

**ECE 580 Network Theory, Fall 2016**

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**Test Date: 10/31/2016**

**Problems: 3**

**Total Pages: 6**

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**Name:** \_\_\_\_\_

**Secret Code (5 Digit):** \_\_\_\_\_

**1. (15 points)** \_\_\_\_\_

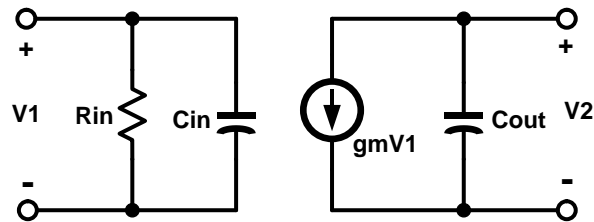
**2. (15 points)** \_\_\_\_\_

**3. (5 points)** \_\_\_\_\_

**Total (35 points)** \_\_\_\_\_

**Good Luck**

**Problem 1: (15 points)** Estimate the H parameters for the circuit shown below.



$$V_1 = h_{11} I_1 + h_{12} V_2$$

$$I_2 = h_{21} I_1 + h_{22} V_2$$

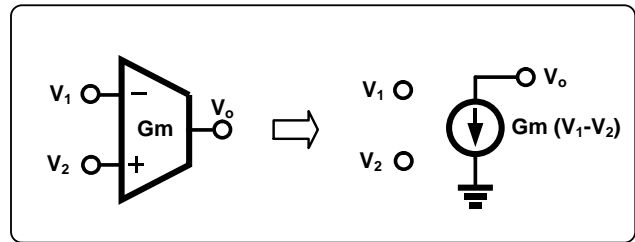
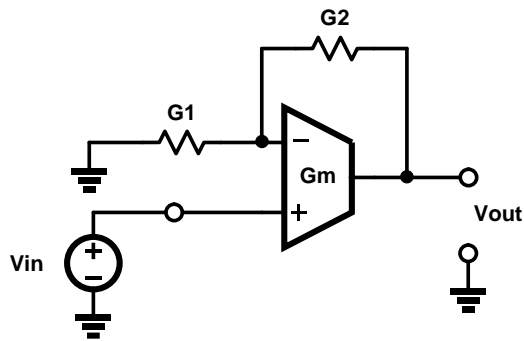
$$h_{11} = \frac{R_{in}}{1 + s R_{in} C_{in}}$$

$$h_{21} = \frac{g_m R_{in}}{1 + s C_{in} R_{in}}$$

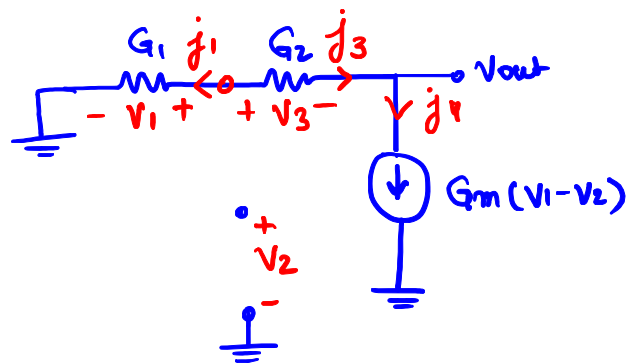
$$h_{12} = 0$$

$$h_{22} = s C_{out}$$

**Problem 2: (15 points)** Calculate the sensitivity of  $V_{out}$  to network parameters:  $G_1$  and  $G_2$  using the adjoint network concept.

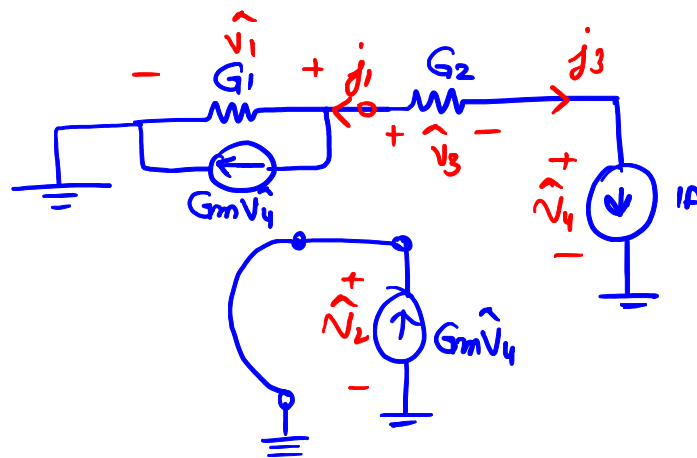


Network  $N$ :



$$G = \begin{bmatrix} G_1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & G_2 & 0 \\ G_m & -G_m & 0 & 0 \end{bmatrix}; \quad \hat{G} = G^T$$

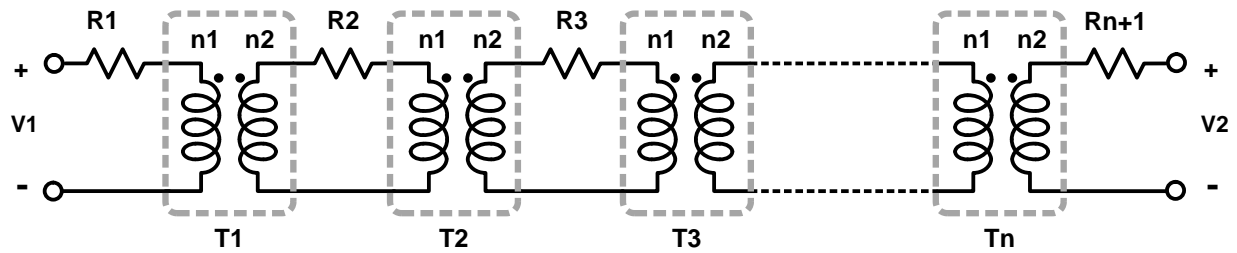
Network  $\hat{N}$ :



$$\frac{\partial V_{out}}{\partial G_1} = \hat{V}_1 V_1 = \frac{V_{in} G_m (G_m - G_2)}{G_2 (G_m + G_1)^2}$$

$$\frac{\partial V_{out}}{\partial G_2} = \hat{V}_3 V_3 = \frac{-V_{in} G_m G_1}{G_2^2 (G_m + G_1)}$$

**Problem 3: (5 points)** Calculate  $Y_{11}$  for the network shown below:



For  $Y_{11}$  Set  $V_2 = 0$

$$Y_{11} = \frac{1}{R_1 + \left(\frac{n_1}{n_2}\right)^2 \left( R_2 + \left(\frac{n_1}{n_2}\right)^2 \left( R_3 + \dots + \left(\frac{n_1}{n_2}\right)^2 \left( R_n + \left(\frac{n_1}{n_2}\right)^2 R_{n+1} \right) \right) \right)}$$

$$Y_{11} = \frac{1}{R_1 + \left(\frac{n_1}{n_2}\right)^2 R_2 + \left(\frac{n_1}{n_2}\right)^4 R_3 + \dots + \left(\frac{n_1}{n_2}\right)^{2n} R_{n+1}}$$

**Supplementary page:**