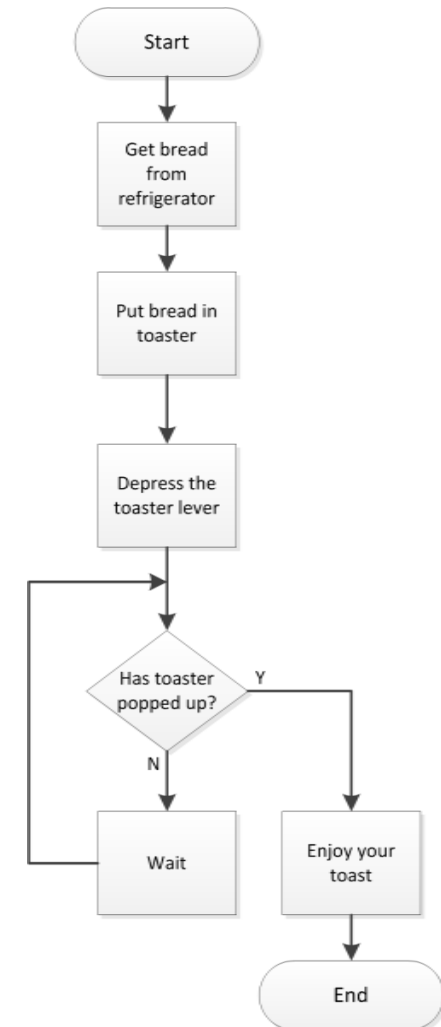
- Input or output of variables or data



Flowchart – Example

8

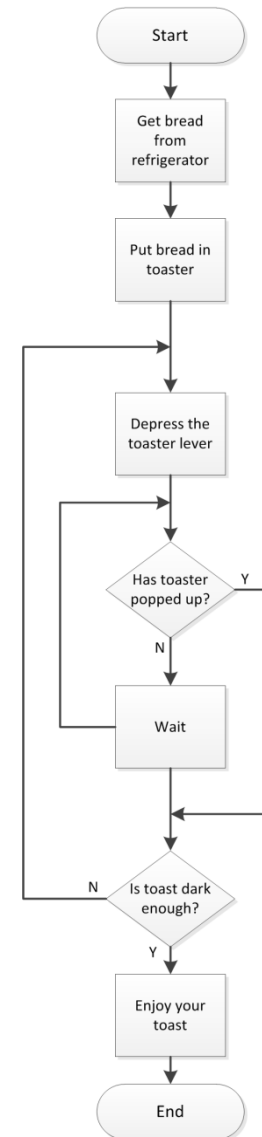
- Consider the very simple example of making toast
- Process flows from Start to the End through the process and conditional blocks
 - ▣ Arrows indicate flow
 - ▣ Conditional blocks control flow branching
- Note the loop defining the waiting process
 - ▣ *Wait* block is unnecessary



Flowchart – Example

9

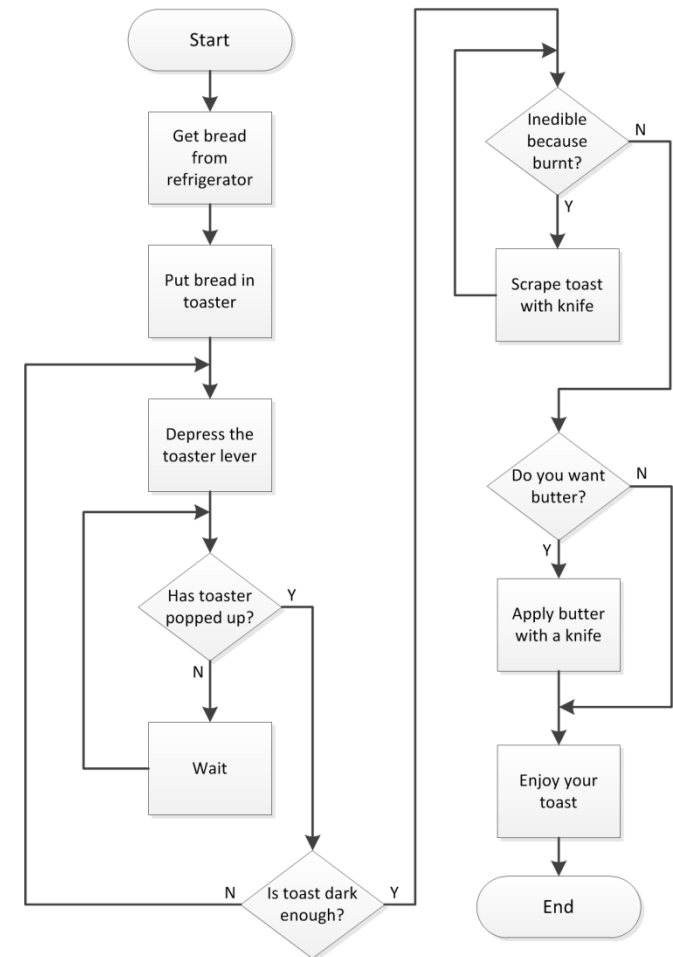
- Flowchart for a given procedure is not unique
 - ▣ Varying levels of complexity and detail are always possible
- Often important to think about and account for various possible outcomes and cases
 - ▣ For example, is your toast always done after it first pops up?
 - ▣ Here, part of the procedure is repeated if necessary



Flowchart – Example

10

- Taking this example further, consider the possibility of burnt toast or the desire for butter
 - ▣ Another loop added for continued scraping until edible
 - ▣ Also possible to bypass portions of the procedure – e.g., the scraping of the toast or the application of butter
- Can imagine significantly more complex flow chart for the same simple procedure ...



11

Common Flowchart Structures

Common Flowchart Structures

12

- Several basic structures occur frequently in many different types of flowcharts
 - ▣ Recurrent basic structures in many algorithms
- Ultimately translate to recurrent code structures
- Two primary categories
 - ▣ ***Conditional statements***
 - ▣ ***Loops***
- In this section of notes, we'll gain an understanding of flowchart structures that fall into these two categories
- In the next section of notes we'll learn how to implement these structures in code

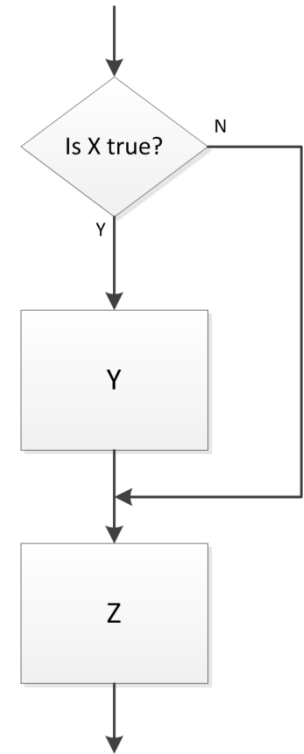
Conditional Statements

- `if` statements
- Logical and relational operators
- `if...else` statements

Conditional Statements – *if*

14

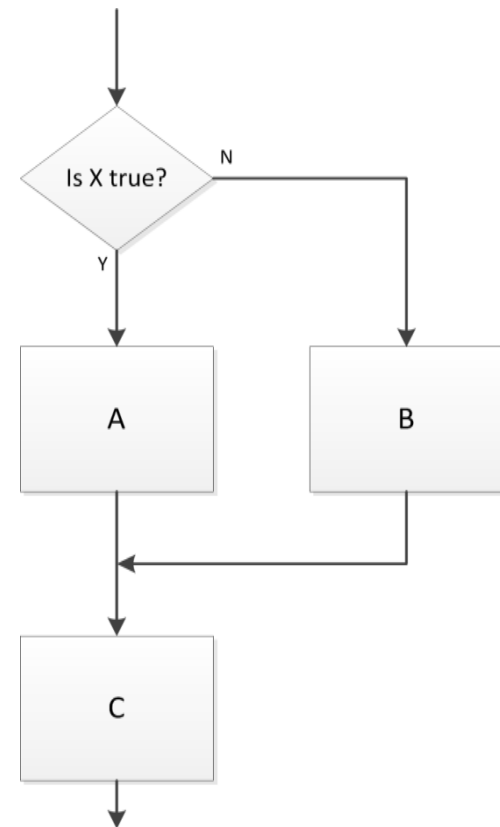
- Flowcharts represent a set of instructions
 - Blocks and block structures can be thought of as ***statements***
- Simplest ***conditional statement*** is a single ***conditional block***
 - An ***if structure***
 - If X is true, then do Y, if not, don't do Y
 - In either case, then proceed to do Z
 - Y and Z could be any type of process or action
 - E.g. add two numbers, turn on a motor, butter the toast, etc.
 - X is a ***logical expression*** or ***Boolean expression***
 - Evaluates to either true (1) or false (0)



