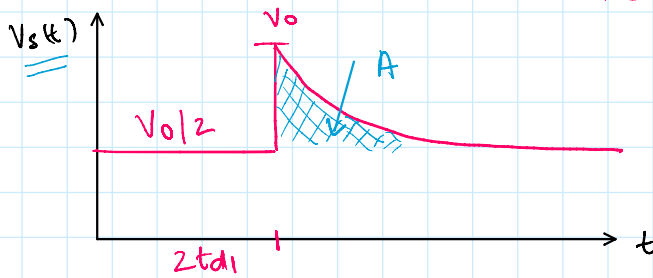
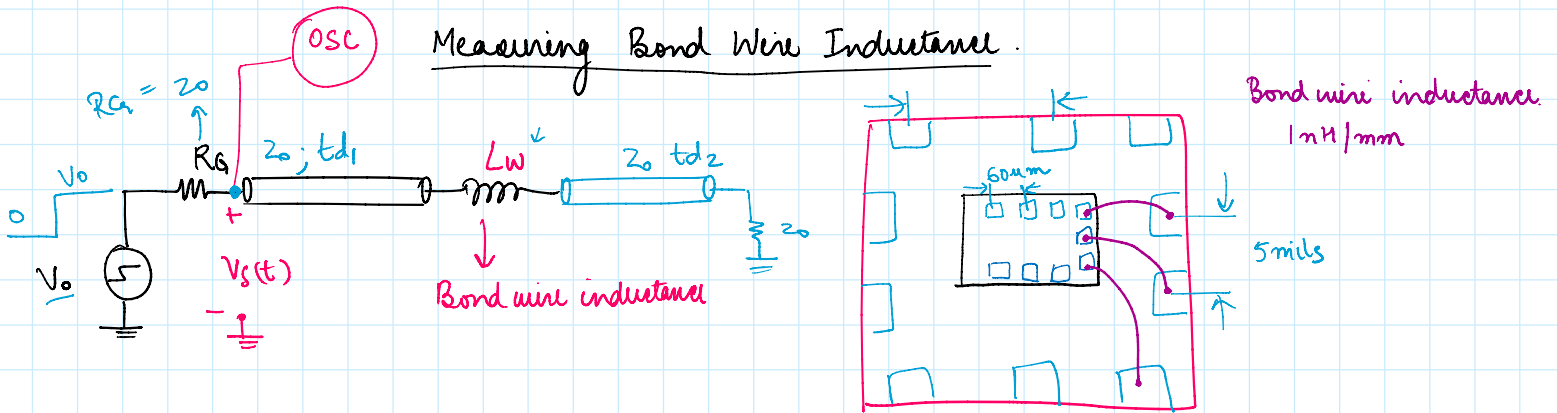


Measuring Bond Wire Inductance.



$$V_s(t) = \begin{cases} \frac{V_0}{2} & 0 < t < 2td_1 \\ \frac{V_0}{2} \left[1 + e^{-\frac{(2Z_0/L_w)(t-2td_1)}{}} \right] & t \geq 2td_1 \end{cases}$$

Area \rightarrow Integrate $\left(V_s(t) - \frac{V_0}{2} \right)$ from $t = 2td_1$ to $t = \infty$

$$A = \int_{2td_1}^{\infty} \frac{V_0}{2} e^{-\frac{(2Z_0/L_w)(t-2td_1)}{}} dt$$

$$t - 2td_1 = t'$$

$$A = \int_0^{\infty} \frac{V_0}{2} e^{-\frac{(2Z_0/L_w)t'}{}} dt'$$

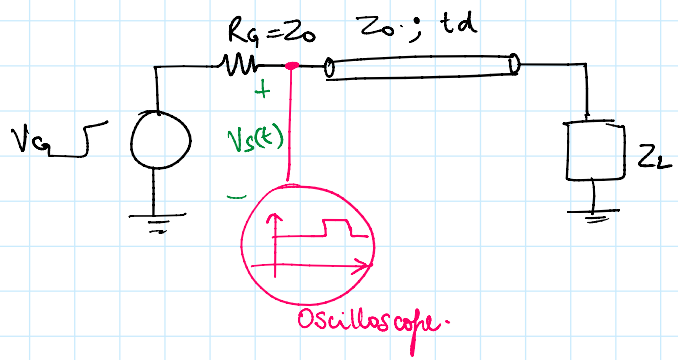
$$A = L_w \cdot \frac{V_0}{4Z_0}$$

$$L_w = \frac{A \cdot 4z_0}{V_0}$$

Time Domain Reflectometry (TDR)

