DP Practice Questions

1. Modify the dynamic program for the knapsack problem to find a set of items of maximum value whose total weight is exactly the capacity of the knapsack. Note that for a given set of items, there may not be a subset of items whose total weight is exactly the capacity of the knapsack; in this case, your algorithm should correctly say there is no solution.

You should:

(a) Define the dynamic programming table.
(b) Give a recursive formula for an entry in the dynamic programming table.
(c) Describe in words how to fill the dynamic programming table.
(d) Give pseudocode for the final algorithm including how to find and return the items in the knapsack.

2. Give an $O(nt)$ dynamic programming algorithm for the following task:

   Input: A list of $n$ positive integers $a_1, a_2, \ldots, a_n$ and a positive integer $K$. Question: Does some subset of the $a_i$’s add up to $K$? (You can use each $a_i$ at most once.)

You should:

(a) Define the dynamic programming table.
(b) Give a recursive formula for an entry in the dynamic programming table.
(c) Describe in words how to fill the dynamic programming table.
(d) Give pseudocode for the final algorithm.
(e) Give the running time of your algorithm.