Conditional Statements – *if ... else*

15

- Can instead specify an action to perform if X is not true
 - ▣ An ***if ... else structure***
 - ▣ If X is true, then do A, else do B
 - ▣ Then, move on to do C
- Here, a different process is performed depending on the value of X (1/0, T/F, Y/N)



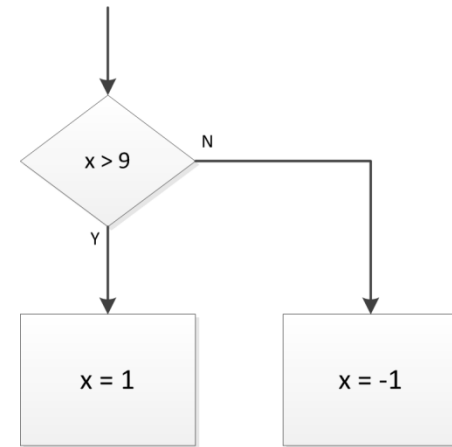
Conditional Statements – *if ... else*

16

- Logical expression with a single **relational operator**

$$x > 9$$

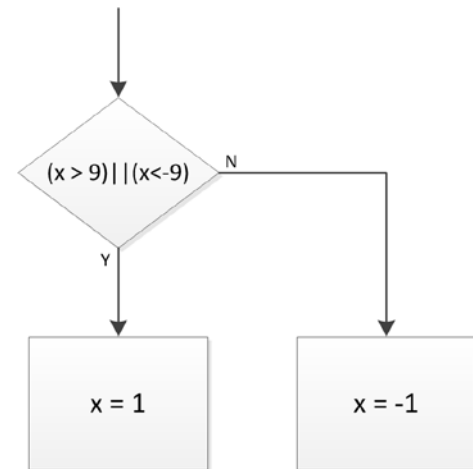
- Either **true** (Y) or **false** (N)
- If true, $x = 1$
- If false, $x = -1$



- Logical expression may also include a **logical operator**

$$(x > 9) || (x < -9)$$

- Again, statement is either **true** or **false**
- Next process step dependent on value of the conditional logical expression



Logical or Relational Expressions

17

- Logical expressions use **logical** and **relational operators**

Operator	Relationship or Logical Operation	Example
==	Equal to	x == b
~=	Not equal to	k ~= 0
<	Less than	t < 12
>	Greater than	a > -5
<=	Less than or equal to	7 <= f
>=	Greater than or equal to	(4+r/6) >= 2
~	NOT– negates the logical value of an expression	~(b < 4*g)
&&	AND – both expressions must evaluate to true for result to be true	(t > 0) && (c == 5)
	OR – either expression must evaluate to true for result to be true	(p > 1) (m > 3)

Logical Expressions – Examples

18

- Let $x = 12$ and $y = -3$
- Consider the following logical expressions:

Logical Expression	Value
$(x + y) == 15$	0
$(y == 2) (x > 8)$	1
$\sim(y < 0)$	0
$(y/2 + 1 < -1)$	0
$(x == 12) \&\& \sim(y \geq 5)$	1
$(y \sim = 2) (x < 10) (x < y)$	1
$((x == 2) \&\& (y < 0)) ((x \geq 5) \&\& (y \sim = 8))$	1

Conditional Statements – *if ... elseif ... else*

19

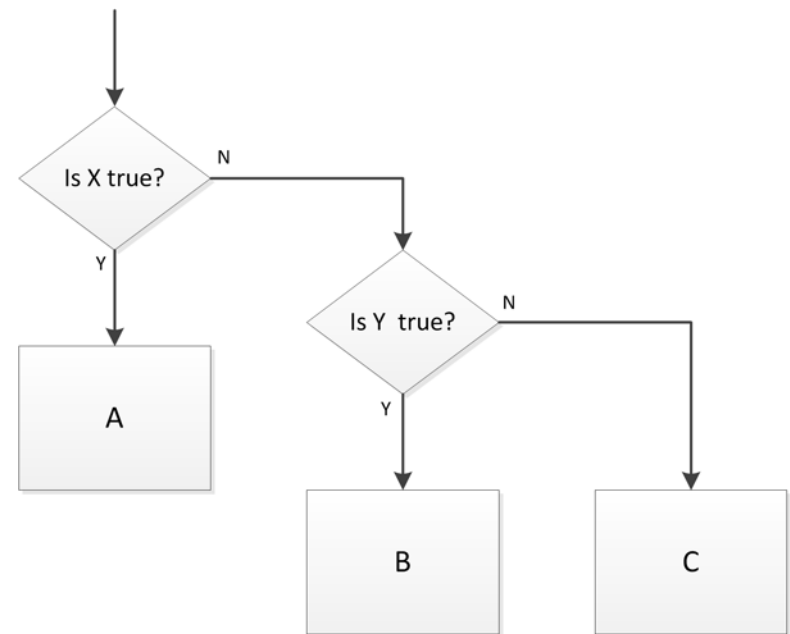
- Two conditional logical expressions

- If the X is true, do A
- If X is false, evaluate Y
 - If Y is true, do B
 - If Y is false, do C

- The ***if ... elseif ... else structure***

- Can include an arbitrary number of *elseif* statements

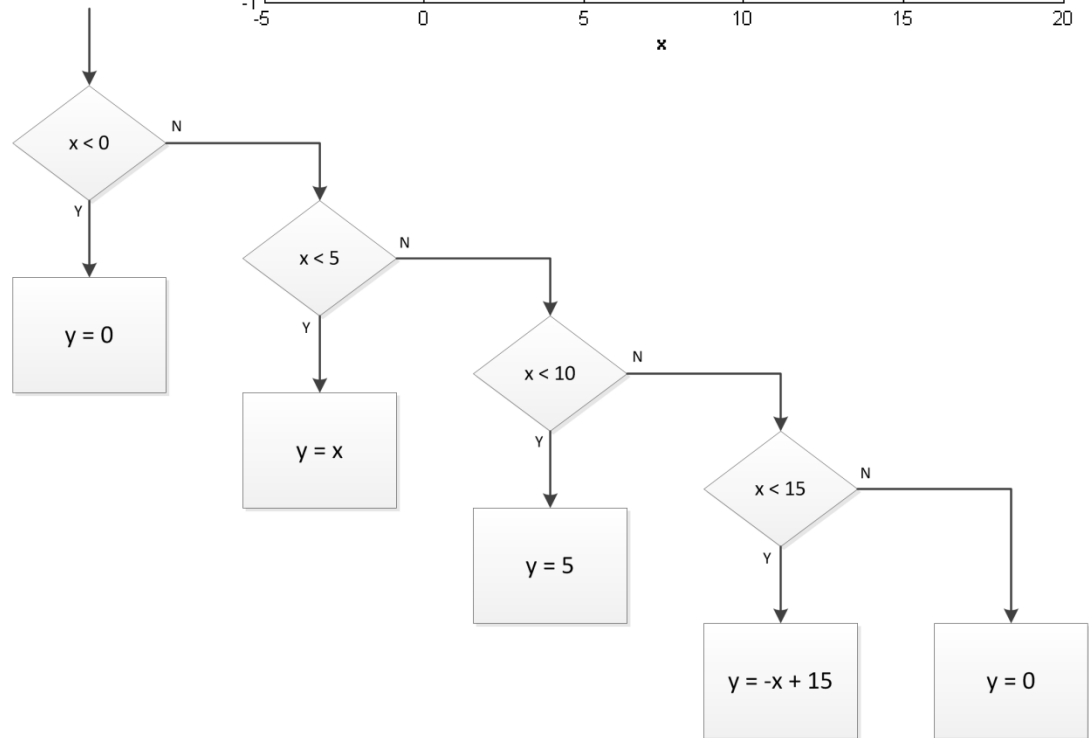
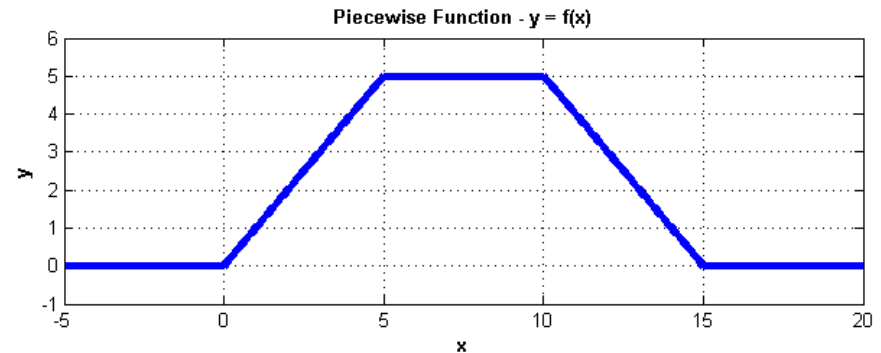
- Successive logical statements evaluated only if preceding statement is false