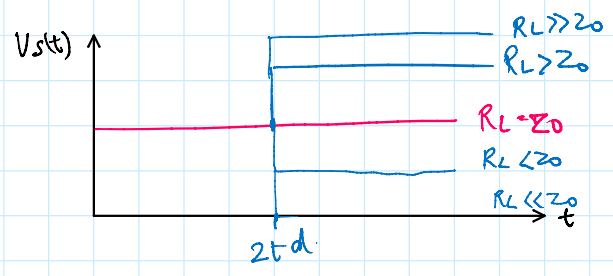
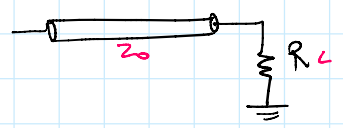
1. Measure unknown characteristic impedance.
2. Understand the nature of termination load.
3. Detect the presence of discontinuity on a transmission line.

TDR instrument : • Step pulse source with sharp rise time $t_r < 50ps$
 • Oscilloscope.

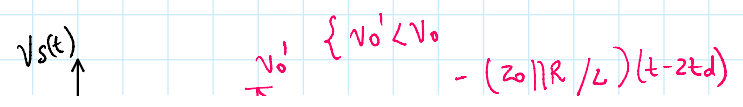
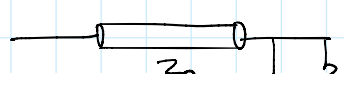
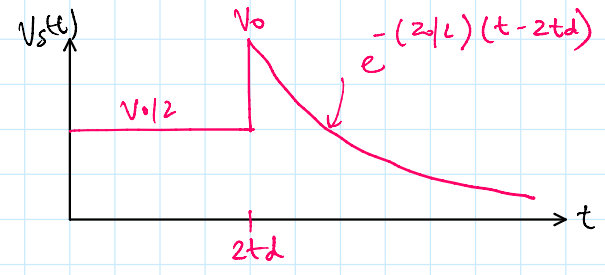
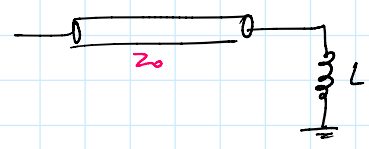


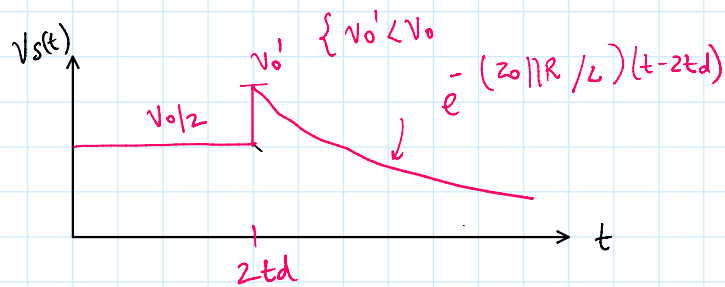
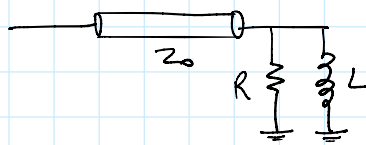
Termination Types:

1. Resistive Termination



2. Inductive Termination



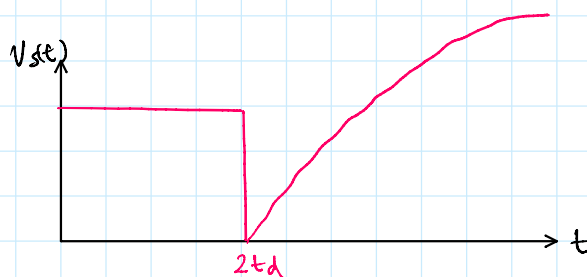
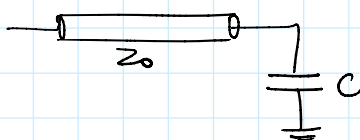


$$V_0' > \frac{V_0}{2} \quad \text{if } R > Z_0$$

$$V_0' < \frac{V_0}{2} \quad \text{if } R < Z_0$$

$$V_0' = \frac{V_0}{2} \quad \text{if } R = Z_0$$

3. Capacitive Termination



Waveforms are TDR signatures

(Fig 2.34 in the text book)

Transmission Lines with Sinusoidal Excitation

Loss-Less Transmission Line $\rightarrow \alpha = 0$
 $\gamma = j\beta$

Voltage : $V(z) = V^+ e^{j\beta z} + V^- e^{-j\beta z}$

$$V(z) = V^+ e^{j\beta z} \left[1 + \frac{V^-}{V^+} e^{-2j\beta z} \right]$$

$$V(z) = V^+ e^{j\beta z} \left[1 + \Gamma_L e^{-2j\beta z} \right] \rightarrow \text{Standing voltage expression}$$

Current : $I(z) = \frac{V^+}{Z_0} e^{j\beta z} - \frac{V^-}{Z_0} e^{-j\beta z}$

Notice!

