

Smith Chart-4

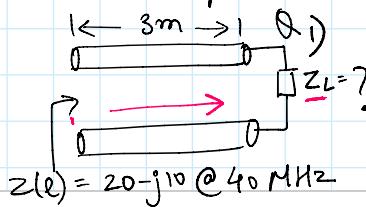
Friday, May 22, 2020 8:21 AM

Example 3:

$$Z_0 = 50 \Omega$$

$$\epsilon_r = 2.25$$

$l = 3m$ (length of the transmission line)



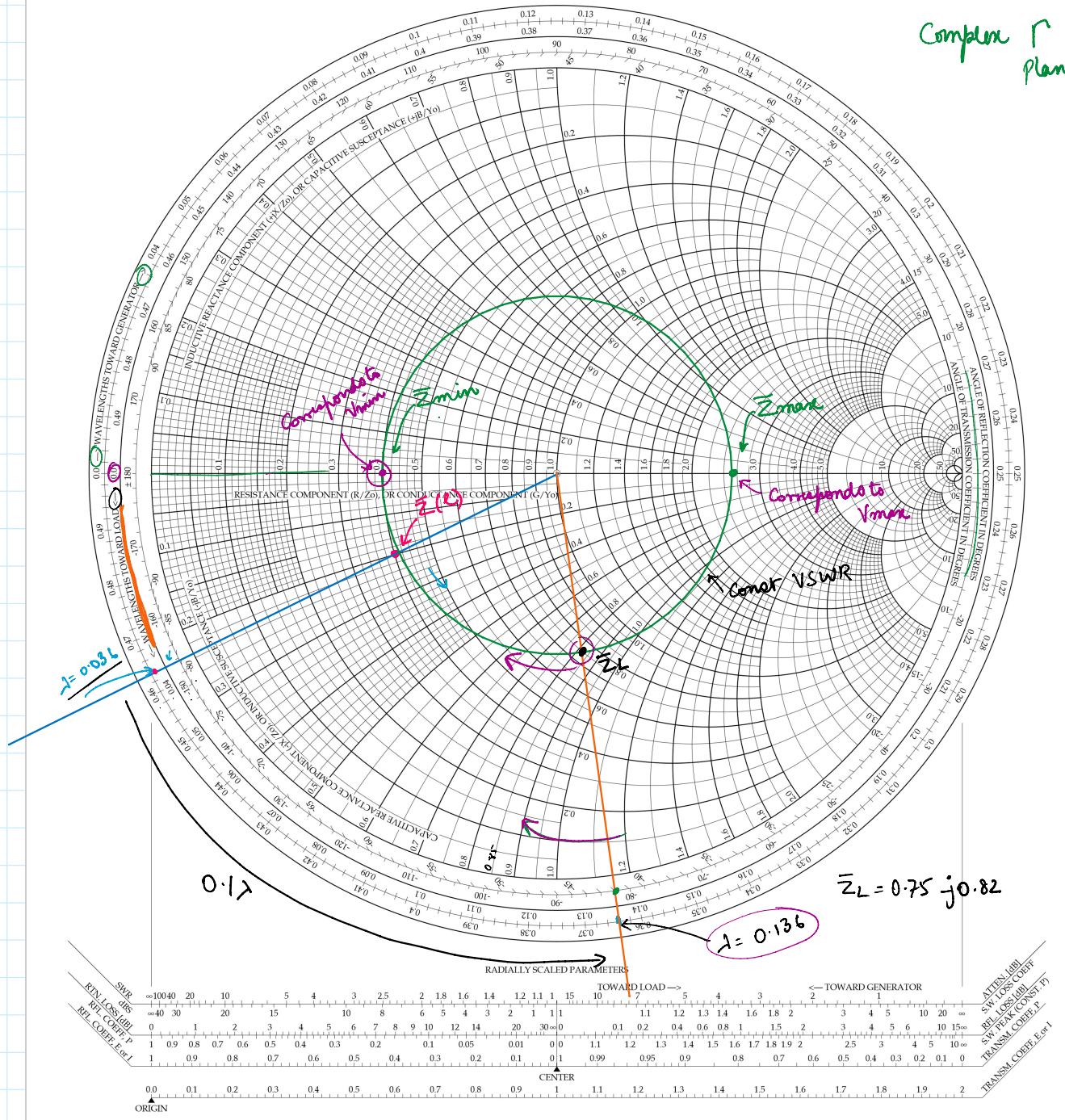
Given

Q 2) Find the position of V_{min} in meters from the load.

$$Z(l) = 20 - j10 \Omega \text{ @ } 40 \text{ MHz}$$

Smith Chart

Complex Γ plane



Step 1: Normalize $Z(l)$ $\bar{Z}(l) = \frac{20-j10}{50} = 0.4-j0.2$

Step 2: Calculate λ (wavelength).

$$\lambda = \frac{c}{f} = \frac{3 \times 10^8 \text{ m/s}}{\sqrt{6}\sqrt{40} \times 10^6} = 5 \text{ m}$$

Electrical length of the transmission line (in λ) = $\frac{3\text{m}}{5\text{m}} = 0.6\lambda$

Step 3: Go counterclockwise on constant VSWR circle by 0.6λ

$$\underline{0.6\lambda} = \underbrace{0.5\lambda}_{2\pi \text{ rotation}} + \underline{0.1\lambda}$$

$$2\beta l = 2\pi$$

$$2 \frac{2\pi}{\lambda} l = 2\pi$$

$$l = \lambda/2$$

Step 4: Draw a line-B from centre to 0.136λ

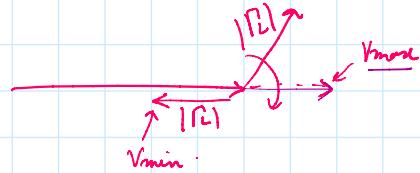
Step 5: Observe the intersection of line-B & VSWR circle as \bar{Z}_L

Step 6: $Z_L = 50(0.75-j0.82) = 37.5-j41 \Omega$

(b) Minimum voltage location from the load.

$$V_{\min} = V^+ (1 - |F_L|)$$

$$V_{\max} = V^+ (1 + |F_L|)$$



Step 7: Measure distance between \bar{Z}_L & V_{\min} pt in terms of λ

Distance = 0.136λ

Distance = $5\text{m} \times 0.136 = 0.68 \text{ m}$ from the load.