if ... elseif ... else – Example

20

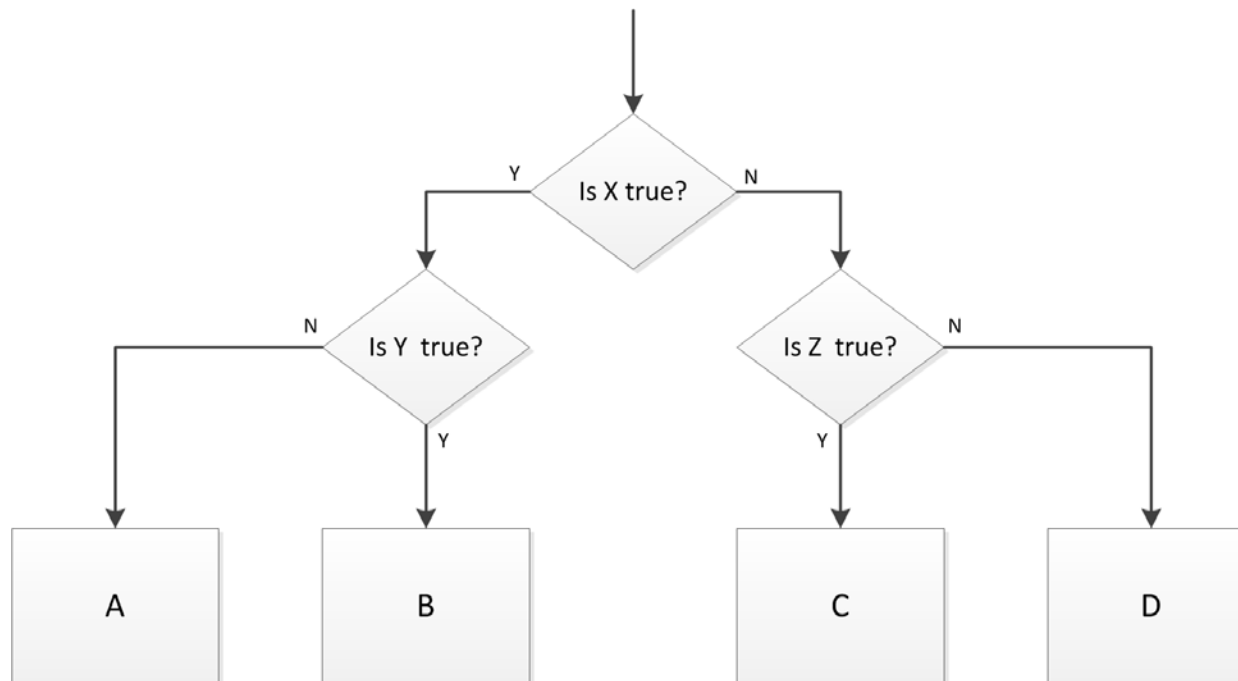
- Consider a ***piecewise linear function*** of x
 - ▣ $y = f(x)$ not defined by a single function
 - ▣ Function depends on the value of x
 - ▣ Can implement with an ***if ... elseif ... else*** structure



if Statements – Other Configurations

21

- In previous examples, successive logical statements only evaluated if preceding statement is false
- Result of a true logical expression can also be the evaluation of a second logical expression



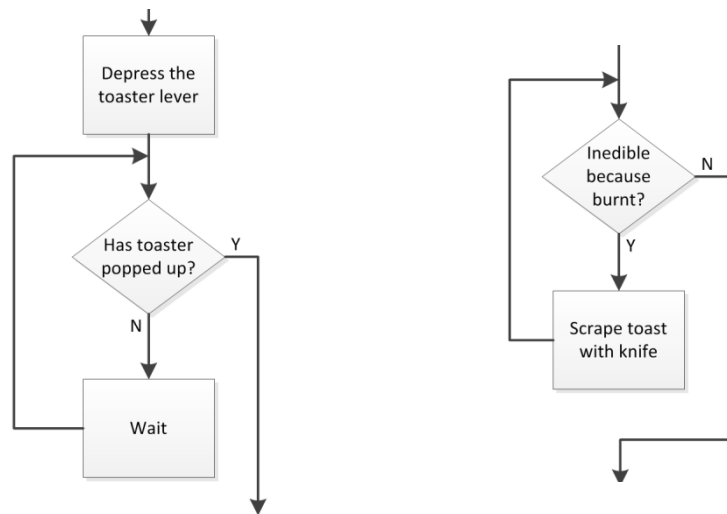
Loops

- *while* loops
- *for* loops

Loops

23

- We've already seen some examples of flow charts that contain **loops**:



- Structures where the algorithmic flow loops back and repeats process steps
 - Repeats as long as a certain condition is met, e.g., toaster has not popped up, toast is inedible, etc.

Loops

24

- Algorithms employ two primary types of loops:
 - **while loops**: loops that execute as long as a specified condition is met – loop executes as many times as is necessary
 - **for loops**: loops that execute a specified exact number of times
- Similar looking flowchart structures
 - for loop can be thought of as a special case of a while loop
 - However, the distinction between the two is very important

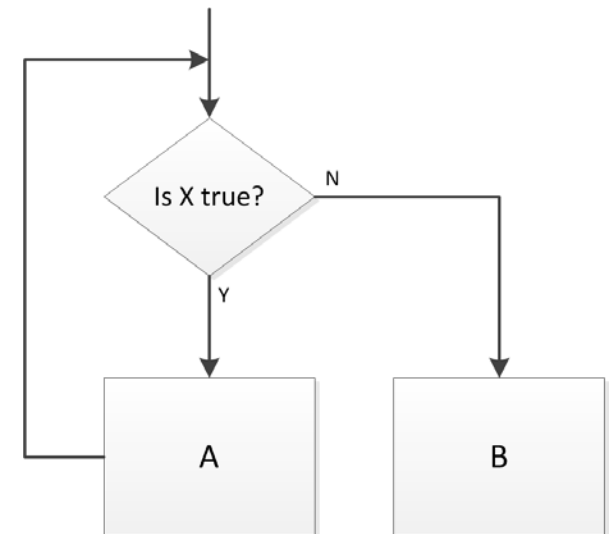
25

while Loop

while Loop

26

- Repeatedly execute an instruction or set of instructions as long as (*while*) a certain condition is met (is *true*)
- Repeat *A while X is true*
 - As soon as *X* is no longer true, *break* out of the loop and continue on to *B*
 - *A* may never execute
 - *A* may execute only once
 - *A* may execute forever – an ***infinite loop***
 - If *A* never causes *X* to be false
 - *Usually* not intentional



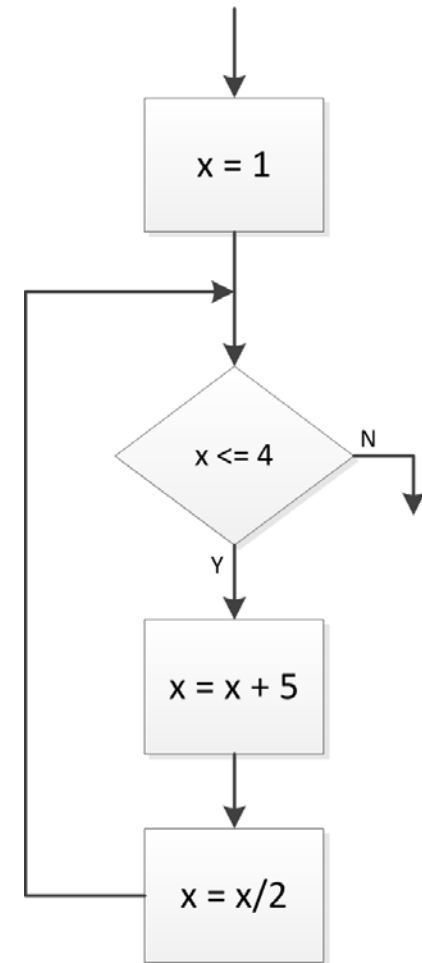
while Loop

27

- Algorithm loops while $x \leq 4$
 - ▣ Loops three times:

Iteration	x
0	1
1	6
2	8
3	9
	4.5

- Value of x exceeds 4 several times during execution
 - ▣ x value checked at the beginning of the loop
- Final value of x is greater than 4

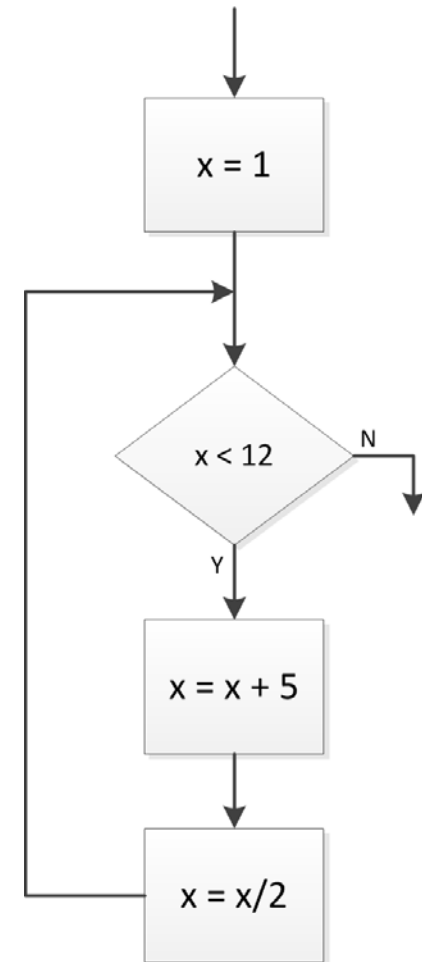


while Loop – Infinite Loop

28

- Now looping continues as long as $x < 12$
 - ▣ x never exceeds 12
 - ▣ Loops forever – an *infinite loop*

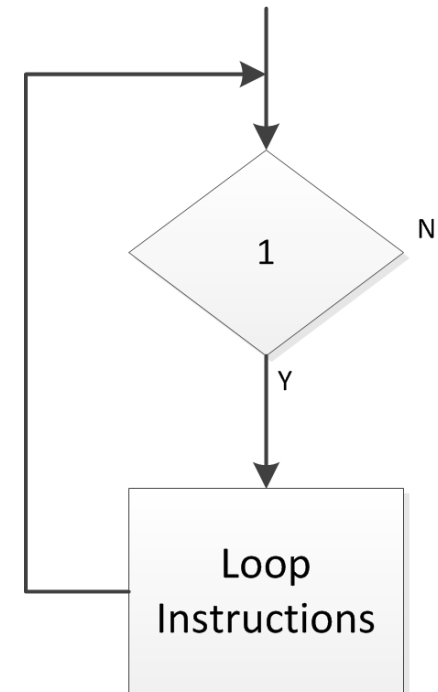
Iteration	x
0	1
1	6 3
2	8 4
3	9 4.5
4	9.5 4.75
5	9.75 4.875
6	9.875 4.9375
⋮	⋮



Infinite Loops

29

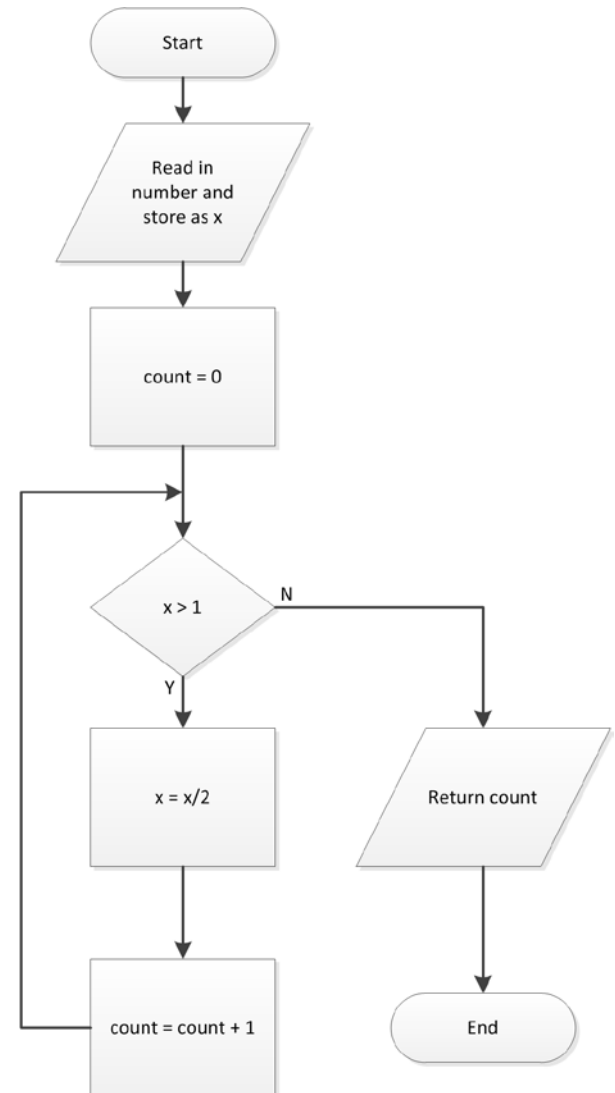
- Occasionally infinite loops are desirable
 - ▣ Consider for example microcontroller code for an environmental monitoring system
 - Continuously takes measurements and displays results while powered on
- Note the logical statement in the conditional block
 - ▣ Logical statements are either true (Y, 1) or false (N, 0)
 - ▣ 1 is the Boolean representation of true or Y



while Loop – Example 1

30

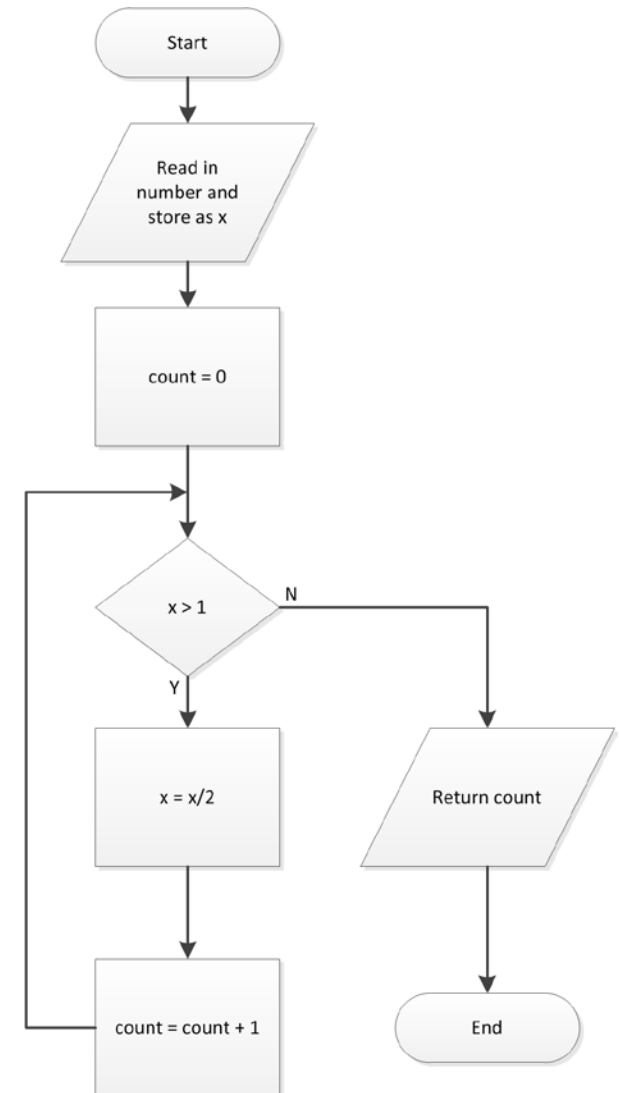
- Consider the following algorithm:
 - ▣ Read in a number (e.g. user input, from a file, etc.)
 - ▣ Determine the number of times that number can be successively divided by 2 before the result is ≤ 1
- Use a ***while loop***
 - ▣ Divide by 2 ***while*** number is > 1



while Loop – Example 1

31

- Number of loop iterations depends on value of the input variable, x
 - ▣ Characteristic of while loops
 - # of iterations unknown a priori
 - ▣ If $x \leq 1$ loop instructions never execute
- Note the data I/O blocks
 - ▣ Typical – many algorithms have *inputs* and *outputs*