Current : $I(l) = \frac{V^+}{Z_0} e^{j\beta l} - \frac{V^-}{Z_0} e^{-j\beta l}$

Notice!

$$I(l) = \frac{V^+ e^{j\beta l}}{Z_0} \left\{ 1 - \Gamma_L e^{-2j\beta l} \right\}$$

$$\frac{Z_L - Z_0}{Z_L + Z_0}$$

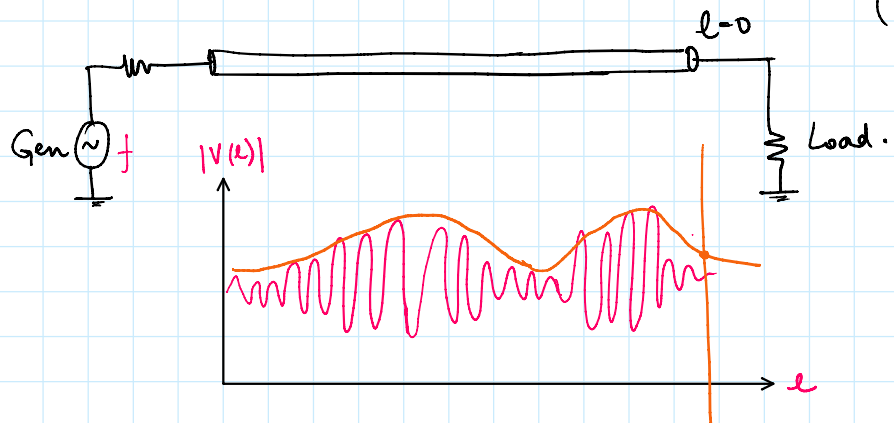
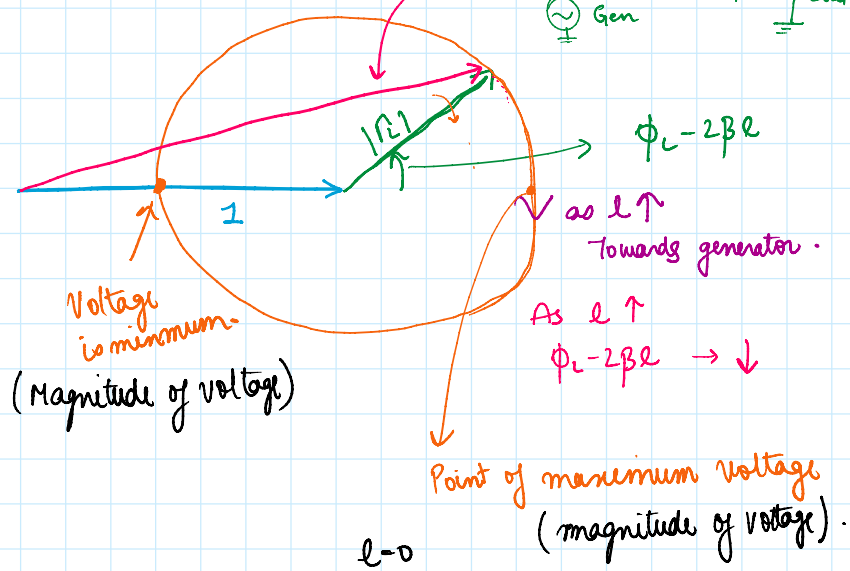
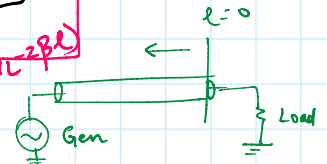
$$\Gamma_L = |\Gamma_L| e^{j\phi_L}$$

↓
complex quantity

$$V(l) = \frac{V^+ e^{j\beta l}}{Z_0} \left[1 + |\Gamma_L| e^{j(\phi_L - 2\beta l)} \right]$$

$$I(l) = \frac{V^+ e^{j\beta l}}{Z_0} \left[1 - |\Gamma_L| e^{j(\phi_L - 2\beta l)} \right]$$

Phasor Notation



Observations :

1. Maximum of voltage & current do not happen at the same point in a transmission line.
2. Point of max $V(l)$ is the point of min $I(l)$ & vice-versa.