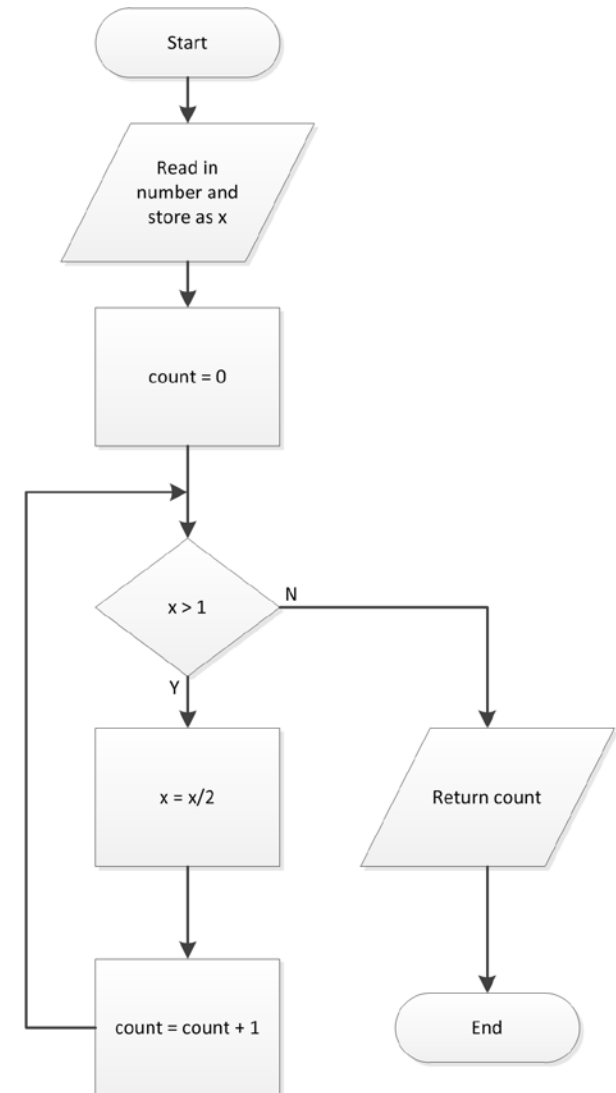


while Loop – Example 1

32

- Consider a few different input, x , values:

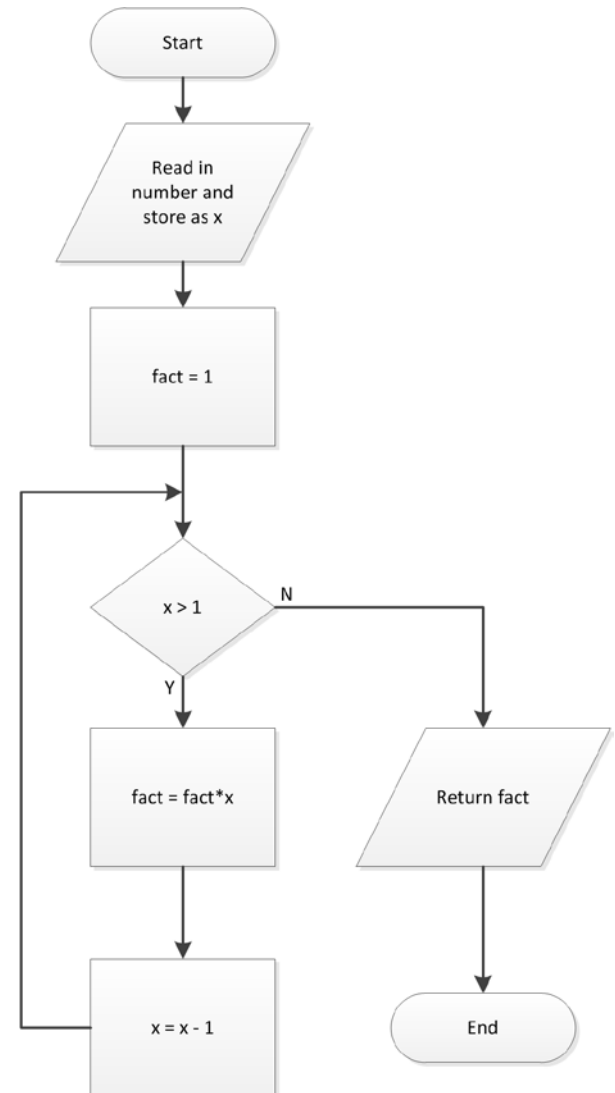
count	x		x		x
0	5		16		0.8
1	2.5		8		-
2	1.25		4		-
3	0.625		2		-
4	-		1		-
5	-		-		-



while Loop – Example 2

33

- Next, consider an algorithm to calculate $x!$, the **factorial** of x :
 - ▣ Read in a number, x
 - ▣ Compute the product of all integers between 1 and x
 - ▣ Initialize result, $fact$, to 1
 - ▣ Multiply $fact$ by x
 - ▣ Decrement x by 1
- Use a **while loop**
 - ▣ Multiply $fact$ by x , then decrement x **while** $x > 1$

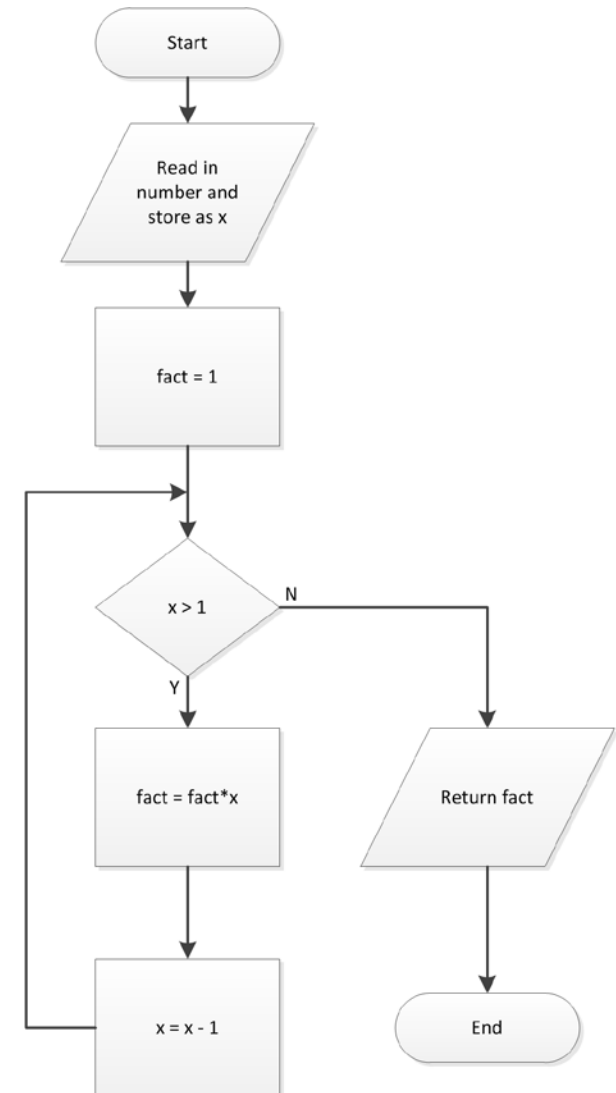


while Loop – Example 2

34

- Consider a few different input, x , values:

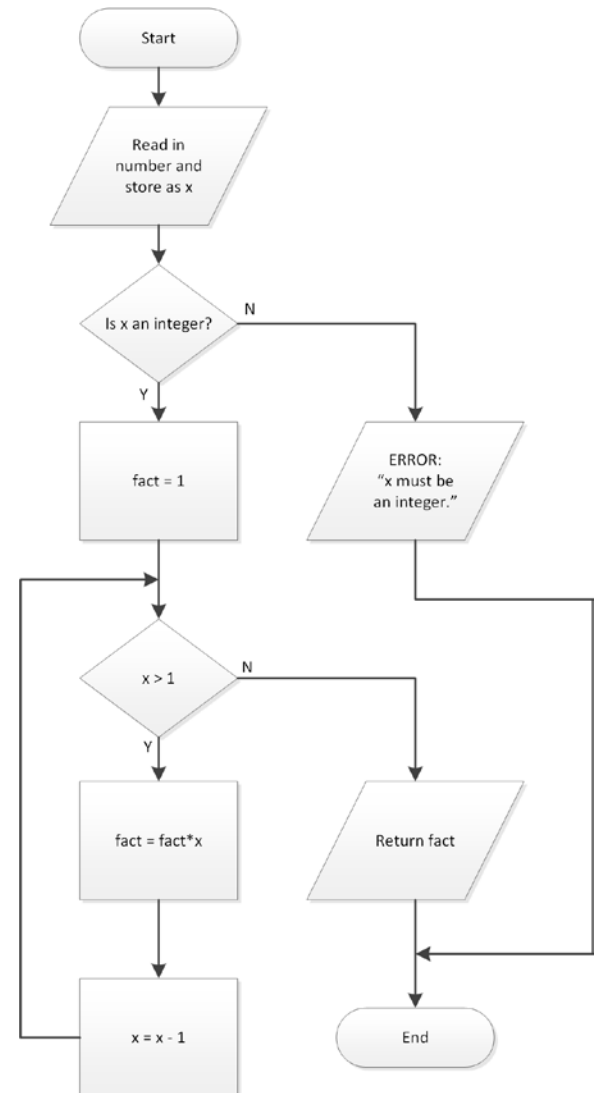
x	fact		x	fact		x	fact
5	1		4	1		0	1
5	5		4	4		-	-
4	20		3	12		-	-
3	60		2	24		-	-
2	120		1	24		-	-
1	120		-	-		-	-



while Loop – Example 2

35

- Let's say we want to define our factorial algorithm only for **integer** arguments
- Add **error checking** to the algorithm
 - ▣ After reading in a value for x , check if it is an integer
 - ▣ If not, generate an error message and exit
 - ▣ Could also imagine rounding x , generating a **warning** message and continuing



36

for Loop

for Loop

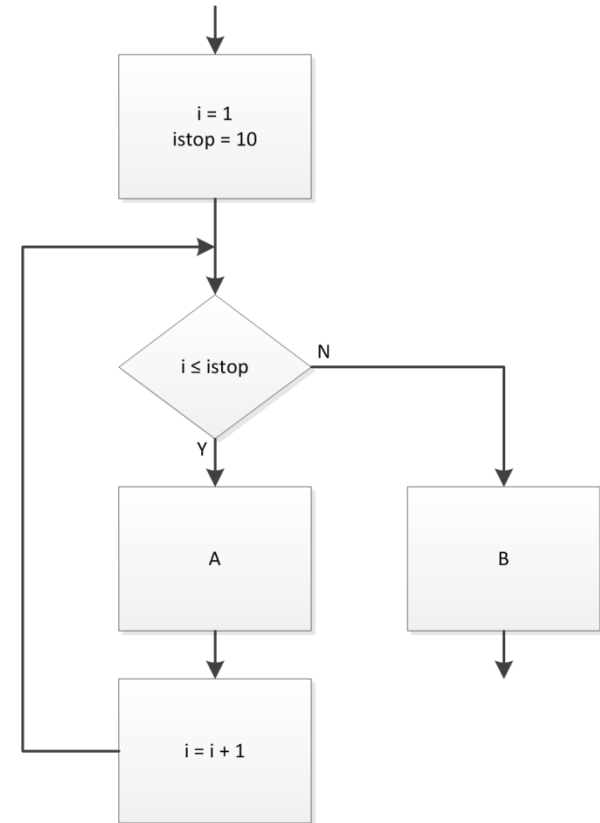
37

- We've seen that the number of while loop iterations is not known ahead of time
 - ▣ May depend on inputs, for example
- Sometimes we want a loop to execute an exact, specified number of times
- **A *for loop***
 - ▣ Utilize a ***loop counter***
 - ▣ Increment (or decrement) the counter on each iteration
 - ▣ Loop until the counter reaches a certain value
- Can be thought of as a while loop with the addition of a loop counter
 - ▣ But, a very distinct entity when implemented in code

for Loop

38

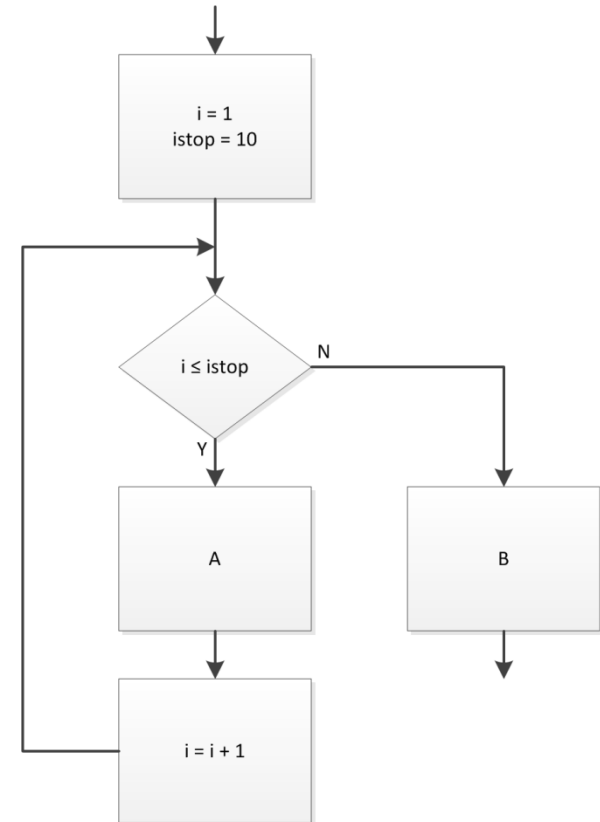
- Initialize the loop counter
 - ▣ i, j, k are common, but name does not matter
- Set the range for i
 - ▣ Not necessary to define variable $istop$
- Execute loop instructions, A
- Increment loop counter, i
- Repeat until loop counter reaches its stopping value
- Continue on to B



for Loop

39

- for loops are ***counted loops***
- Number of loop iterations is known and is constant
 - ▣ Here loop executes 10 times
- Stopping value not necessarily hard-coded
 - ▣ Could depend on an input or vector size, etc.

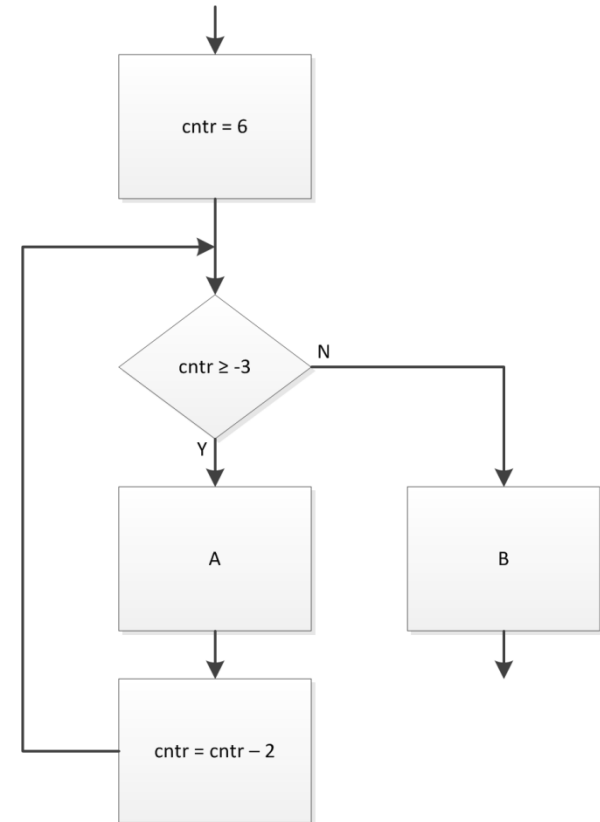


for Loop

40

- ❑ Loop counter may start at value other than 1
- ❑ Increment size may be a value other than 1
- ❑ Loop counter may count backwards

Iteration	cntr	Process
1	6	A
2	4	A
3	2	A
4	0	A
5	-2	A
6	-4	B



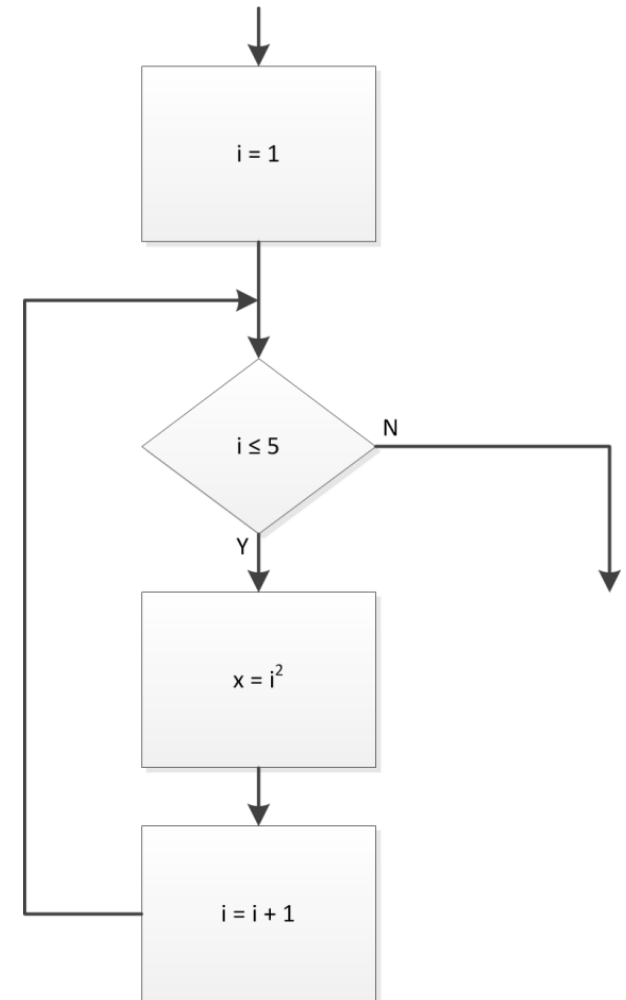
for Loop – Example 1

41

- Here, the loop counter, i , is used to update a variable, x , on each iteration

Iteration	i	x
1	1	1
2	2	4
3	3	9
4	4	16
5	5	25

- When loop terminates, and flow proceeds to the next process step, $x = 25$
 - ▣ A scalar
 - ▣ No record of previous values of x



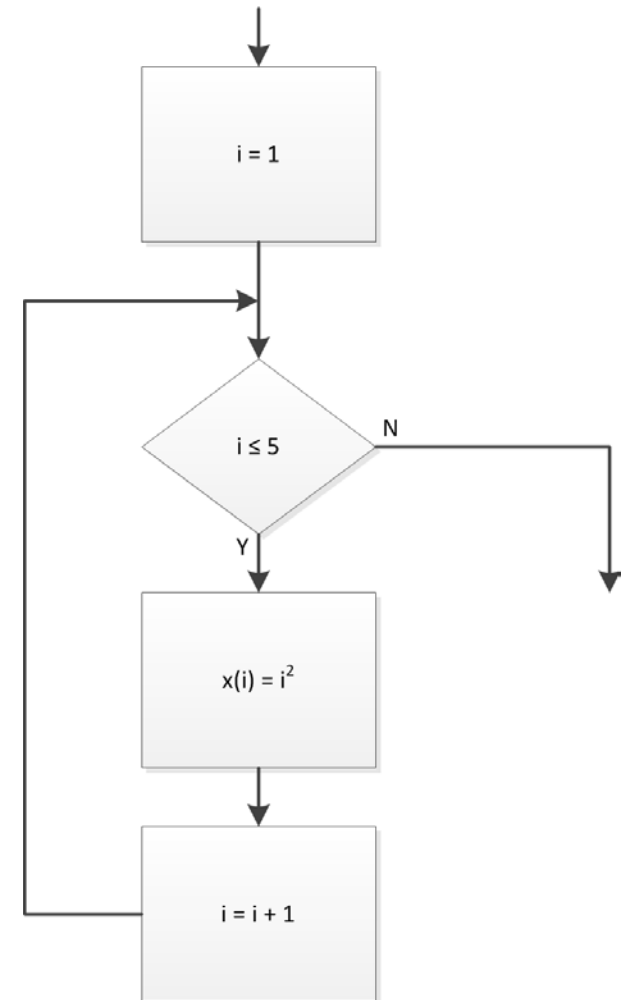
for Loop – Example 2

42

- Now, modify the loop process to store values of x as a **vector**
 - ▣ Use loop counter to index the vector

i	$x(i)$	x
1	1	[1]
2	4	[1, 4]
3	9	[1, 4, 9]
4	16	[1, 4, 9, 16]
5	25	[1, 4, 9, 16, 25]

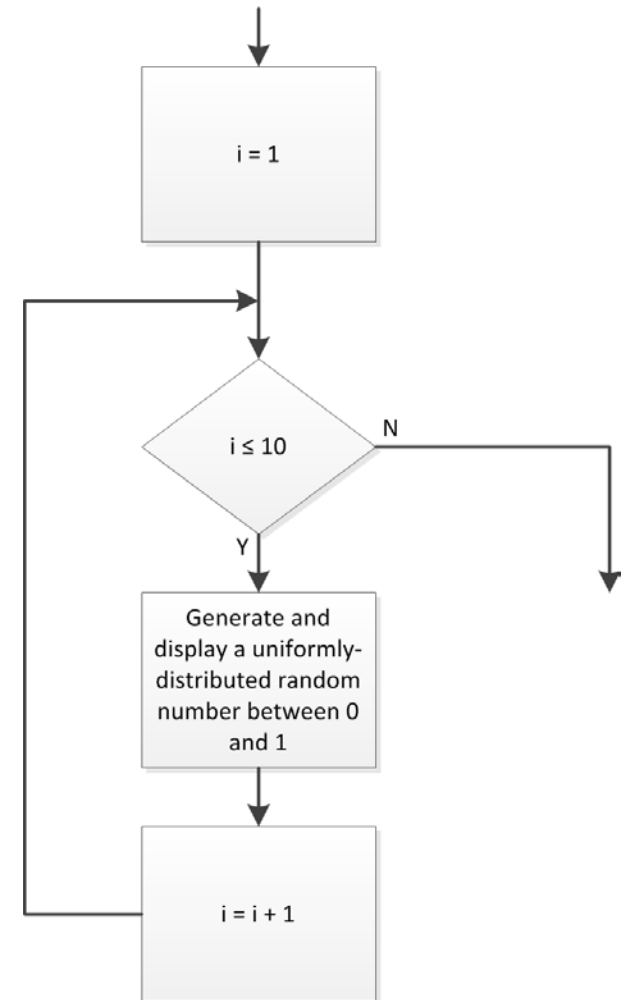
- When loop terminates, $x = [1, 4, 9, 16, 25]$
 - ▣ A **vector**
 - ▣ x grows with each iteration



for Loop – Example 3

43

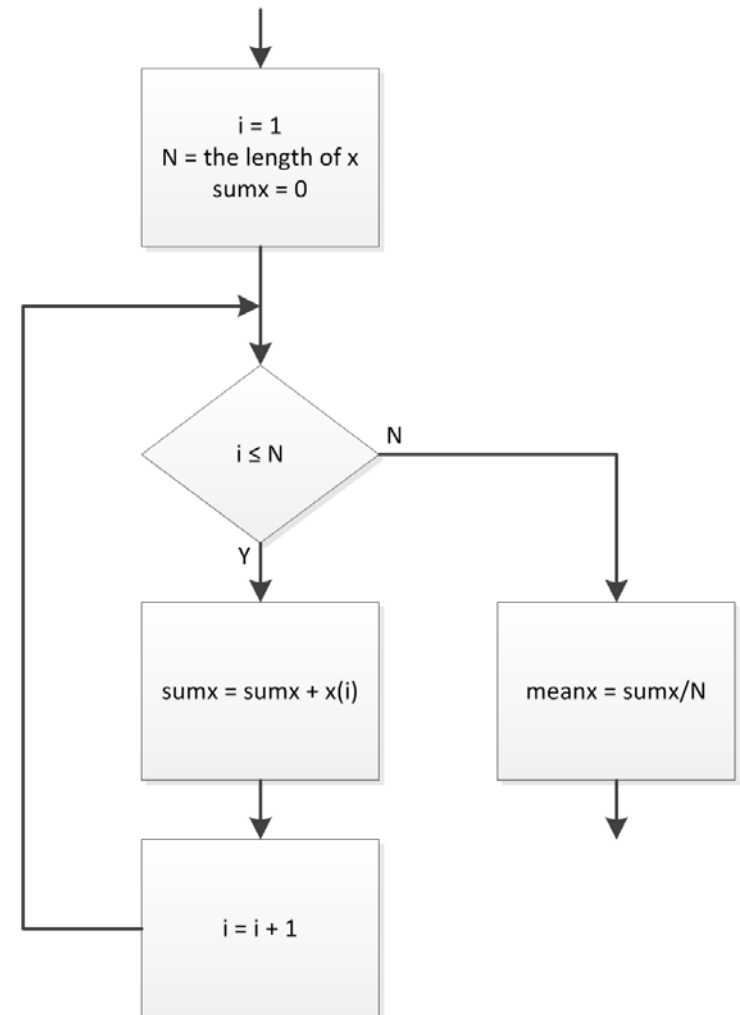
- The loop counter does not need to be used within the loop
 - ▣ Used as a counter *only*
- Here, a random number is generated and displayed each of the 10 times through the loop
 - ▣ Counter, i , has nothing to do with the values of the random numbers displayed



for Loop – Example 4

44

- Have a vector of values, x
- Find the *mean* of those values
 - ▣ Sum all values in x
 - A for loop
 - # of iterations equal to the length of x
 - Loop counter indexes x
 - ▣ Divide the sum by the number of elements in x
 - After exiting the loop



45

Nested Loops

Nested Loops

46

- A loop repeats some process some number of times
 - ▣ The repeated process can, itself, be a loop
 - ▣ A ***nested loop***
- Can have nested *for loops* or *while loops*
 - ▣ Can nest for loops within while loops and vice versa
- One application of a ***nested for loop*** is to step through every element in a matrix
 - ▣ Loop counter variables used as matrix indices
 - ▣ Outer loop steps through rows (or columns)
 - ▣ Inner loop steps through columns (or rows)

Nested for Loop – Example

47

- Recall how we index the elements within a matrix:
 - A_{ij} is the element on the i^{th} row and j^{th} column of the matrix A
 - Using MATLAB syntax: $A(i,j)$
- Consider a 3×2 matrix

$$B = \begin{bmatrix} -2 & 1 \\ 0 & 8 \\ 7 & -3 \end{bmatrix}$$

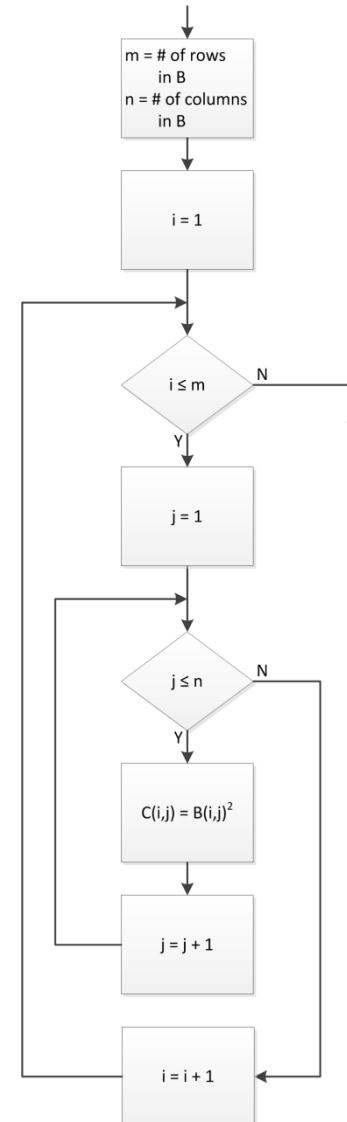
- To access every element in B :
 - start on the first row and increment through all columns
 - Increment to the second row and increment through all columns
 - Continue through all rows
 - Two nested for loops

Nested for Loop – Example

48

$$B = \begin{bmatrix} -2 & 1 \\ 0 & 8 \\ 7 & -3 \end{bmatrix}$$

- Generate a matrix C whose entries are the squares of all of the elements in B
 - ***Nested for loop***
 - Outer loop steps through rows
 - Counter is row index
 - Inner loop steps through columns
 - Counter is column index



49

Pseudocode & Top-Down Design

Pseudocode

50

- Flowcharts provide a useful tool for designing algorithms
 - ▣ Allow for describing algorithmic structure
 - ▣ Ultimately used for generation of code
 - ▣ Details neglected in favor of concise structural and functional description
- **Pseudocode** provides a similar tool
 - ▣ One step closer to actual code
 - ▣ **Textual** description of an algorithm
 - ▣ **Natural language** mixed with language-specific syntax

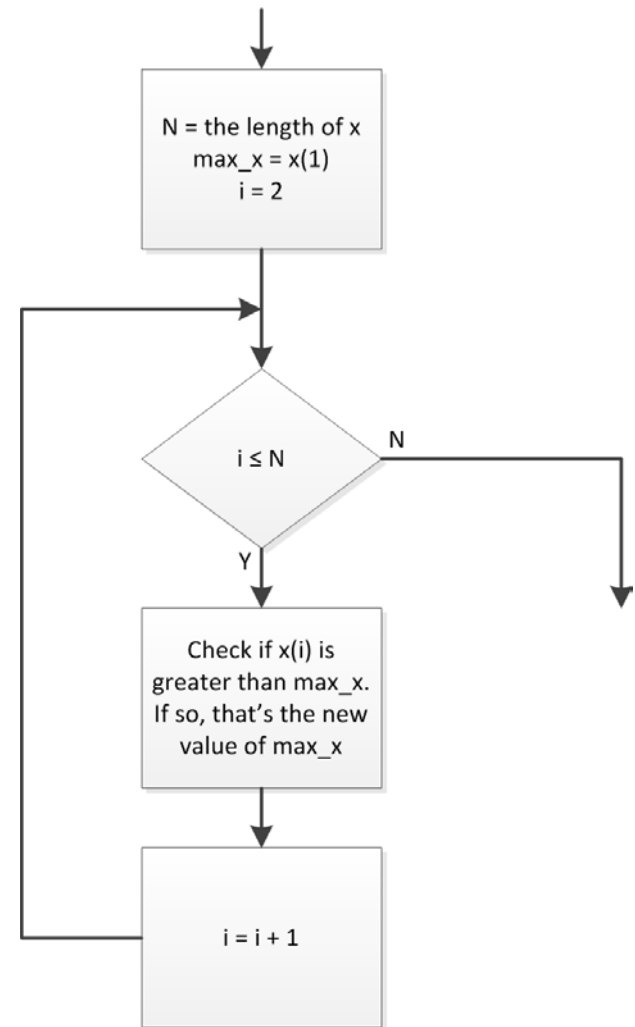
Pseudocode – Example

51

- Consider an algorithm for determining the maximum of a vector of values
- Pseudocode might look like:

```
N = length of x
max_x = x(1)
for i = 2:N
    if x(i) is greater than current
    max_x, then set max_x = x(i)
end
```

- Note the for loop syntax
 - We'll cover this in the following section of notes



Top-Down Design

52

- Flowcharts and pseudocode are useful tools for ***top-down design***
 - ▣ A good approach to any complex engineering design (and writing, as well)
 - ▣ First, define the overall system or algorithm at the top level (perhaps as a flowchart)
 - ▣ Then, fill in the details of individual functional blocks
- Top-level flowchart identifies individual functional blocks and shows how each fits into the algorithm
 - ▣ Each functional block may comprise its own flow chart or even multiple levels of flow charts
 - ▣ ***Hierarchical design***

Top-Down Design - Example

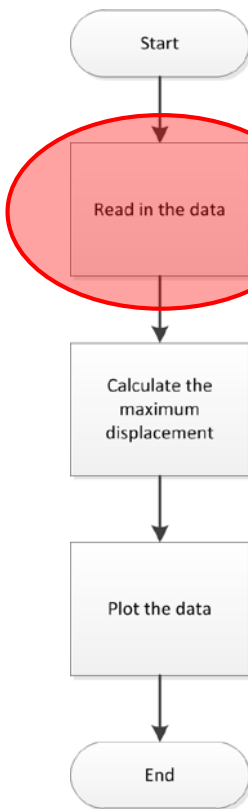
53

- Let's say you have deflection data from FEM analysis of a truss design
 - ▣ Data stored in text files
 - Deflection vs. location along truss
 - ▣ Parametric study
 - Three different component thicknesses
 - Two different materials
 - Six data sets
- Read in the data, calculate the max deflection and plot the deflection vs. position

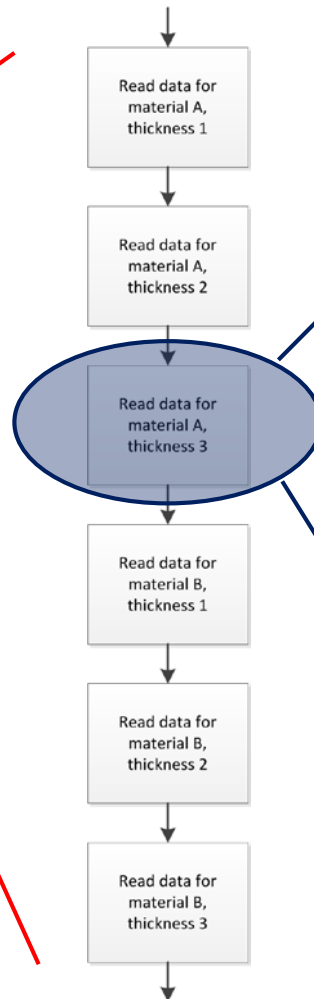
Top-Down Design - Example

54

Level 1:



Level 2:



Level 3:

