

Forest Reranking

Discriminative Parsing with Non-Local Features



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University of Pennsylvania



ACL 2008 talk, Columbus, OH, June 2008

Is Supervised Parsing Done?

is it a done area?

Bod (2007)

**Is the End of Supervised
Parsing in Sight?**

Is Supervised Parsing Done?

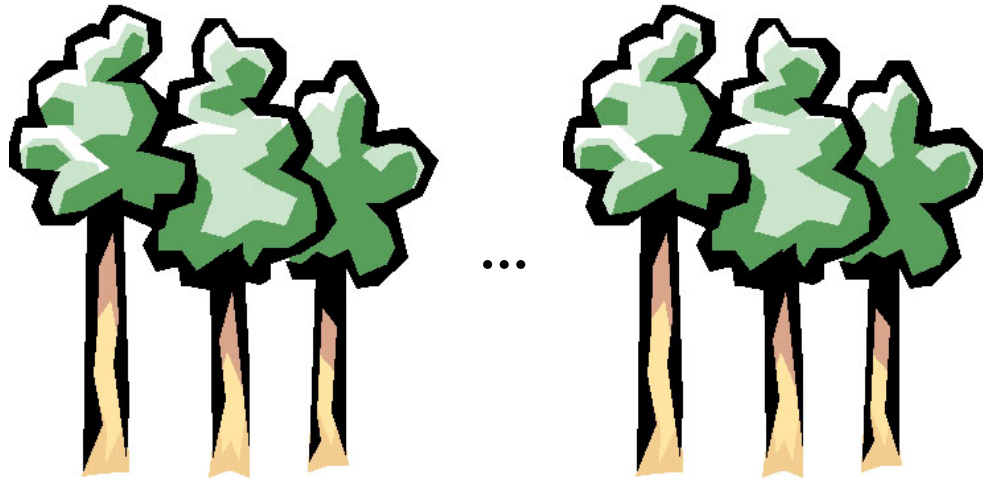
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**Is the End of Supervised
Parsing in Sight?**

- motivation: use **non-local** features
 - linguistically-motivated features for n -best reranking
(Charniak and Johnson, 2005; Collins, 2000)
 - but can we integrate them back into **chart parsing**?
 - YES: using a **packed forest**!
- result: best whole Treebank parsing accuracy to date

Why is *n*-best list a bad idea?



- too few variations (limited scope)
 - 41% correct parses are not in ~30-best (Collins, 2000)
 - worse for longer sentences; tiny fraction of whole space
- too many redundancies
 - 50-best usually encodes 5-6 binary decisions ($2^5 < 50 < 2^6$)

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packed forest



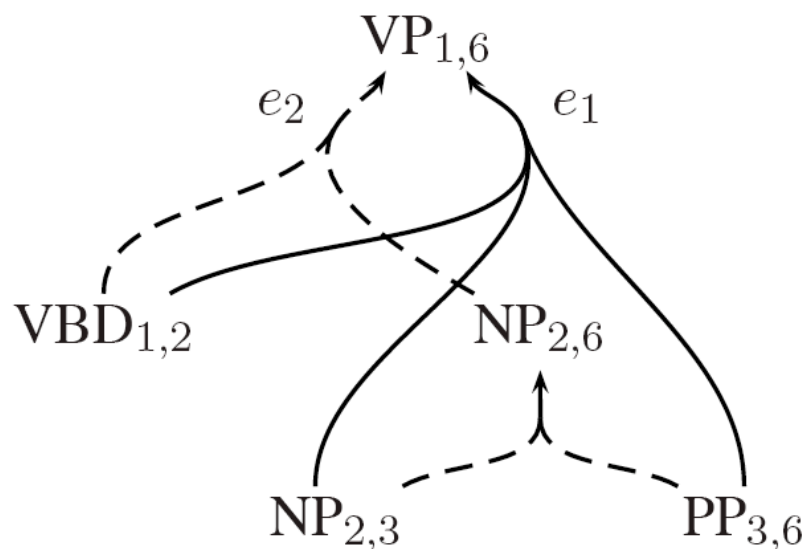
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Outline

- Packed Forest and General Idea
- Forest Reranking and Non-Local Features
 - Perceptron for Generic Reranking
 - Local vs. Non-Local Features
 - Incremental Computation of Non-Local Features
- Decoding Algorithm
- Experiments

Packed Forest

- a compact representation of many parses
- by sharing common sub-derivations
- polynomial-space encoding of exponentially large set

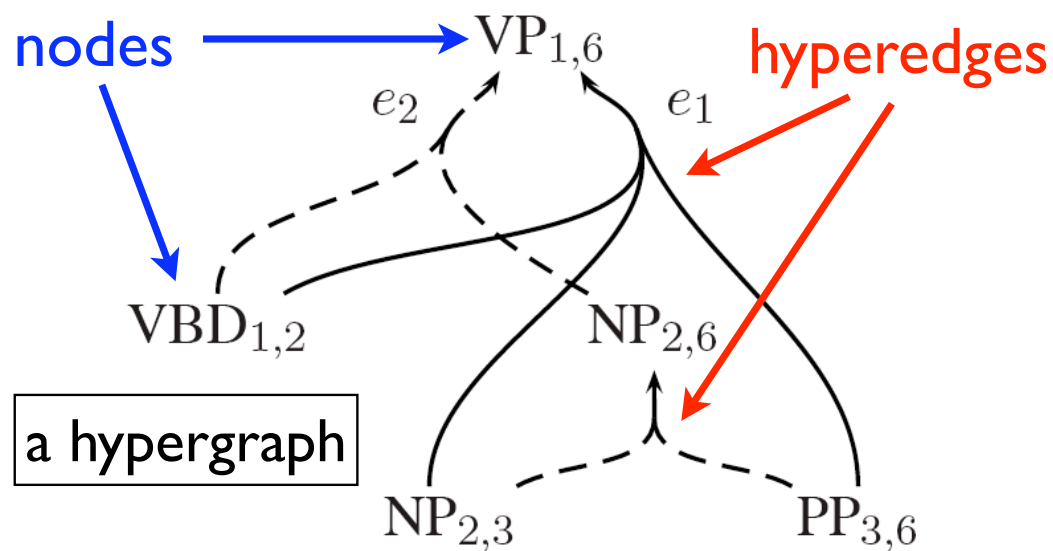


0 I 1 saw 2 him 3 with 4 a 5 mirror 6

(Klein and Manning, 2001; Huang and Chiang, 2005)

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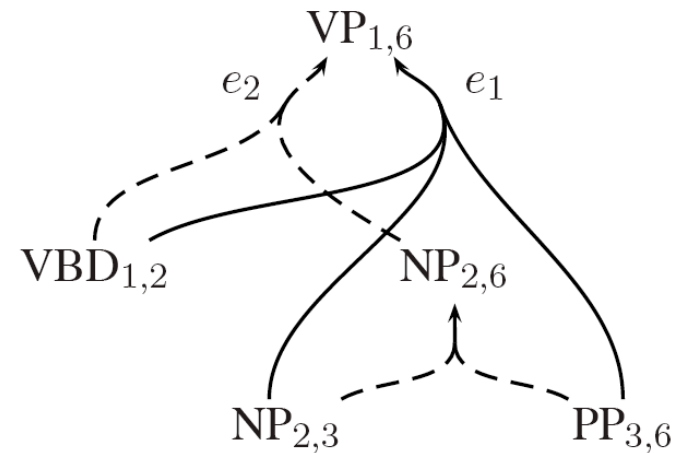
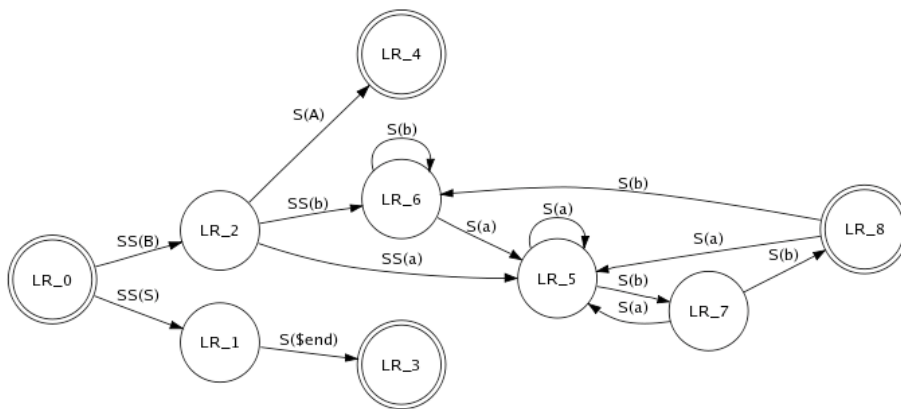


$$e_1 \frac{VBD_{1,2} \quad NP_{2,3} \quad PP_{3,6}}{VP_{1,6}}$$

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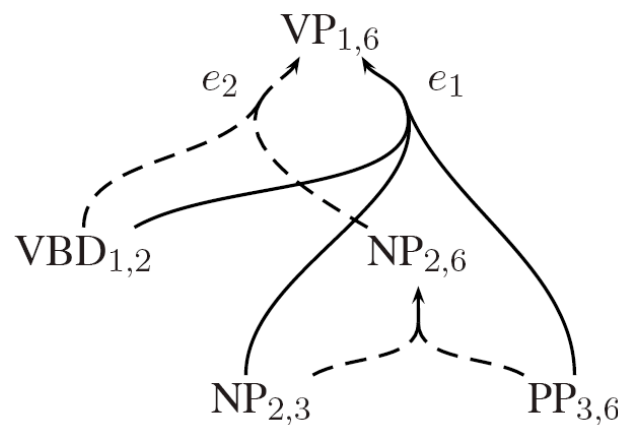
Lattices vs. Forests

- forest generalizes “lattice” from finite-state world
- both are compact encodings of exponentially many derivations (paths or trees)
- graph \Rightarrow hypergraph; regular grammar \Rightarrow CFG



Reranking on a Forest?

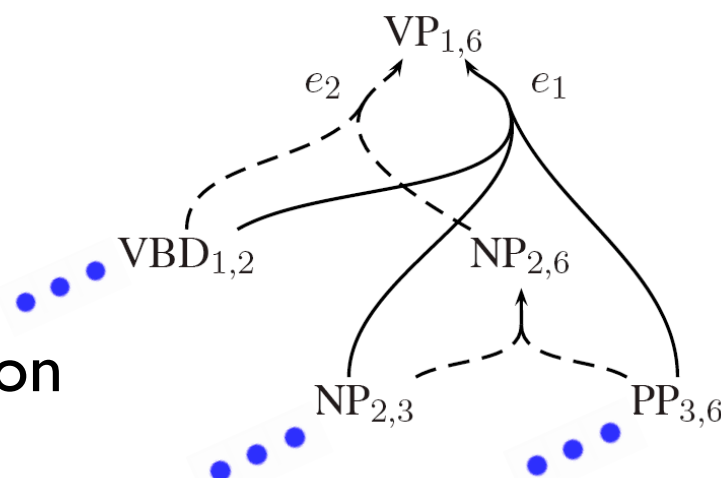
- with only local features
 - dynamic programming, tractable
(Taskar et al. 2004; McDonald et al., 2005)
- with non-local features
 - intractable, so we do approximation
 - on-the-fly reranking at internal
 - use non-locals as early and as much as possible!



<i>methods \ features</i>	<i>local</i>	<i>non-local</i>
<i>n</i> -best reranking	only at the root node	
DP-based discrim. parsing	exact	N/A
forest reranking	exact	on-the-fly

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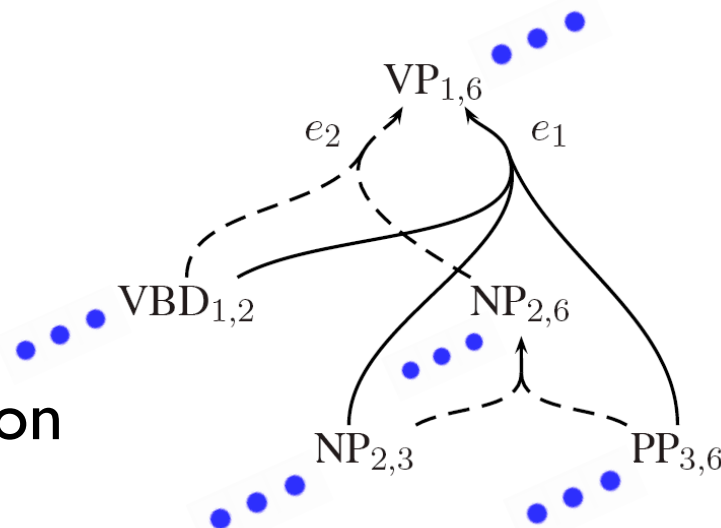
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Generic Reranking by Perceptron

- for each sentence s_i , we have a set of candidates $cand(s_i)$
- and an **oracle** tree y_i^+ , among the candidates
- a feature mapping from tree y to vector $\mathbf{f}(y)$

1: **Input:** Training examples $\{cand(s_i), y_i^+\}_{i=1}^N$

2: $\mathbf{w} \leftarrow \mathbf{0}$

▷ initial weights

3: **for** $t \leftarrow 1 \dots T$ **do**

▷ T iterations

4: **for** $i \leftarrow 1 \dots N$ **do**

5: $\hat{y} = \operatorname{argmax}_{y \in cand(s_i)} \mathbf{w} \cdot \mathbf{f}(y)$

6: **if** $\hat{y} \neq y_i^+$ **then**

7: $\mathbf{w} \leftarrow \mathbf{w} + \mathbf{f}(y_i^+) - \mathbf{f}(\hat{y})$

8: **return** \mathbf{w}

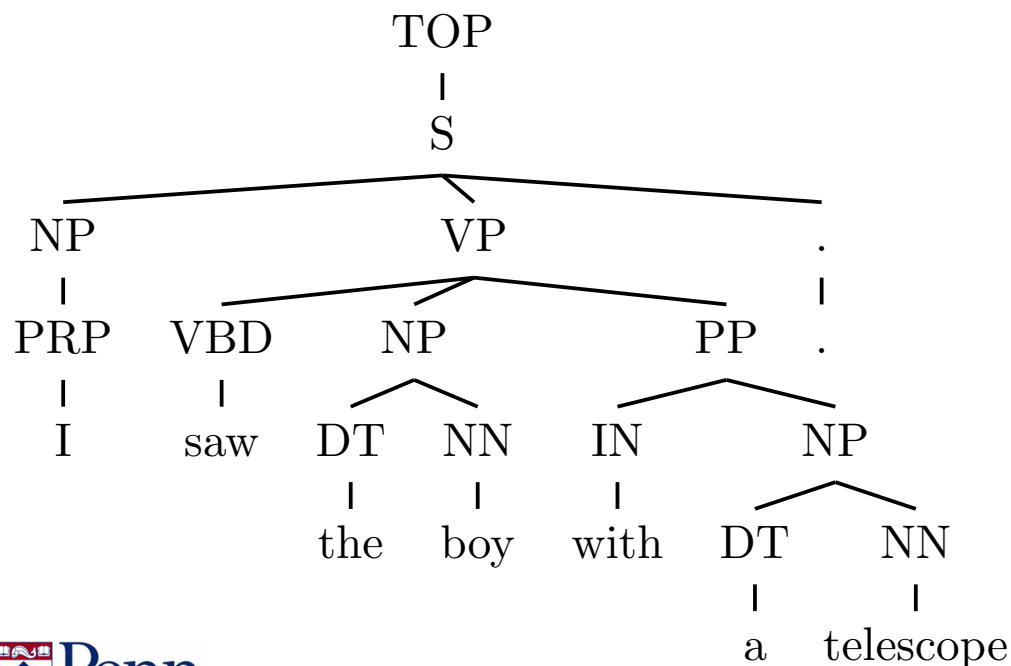
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Features

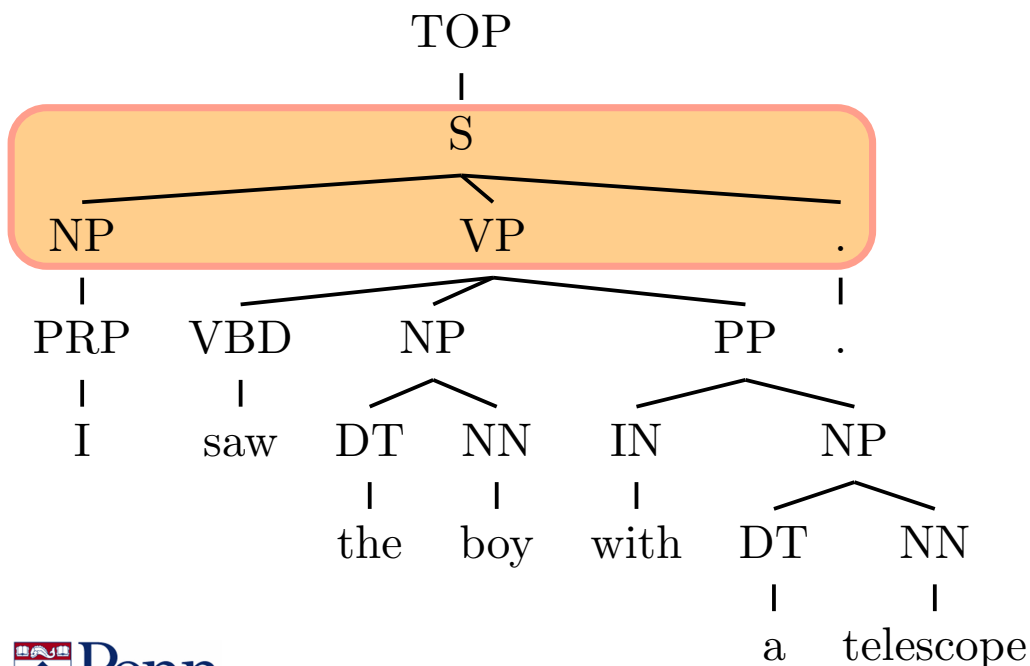
- a feature f is a function from tree y to a real number
- $f_1(y) = \log \text{Pr}(y)$ is the log Prob from generative parser
- every other feature *counts* the number of times a particular configuration occurs in y



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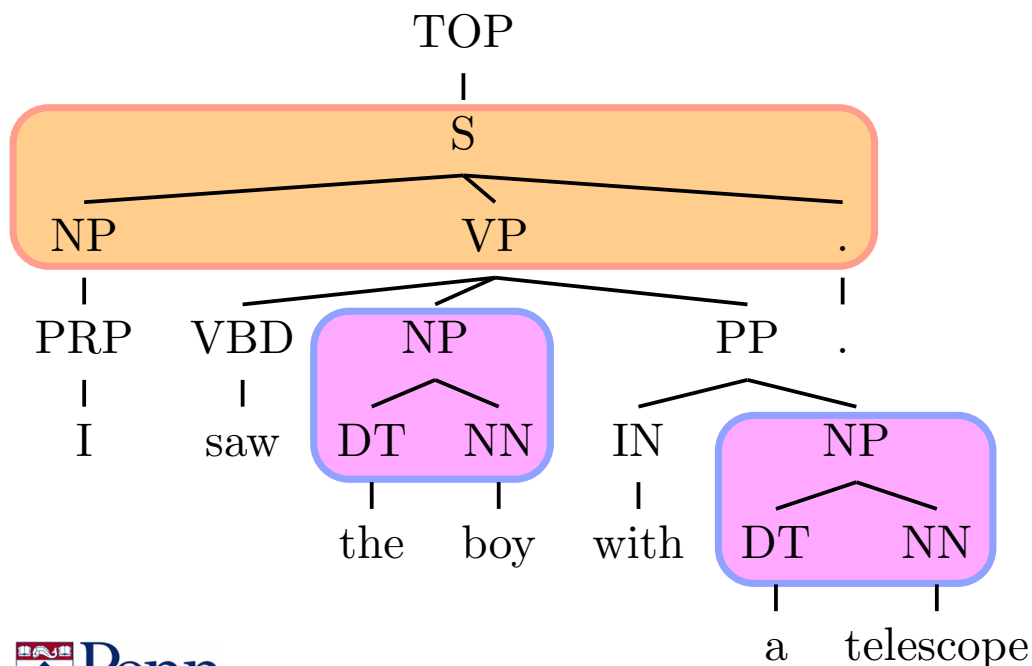
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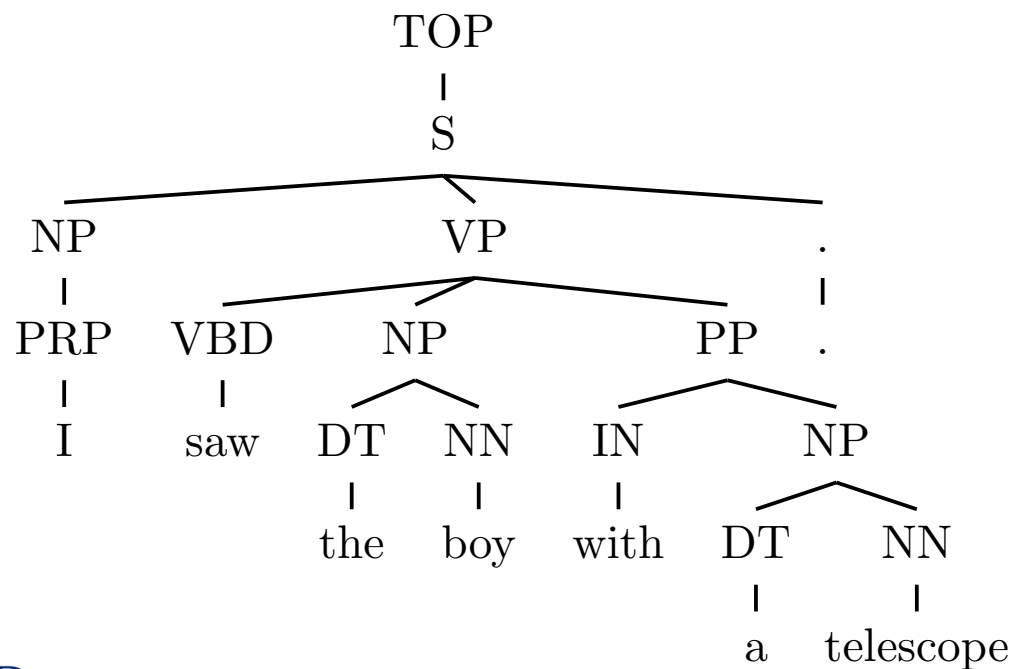
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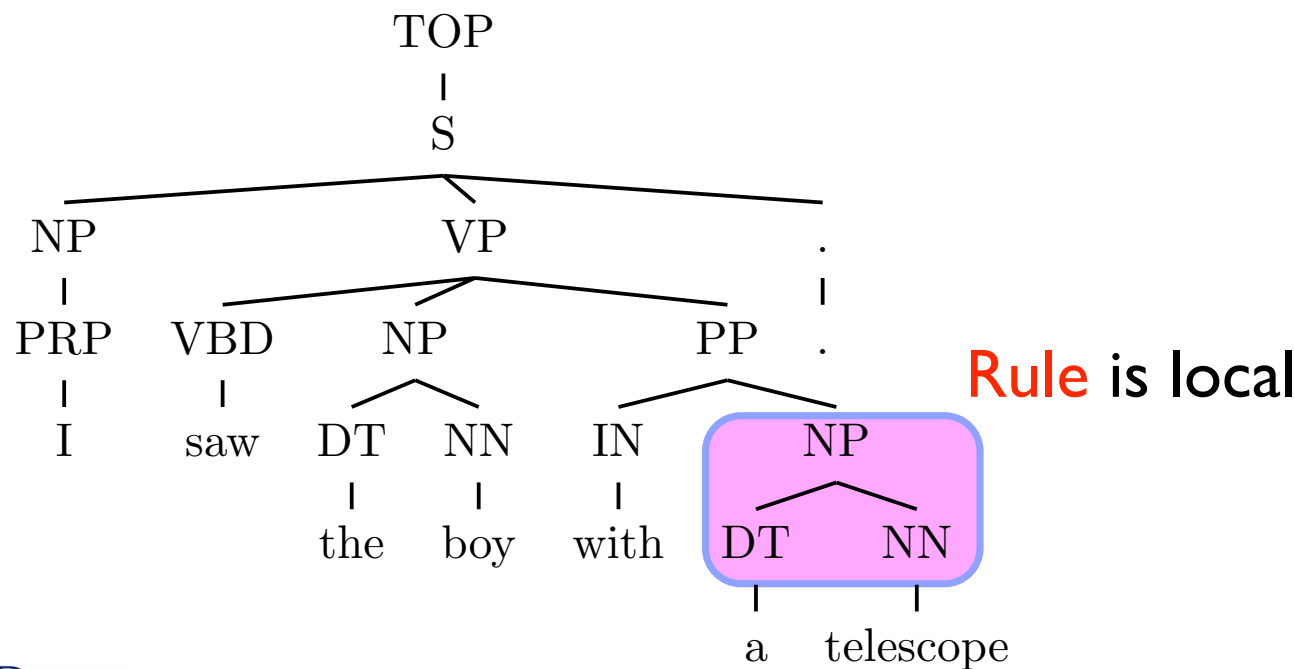
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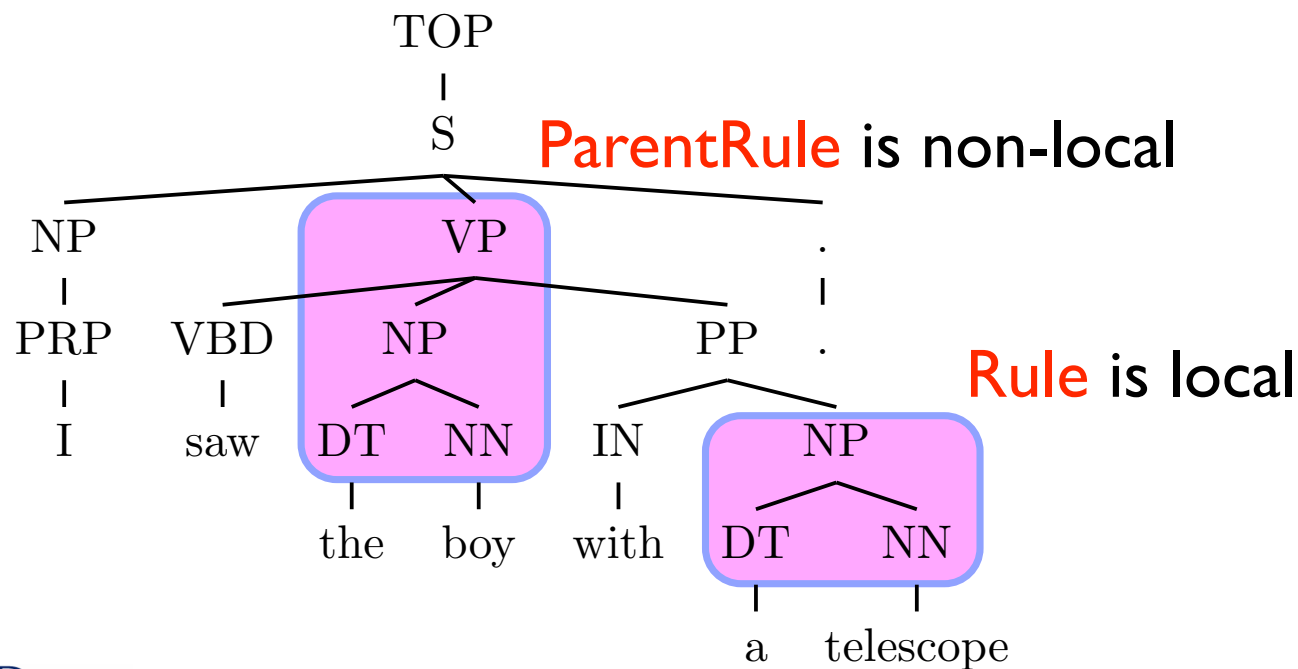
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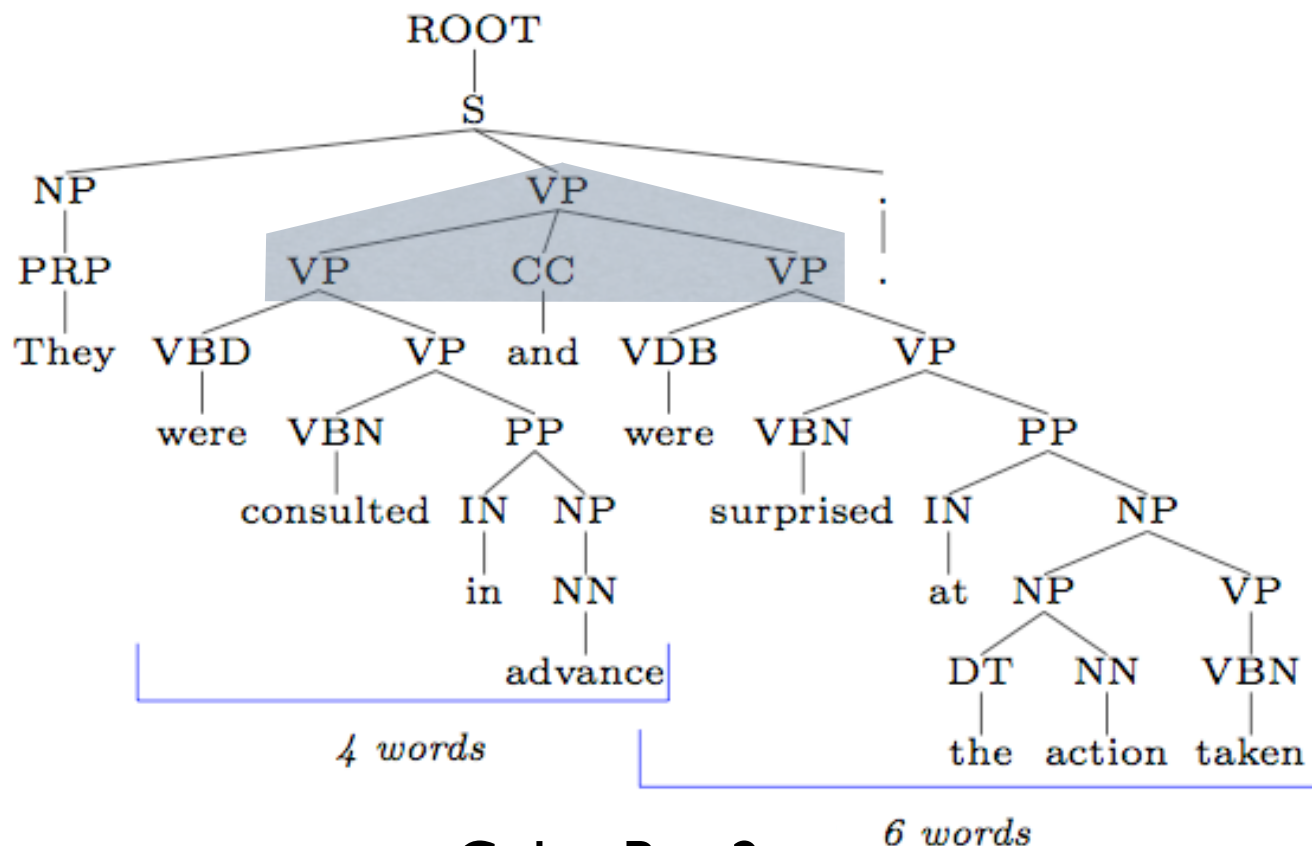
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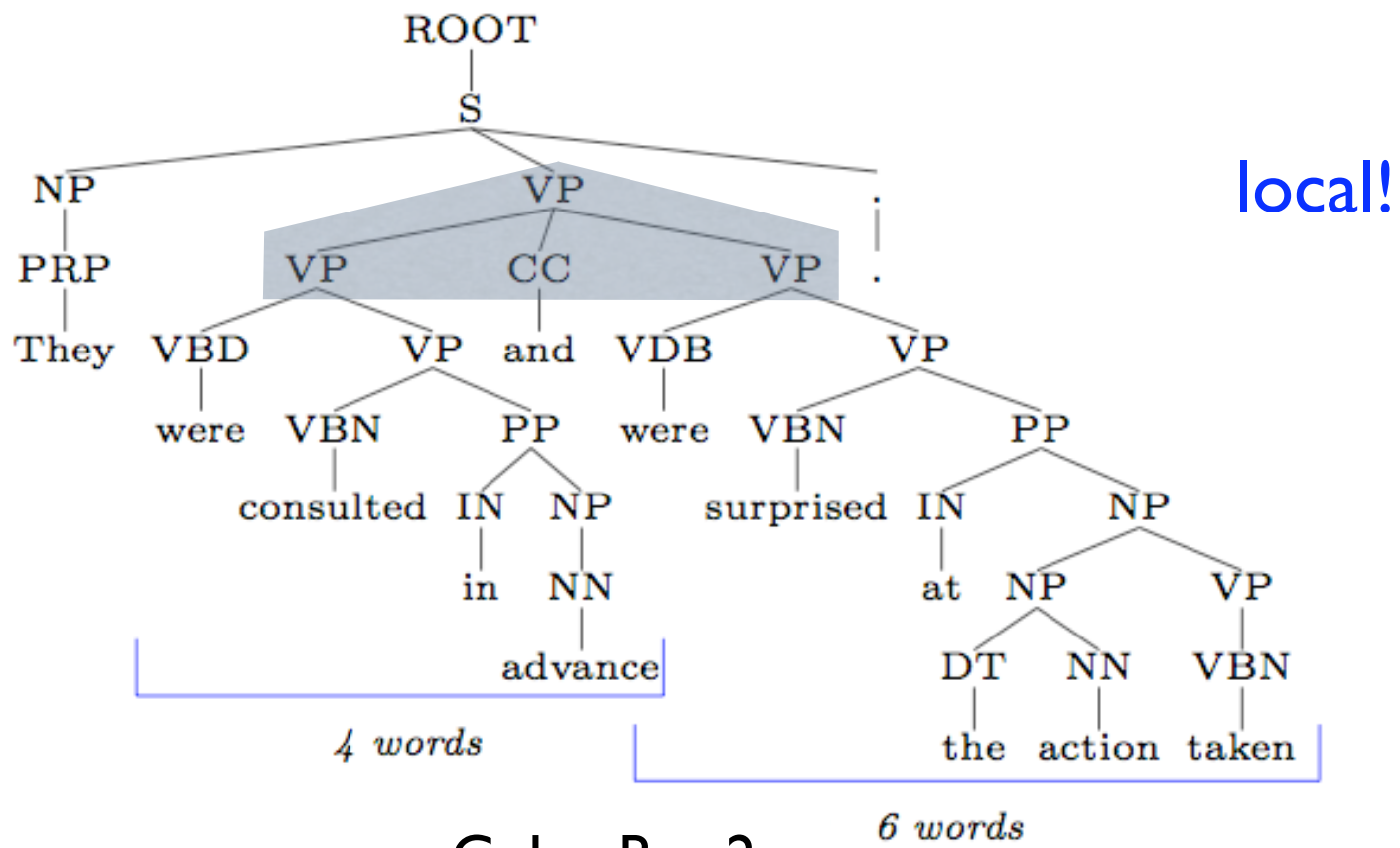
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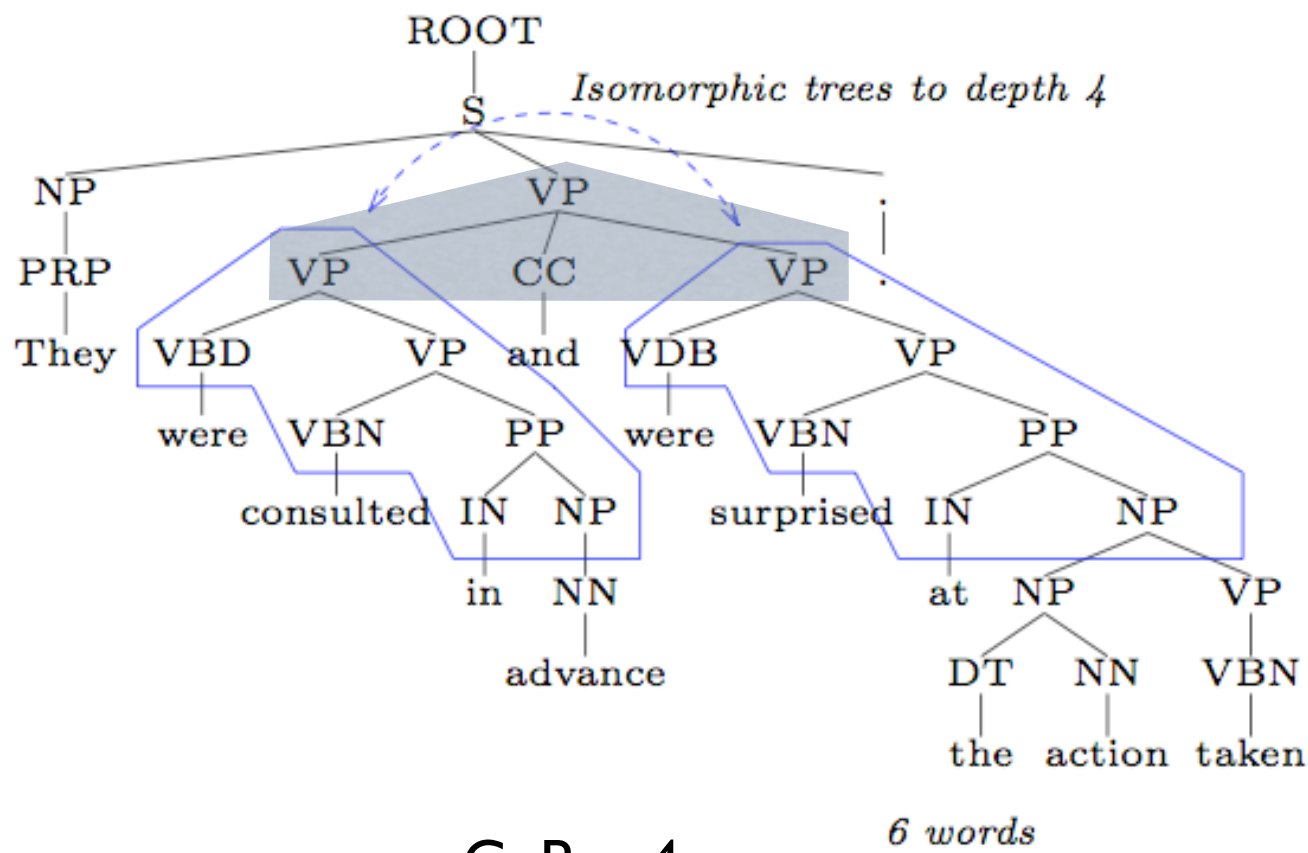
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CoLenPar: 2

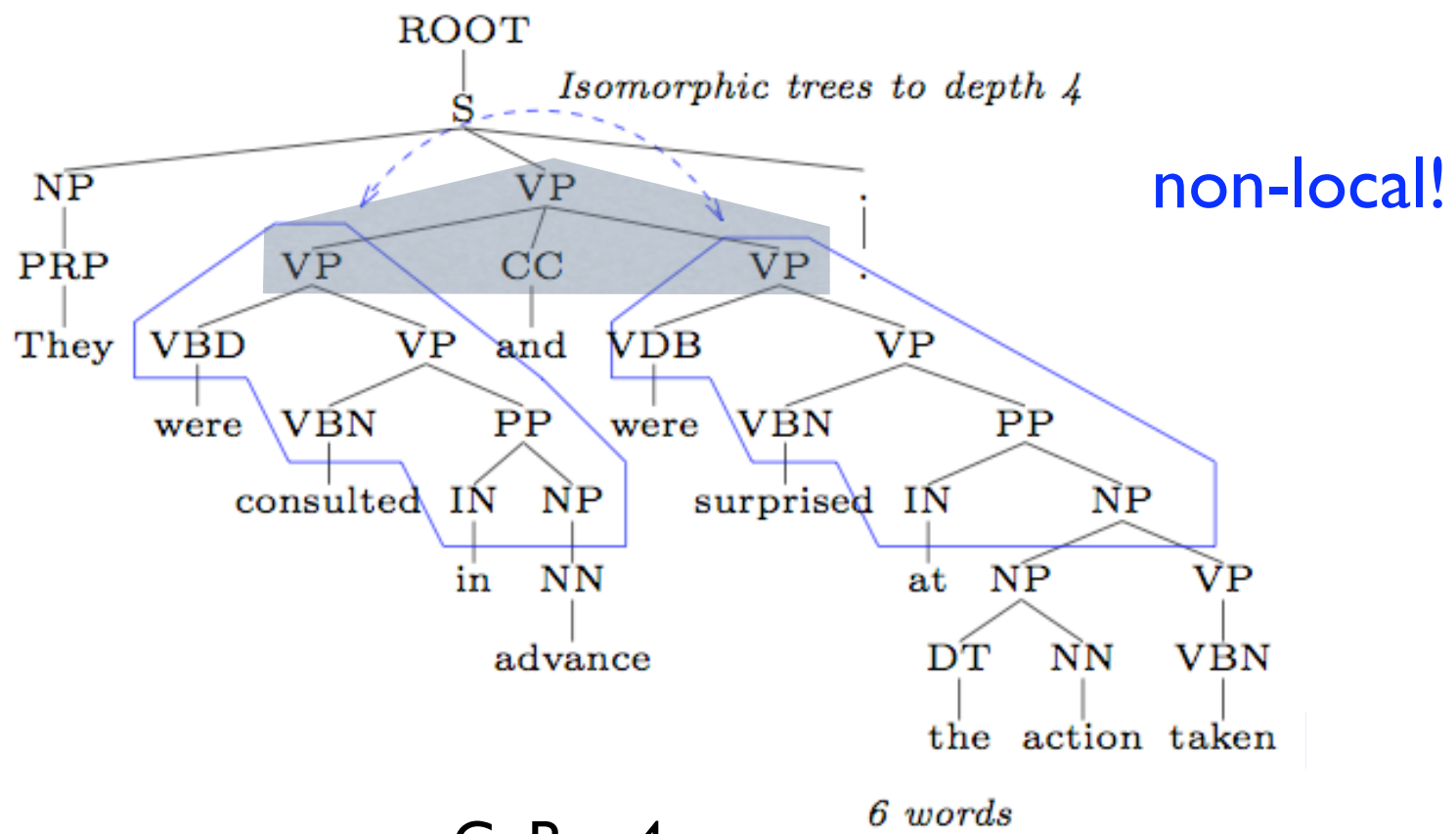
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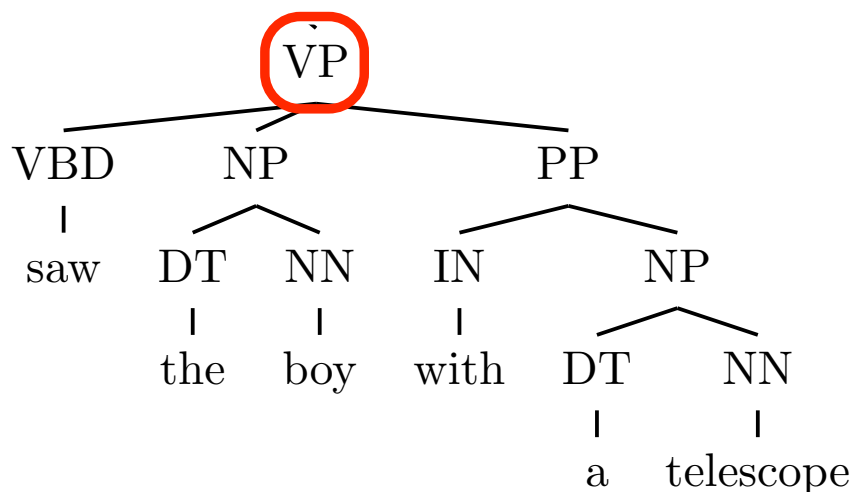
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Factorizing non-local features

- going bottom-up, at each node
- compute (partial values of) feature instances that become computable at this level
- postpone those uncomputable to ancestors

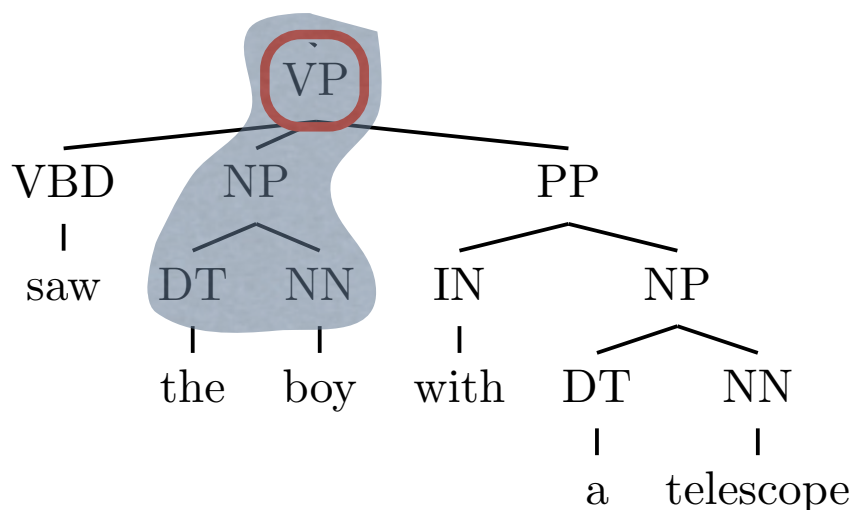
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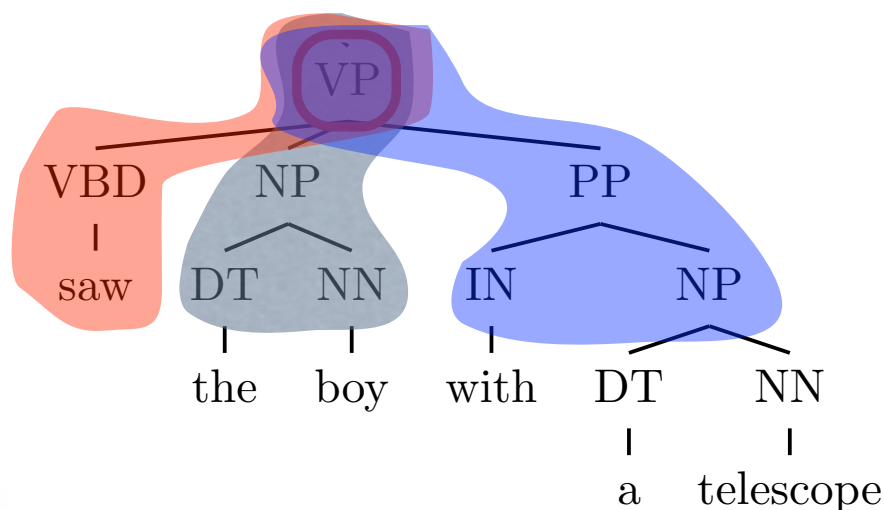
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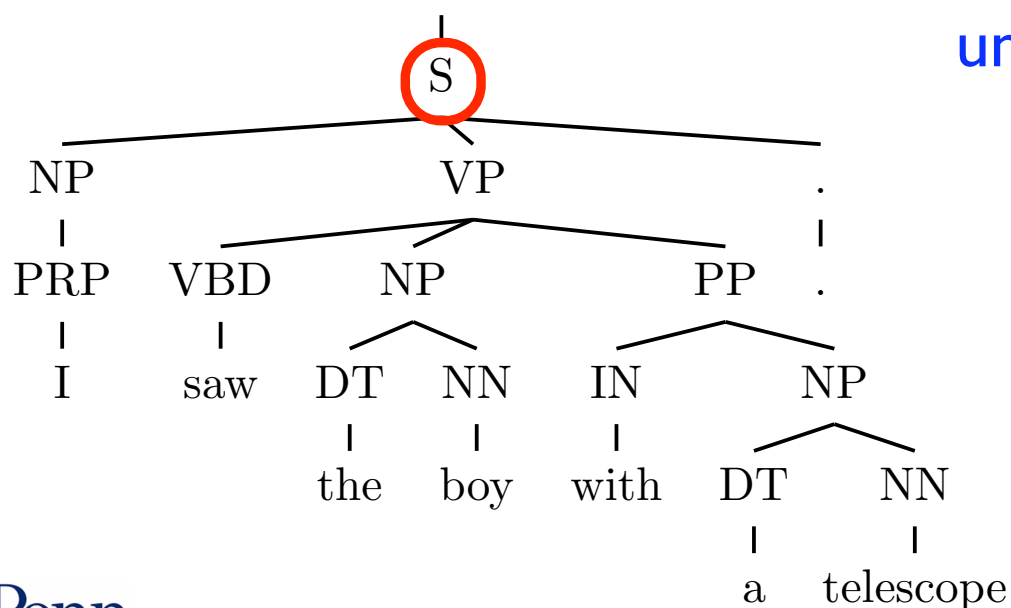
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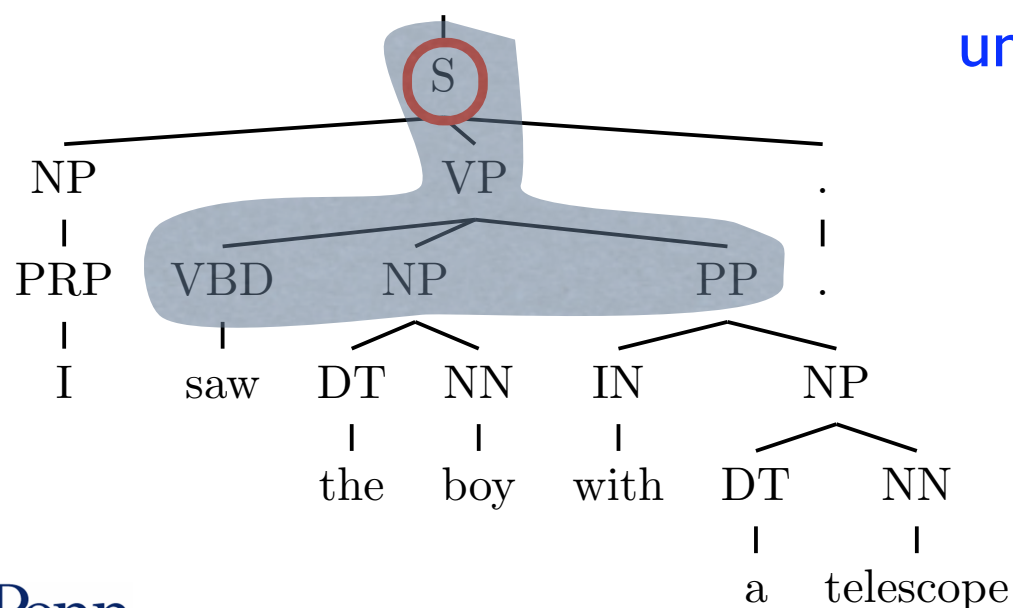
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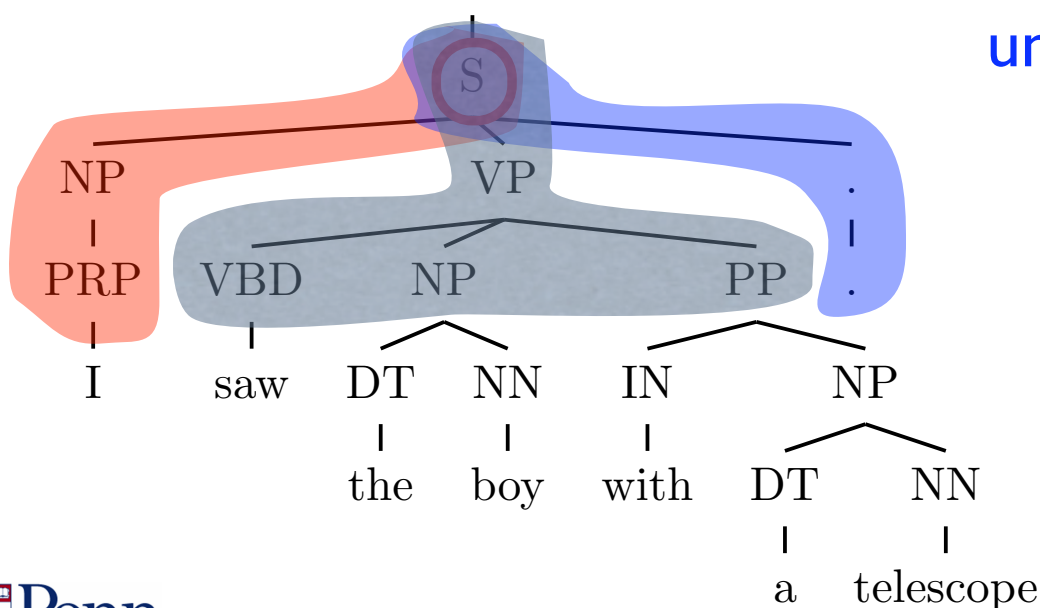
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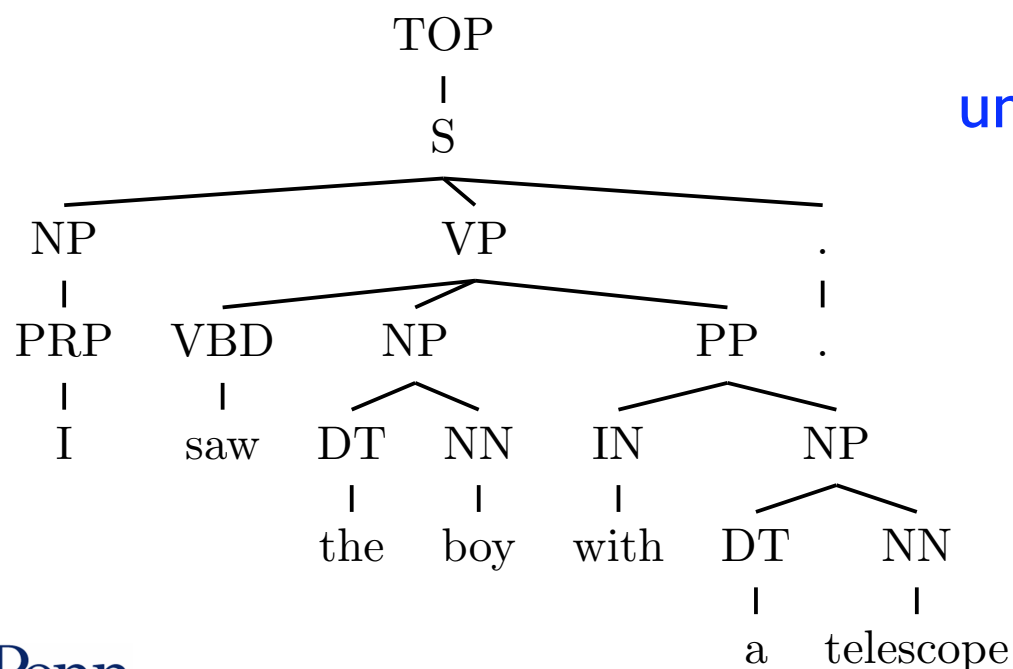
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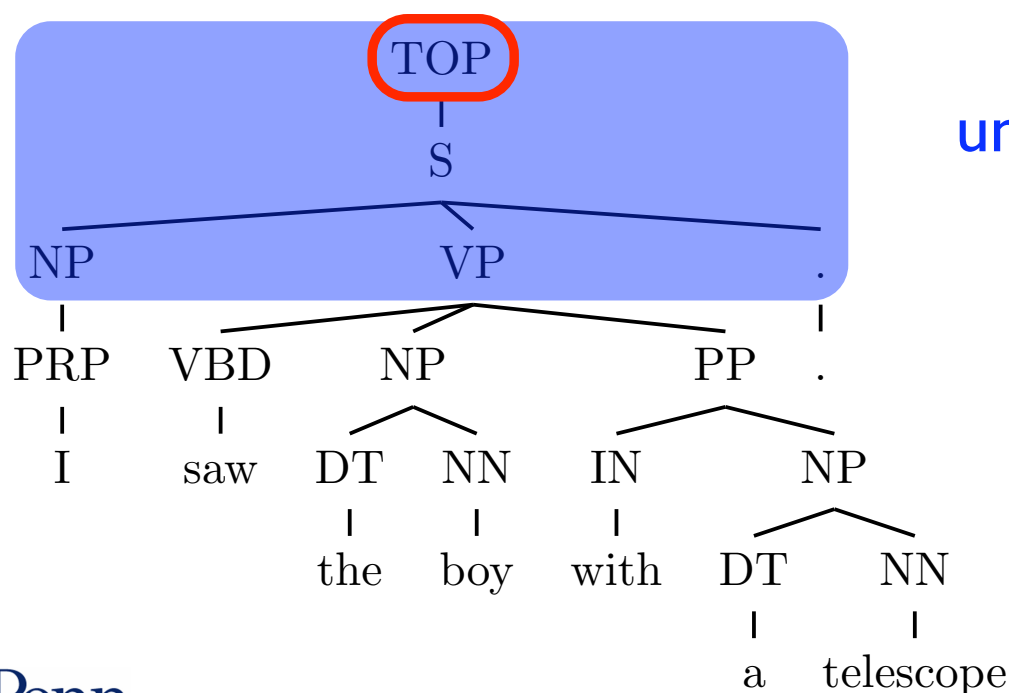
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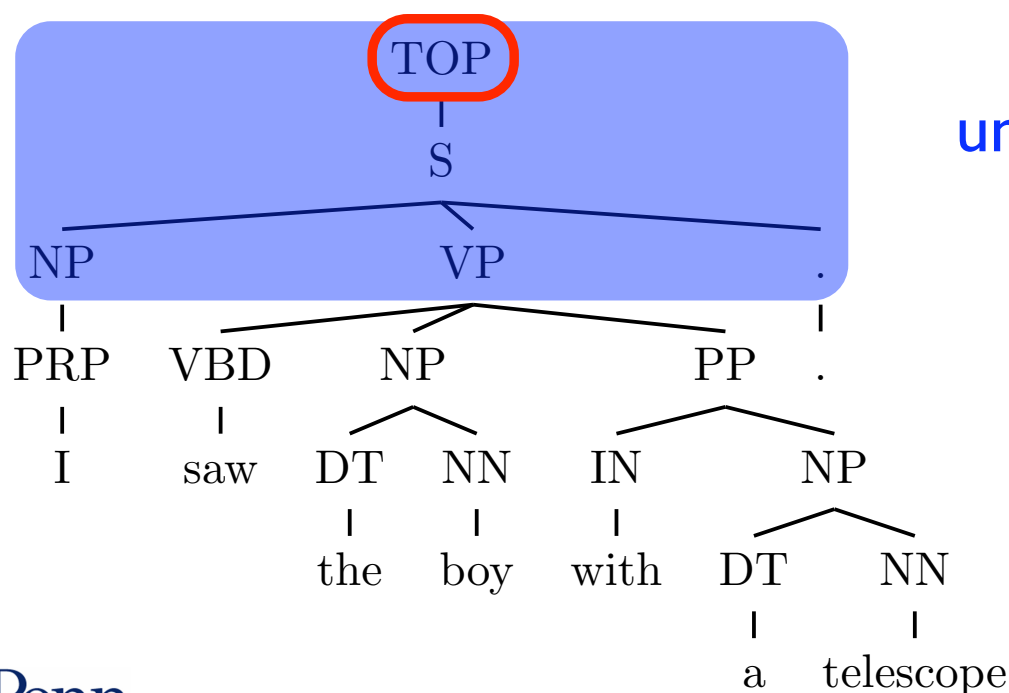
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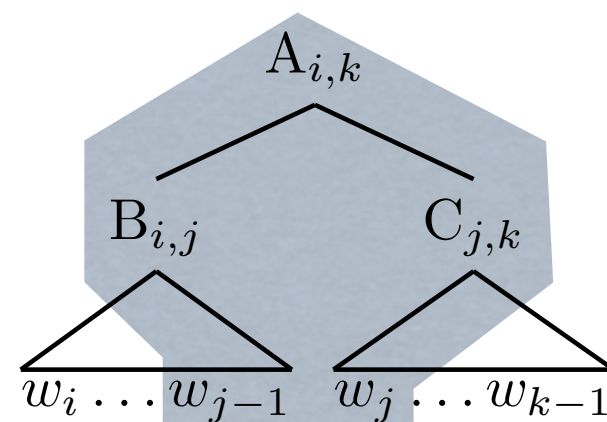
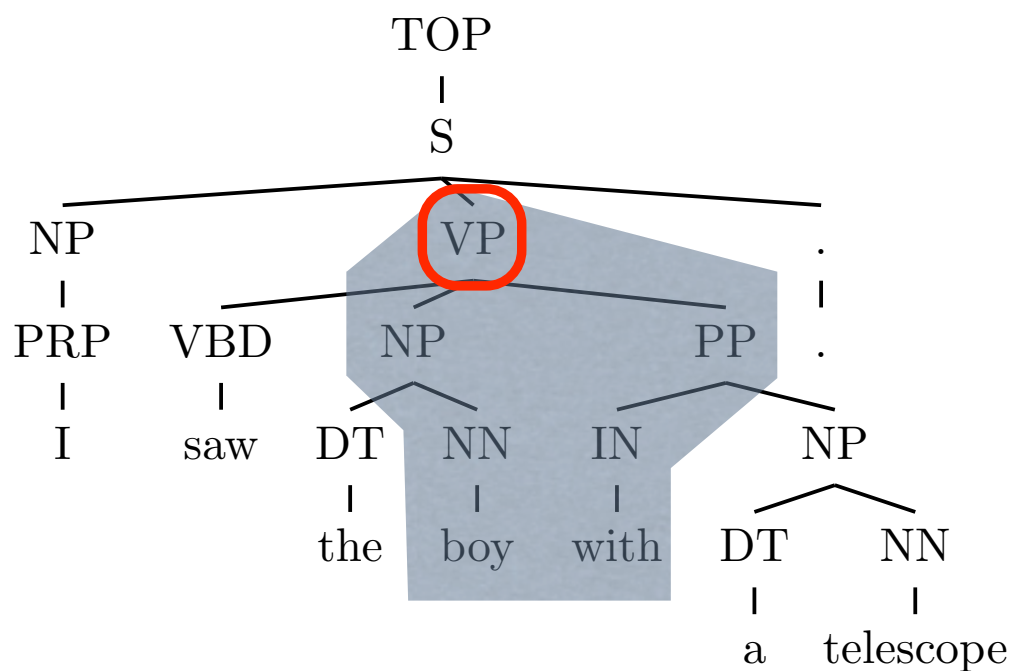
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non-local features factor
across **nodes** *dynamically*

local features factor
across **hyperedges** *statically*

NGramTree (C&J 05)

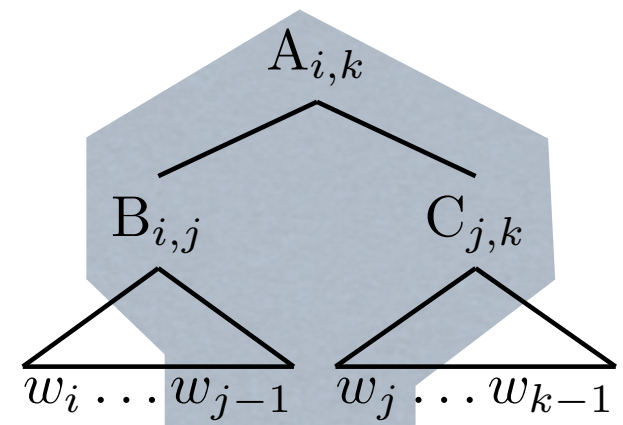
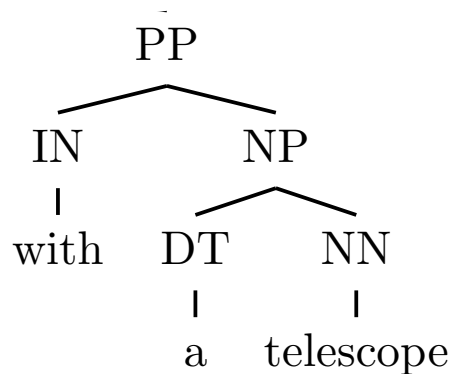
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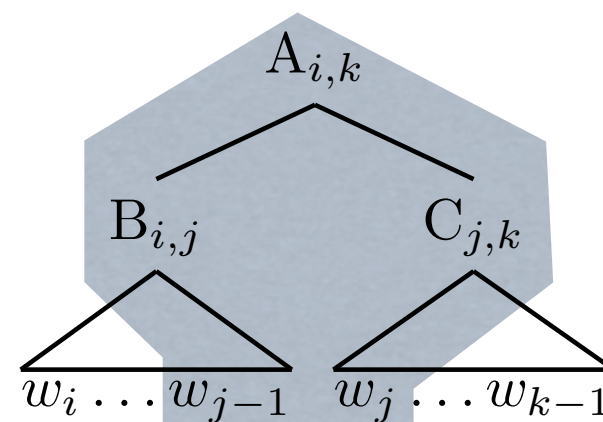
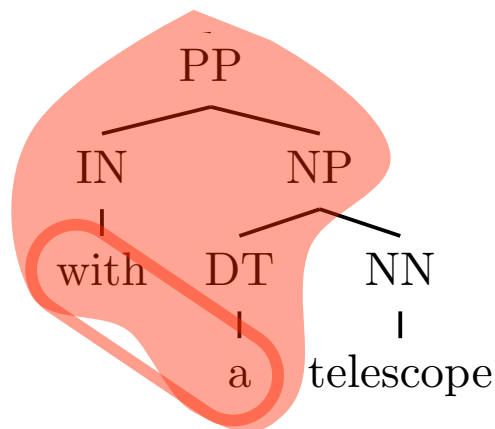
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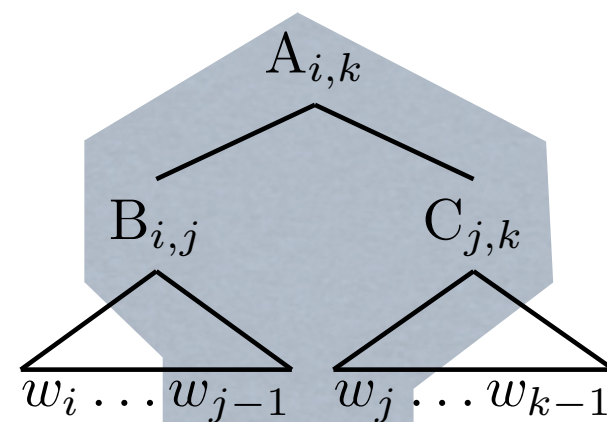
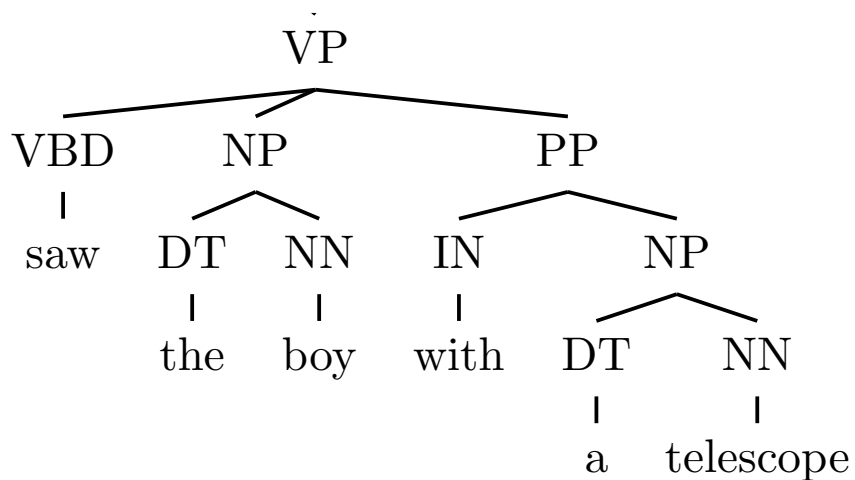
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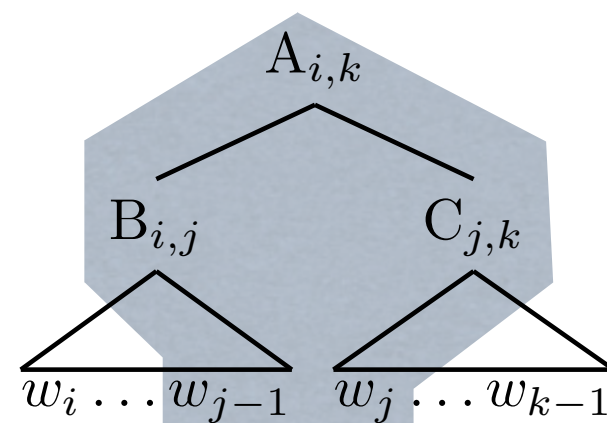
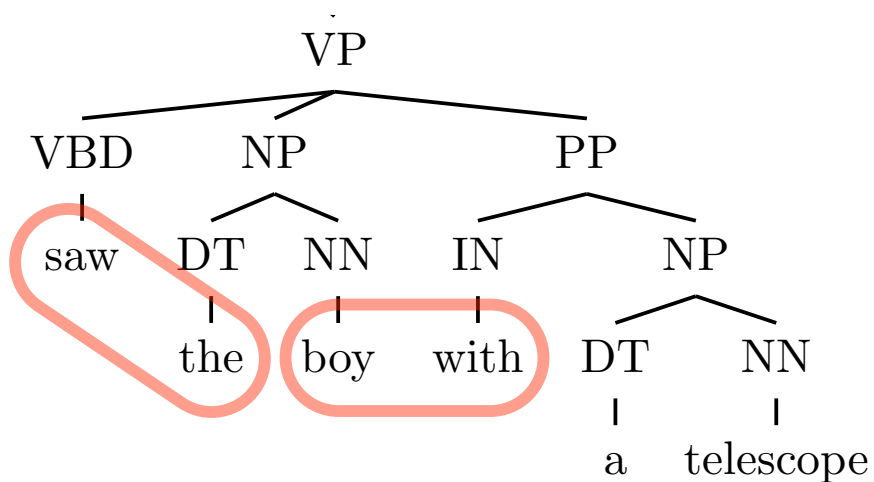
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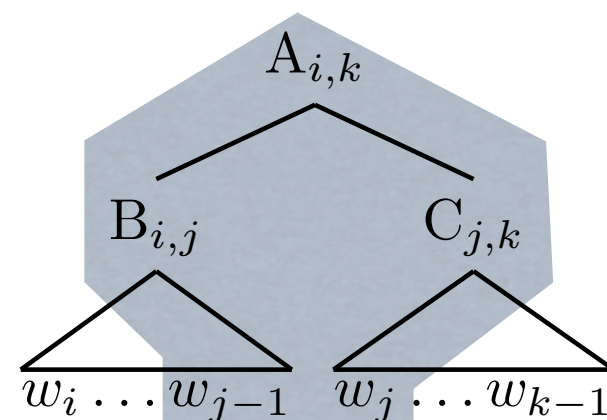
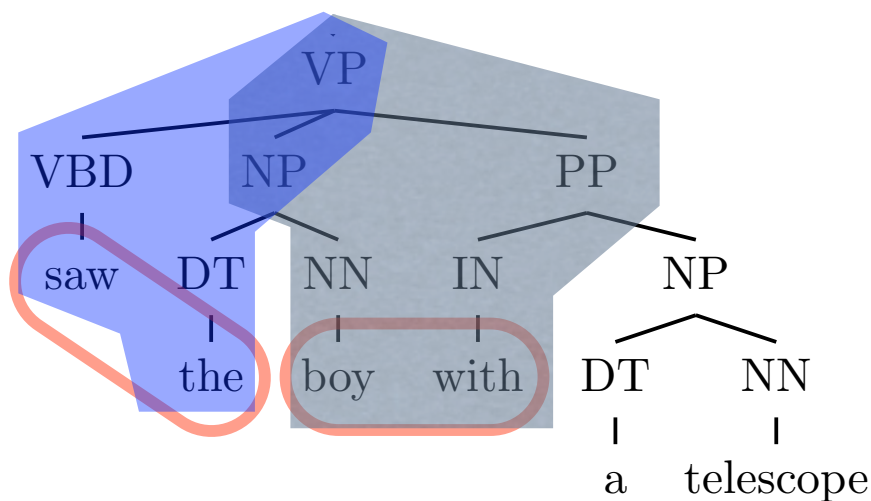
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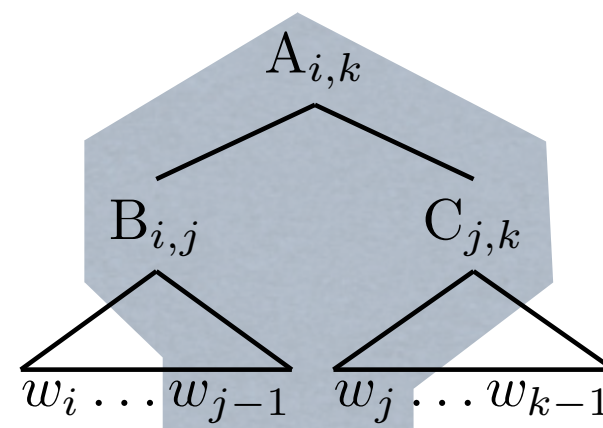
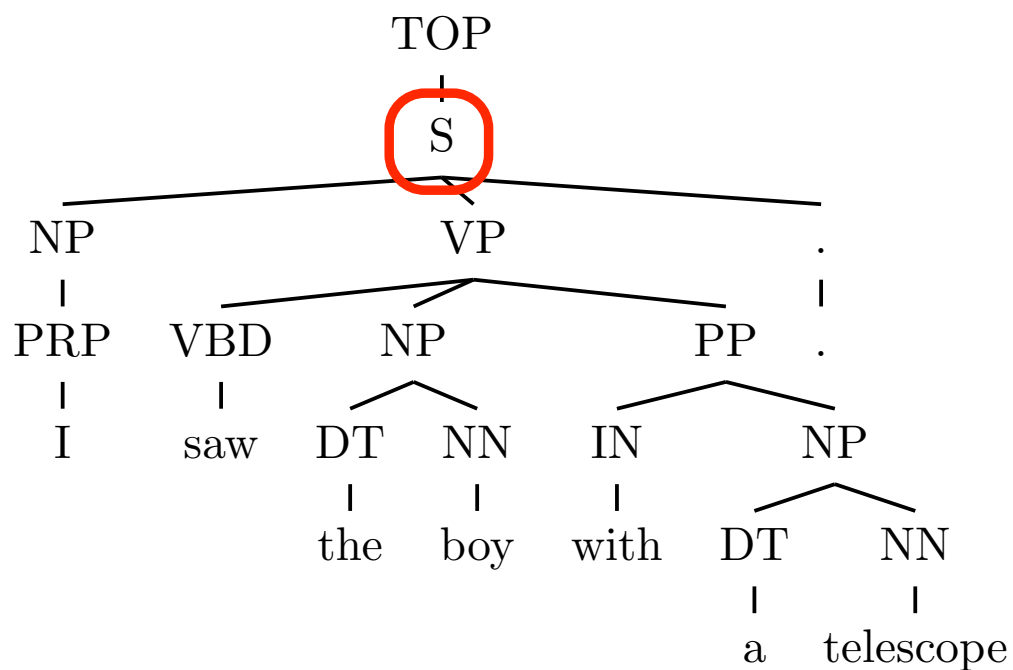
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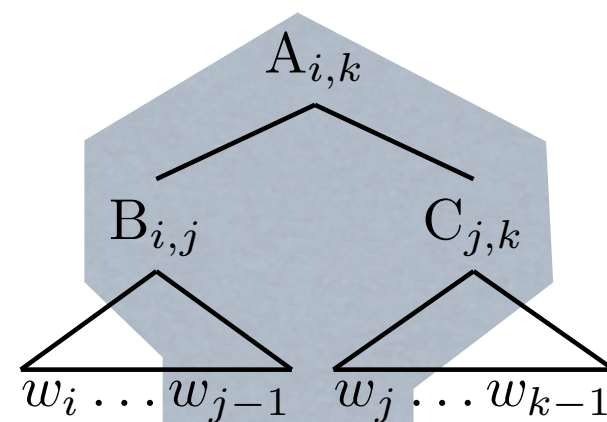
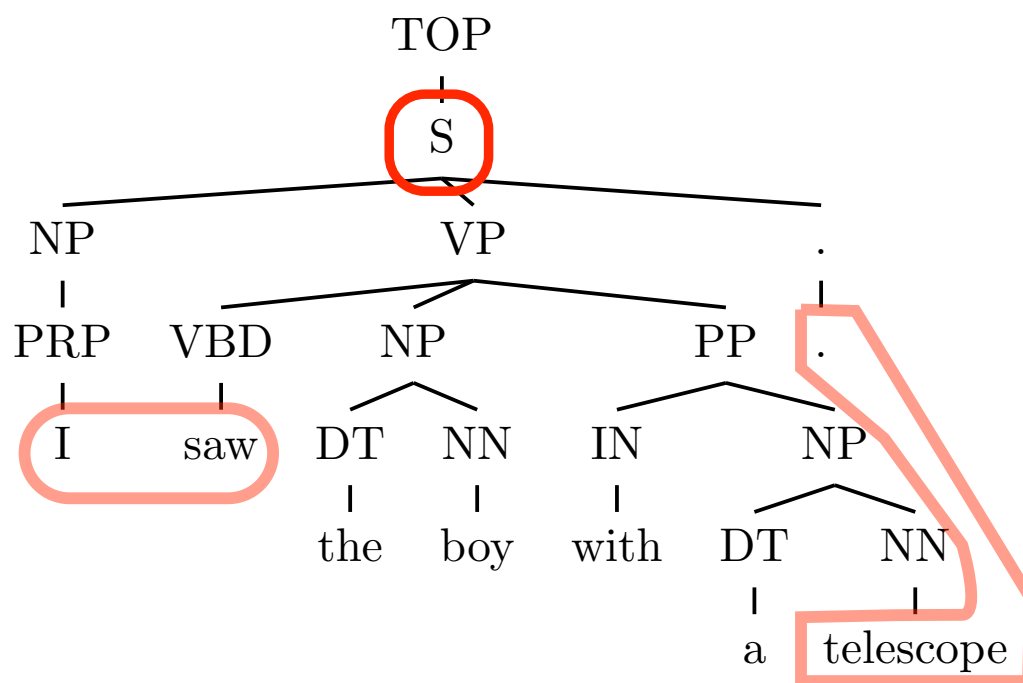
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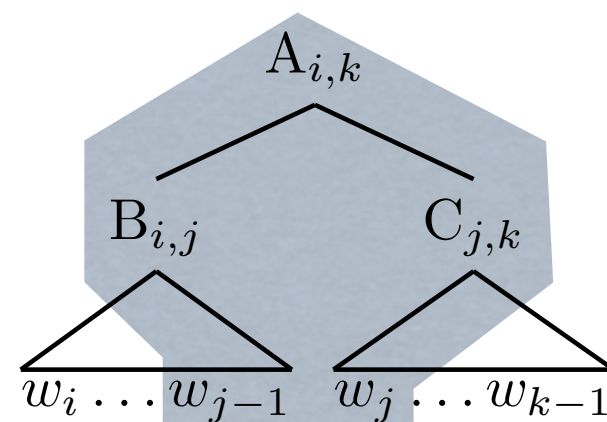
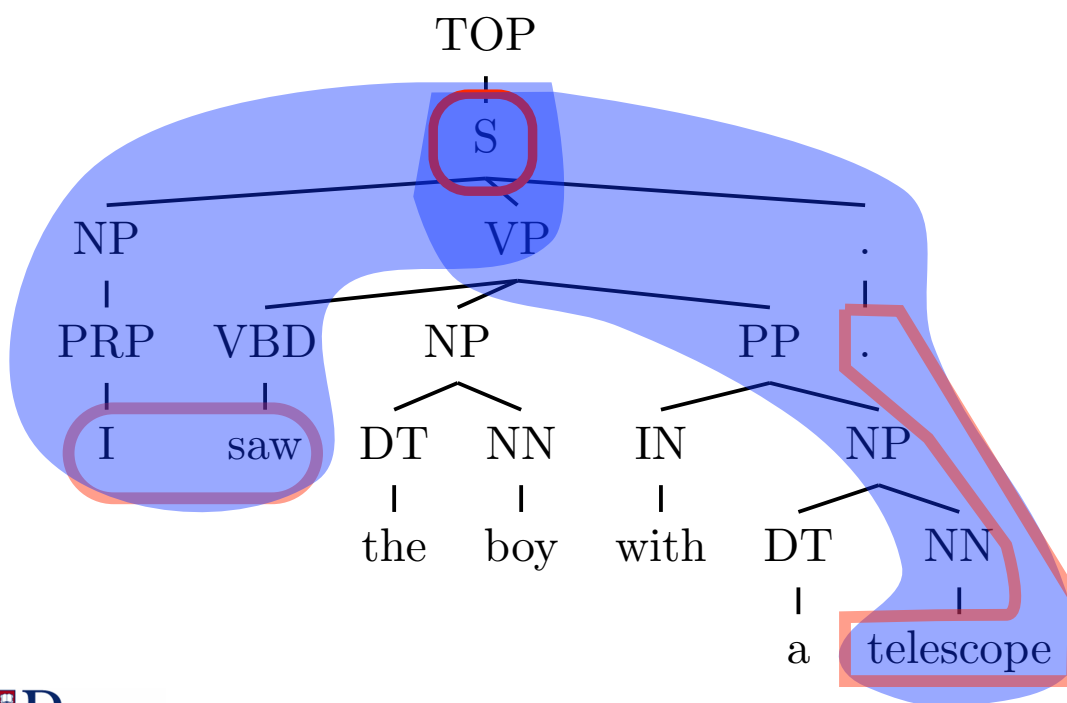
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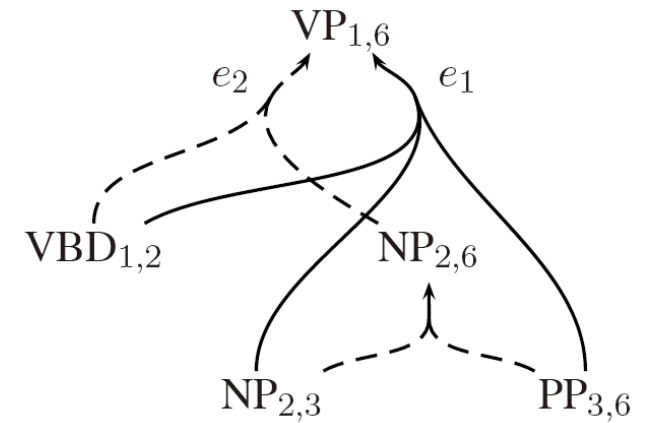


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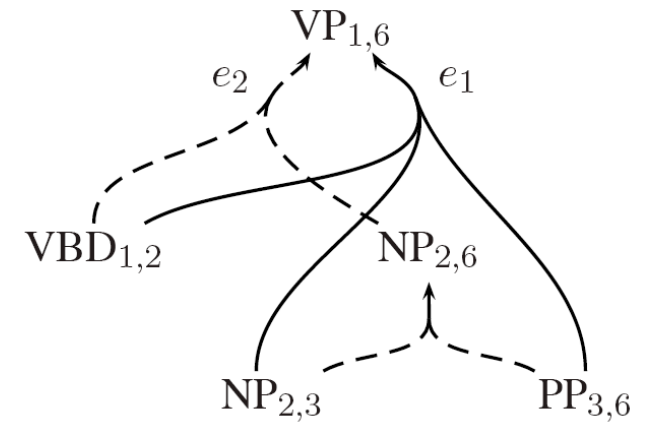
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General Idea of Decoding



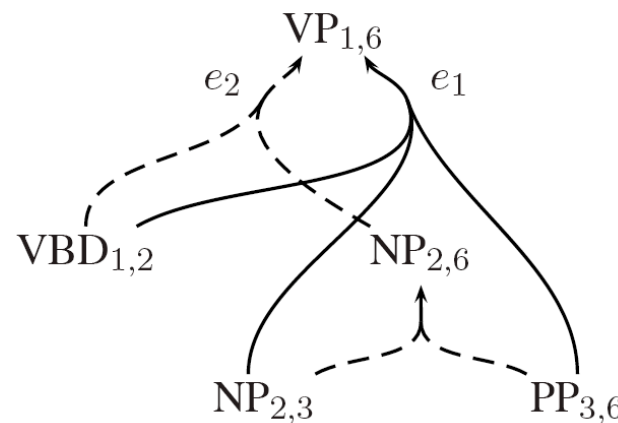
General Idea of Decoding

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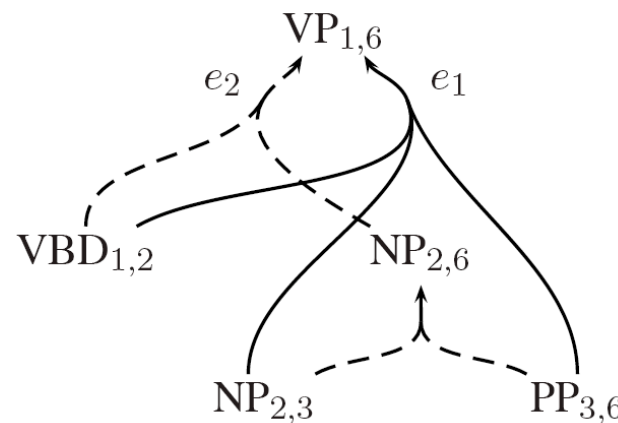
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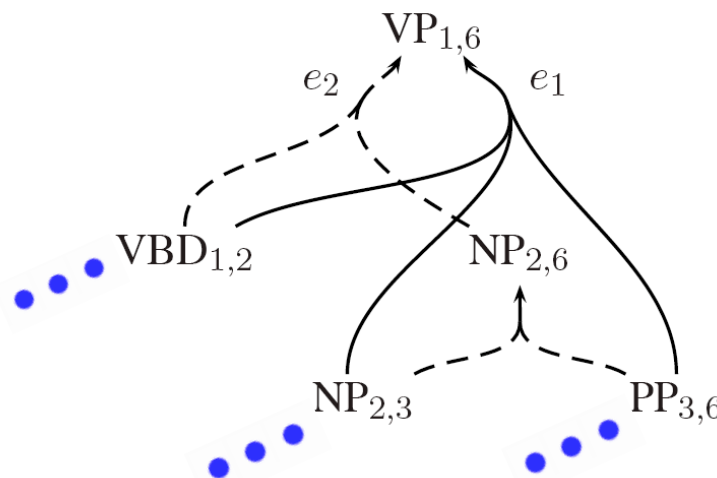
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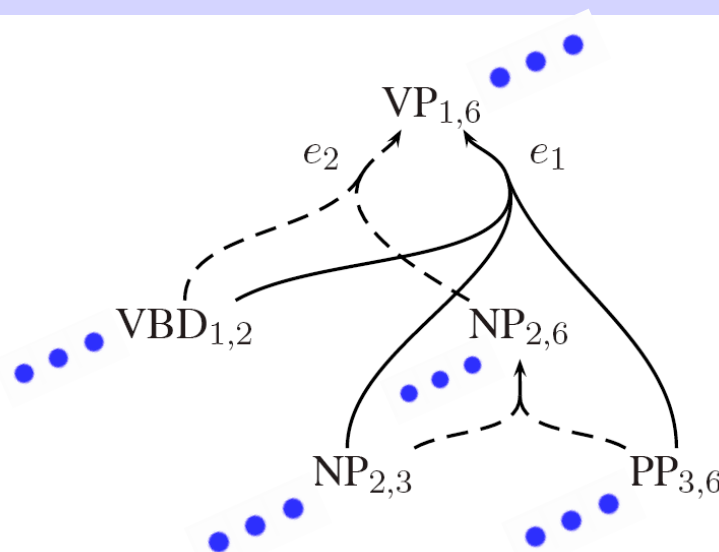
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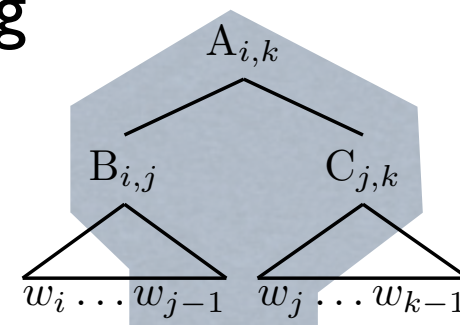
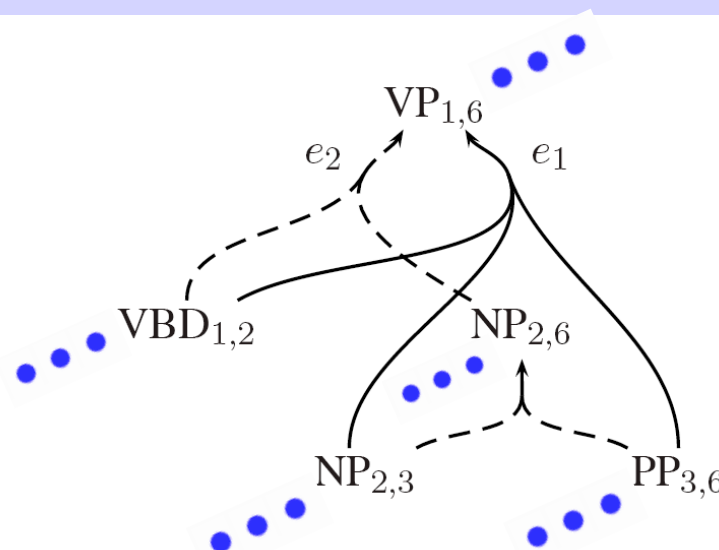
General Idea of Decoding

- bottom-up (chart parsing)
- keep top k trees at each node
 - combine top subtrees
 - score unit non-local features
- similar to machine translation decoding with integrated language models
 - non-local features \Leftrightarrow LM combo
 - so we use forest rescoring from MT
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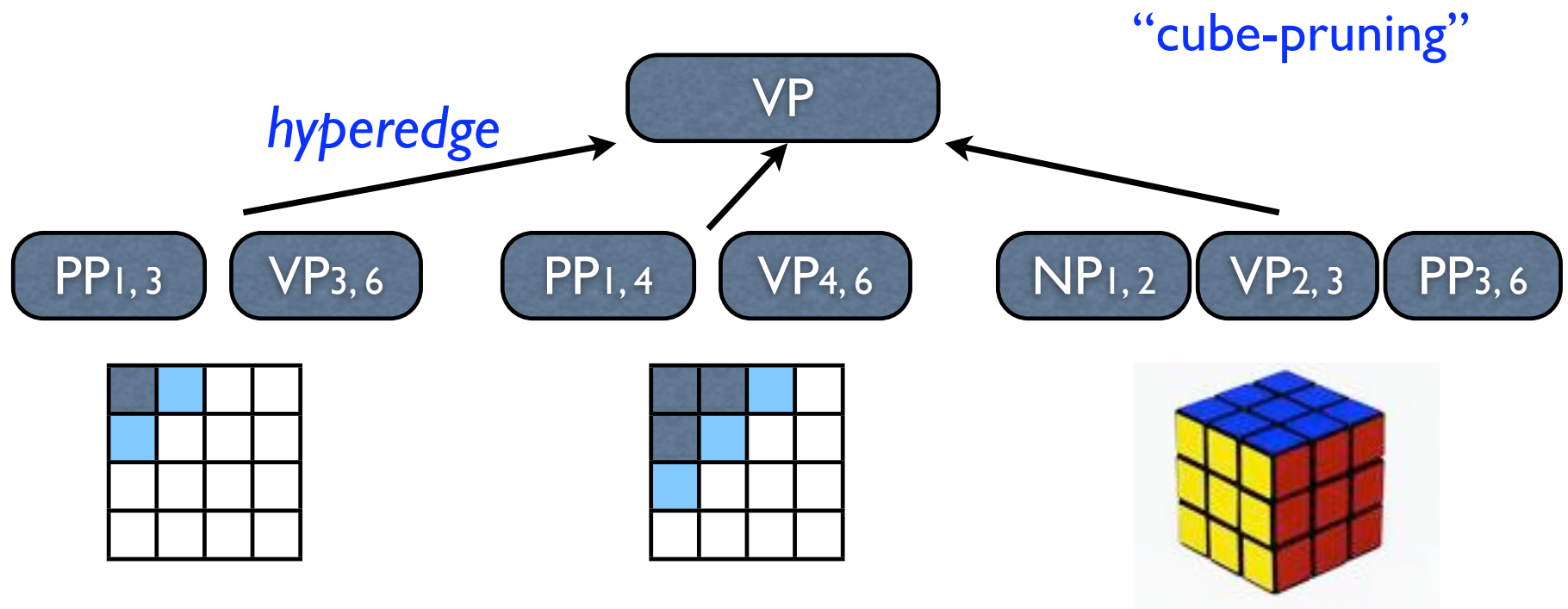
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Faster Decoding

- best-first exploration of hyperedges **simultaneously!**
significant savings of computation
- most of the item combinations are neglected



Experiments

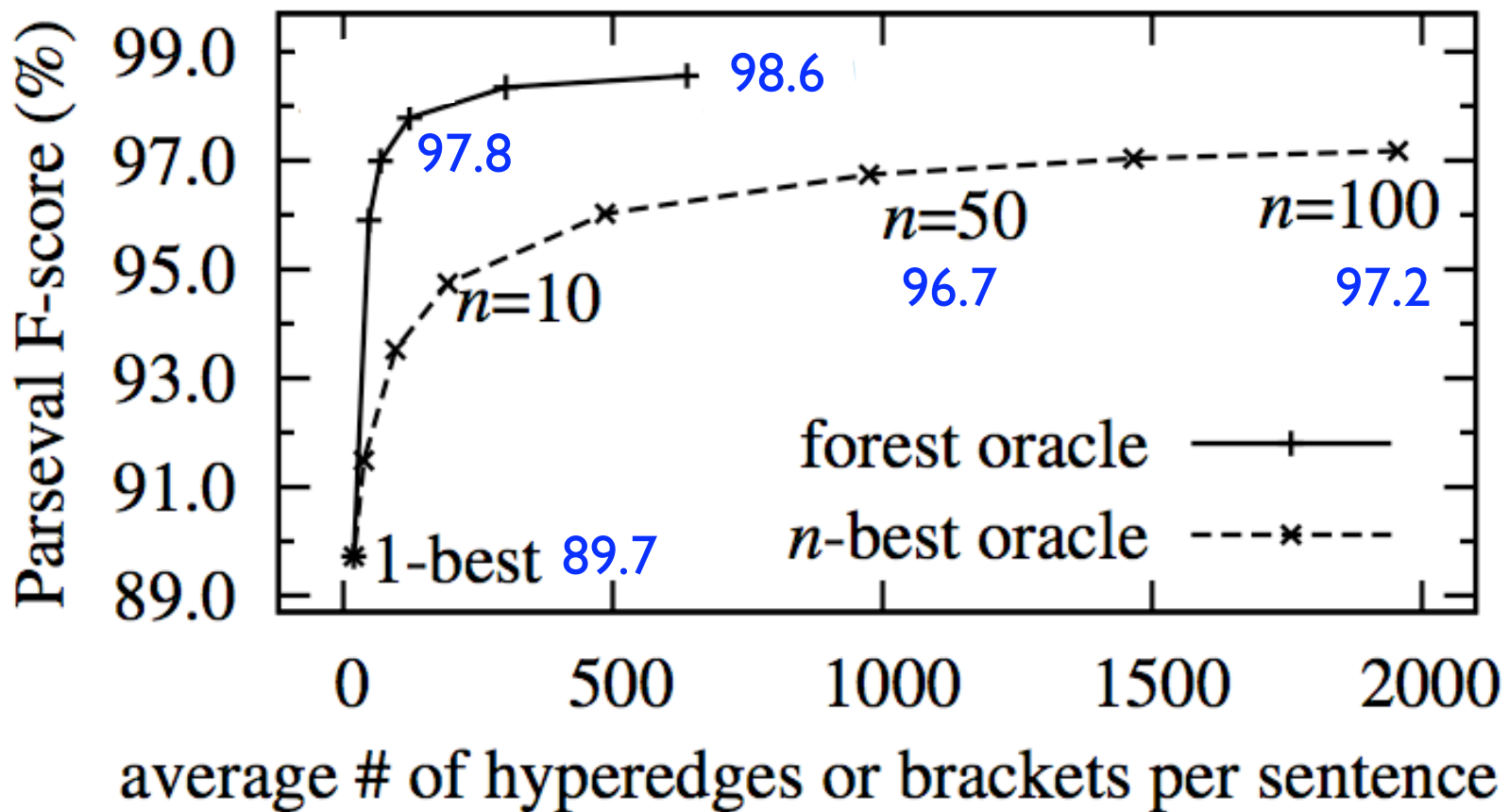
scaled to the whole Penn Treebank

Data Preparation

- use Charniak parser as baseline
- standard split: train: sec 02-21, dev: sec 22, test: sec 23
- training set split into 20 fold (cross-validation style)
- modify Charniak parser to output forests!
 - pruned by an Inside-Outside style algorithm
- use 15 features templates from (Charniak and Johnson, 2005; Collins, 2000); 800, 582 feature instances (~70% local)
- both n -best and forest reranking systems implemented in pure Python, on 64-bit Dual-core 3.0 GHz machines

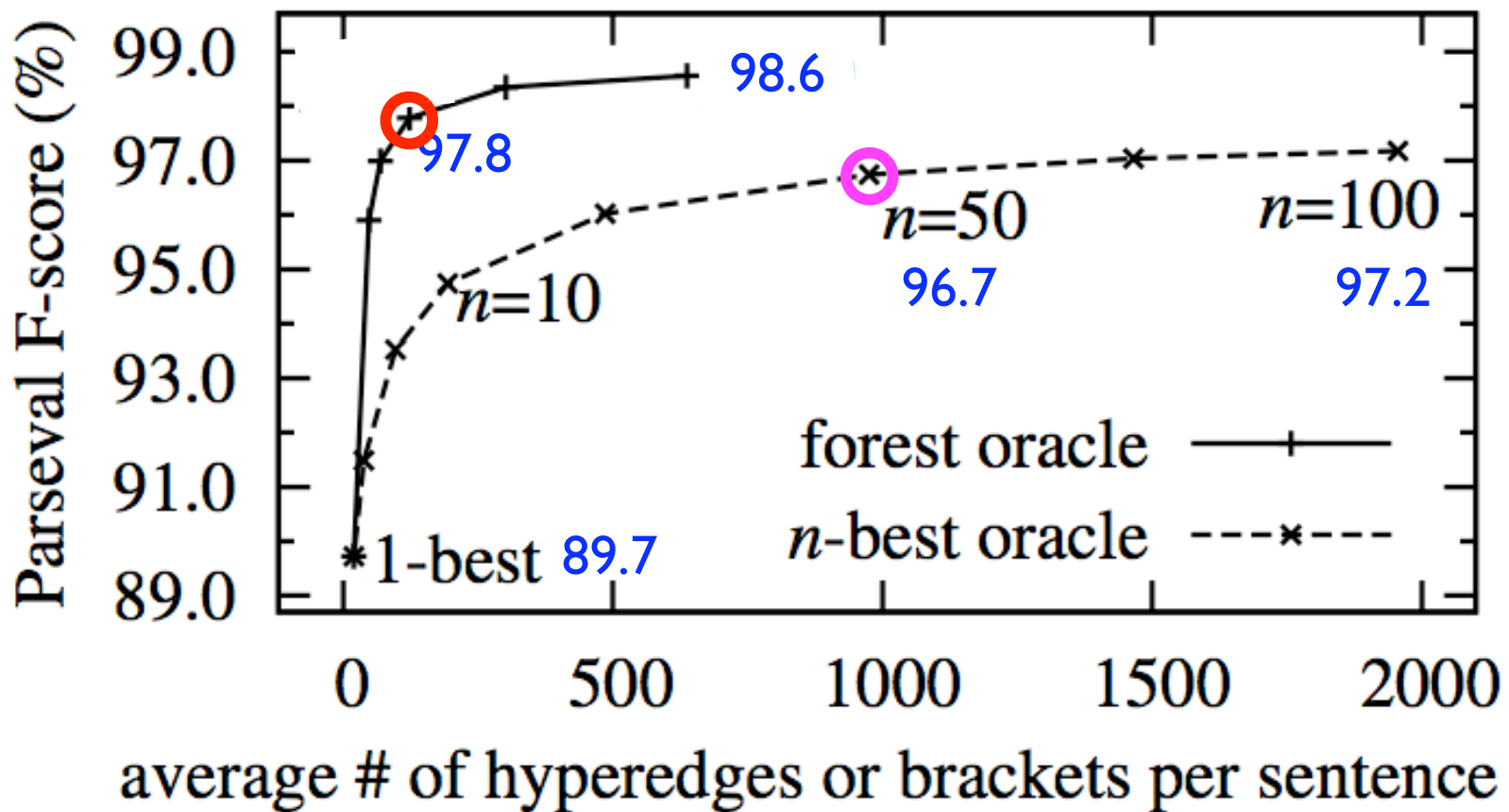
Forest vs. n-best Oracles

- forests enjoy higher oracle scores than *n*-best lists
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Forest vs. n-best Oracles

- forests enjoy higher oracle scores than n -best lists
- a **dynamic programming** algorithm for forest oracle



Main Results

- forest reranking outperforms both 50-best and 100-best reranking
- and can be trained on the whole treebank in ~1 day even with a pure Python implementation!

baseline: 1-best Charniak parser		89.72
approach	training time	F1%
50-best reranking	4 x 0.3h	91.43
100-best reranking	4 x 0.7h	91.49
forest reranking	4 x 6.1h	91.69

details in the paper.

Comparison with Others

approach	system	F ₁ %
reranking	Collins (2000)	89.7
	Charniak and Johnson (2005)	91.0
dynamic programming	Petrov and Klein (2008)	88.3
	<i>this work</i>	91.7
generative	Bod (2000)	90.7
	Petrov and Klein (2007)	90.1
semi-supervised	McClosky et al. (2006)	92.1

Conclusion

- A Framework for Reranking on Packed Forests
 - forests have more variations and smaller sizes
 - dynamic programming algorithm for forest oracles
- Two Key Ideas that made it work
 - incremental, recursive computation of features
 - forest rescore for approximate decoding
- Discriminative training scaled to the whole PTB
 - better than both 50-best and 100-best reranking
 - better than any previous results trained on PTB

Conclusion

- more akin to traditional chart parsing, not reranking!
- multipass search (Goodman, 1997)
 - non-local features in the pruned forest
 - but without blowing up the forest
- better search algorithms should help!
- could in principle incorporate fancier features
- also applicable to other problems involving forest
 - sequence segmentation/labeling, dependency parsing, machine translation, generation, ...

Forest is your friend. Save the forest.



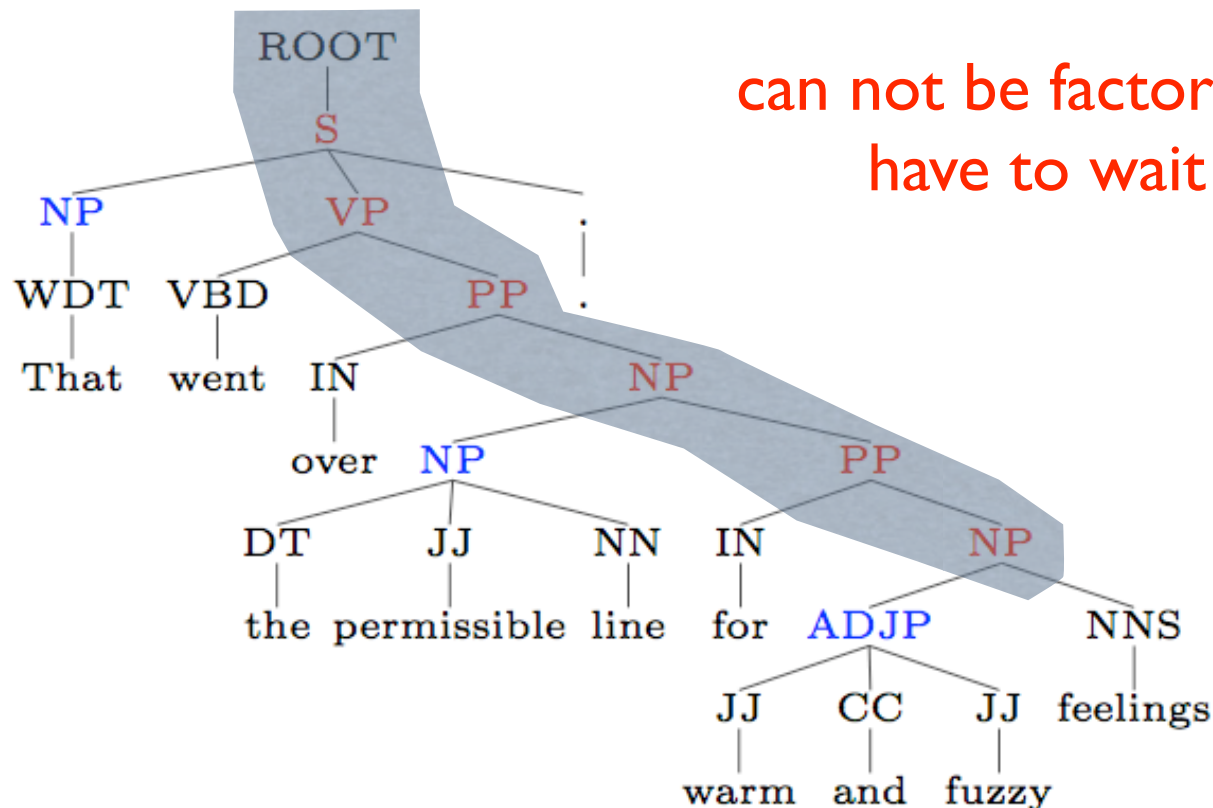
Thank you!

Forest-dumping Charniak parser
will be available online.



Global Feature - RightBranch

- length of rightmost (non-punctuation) path
- English has a right-branching tendency

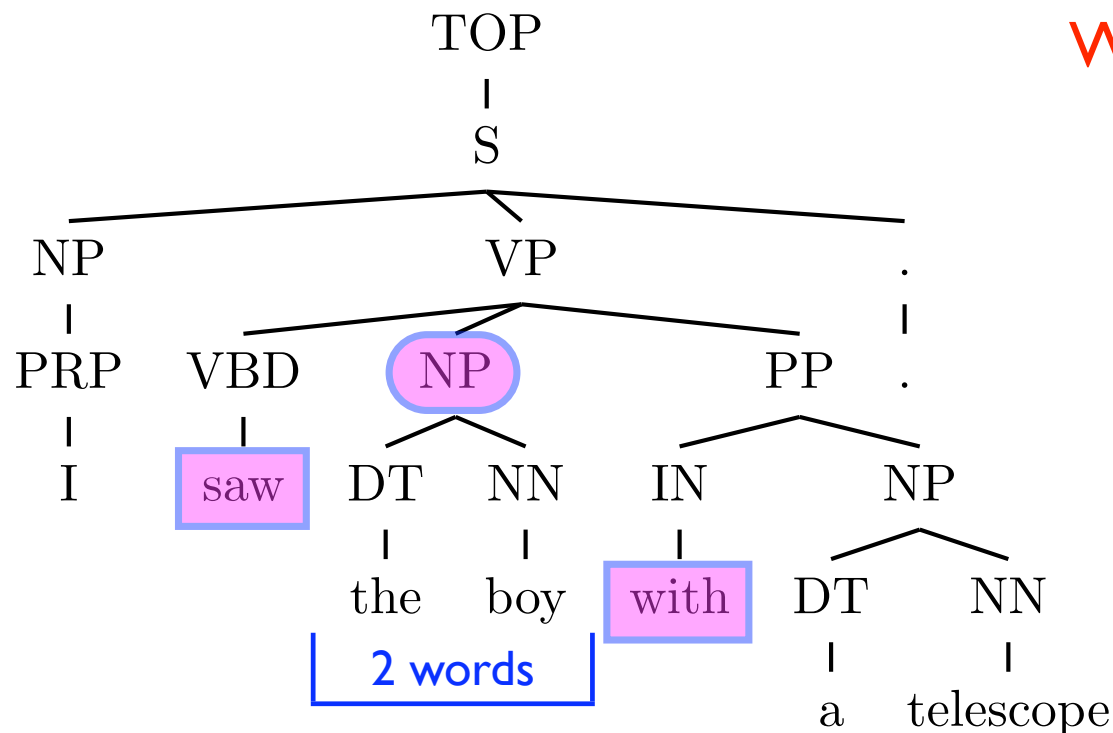


WordEdges (C&J 05)

- a **WordEdges** feature classifies a node by its label, (binned) span length, and surrounding words
- a **POSEdges** feature uses surrounding POS tags

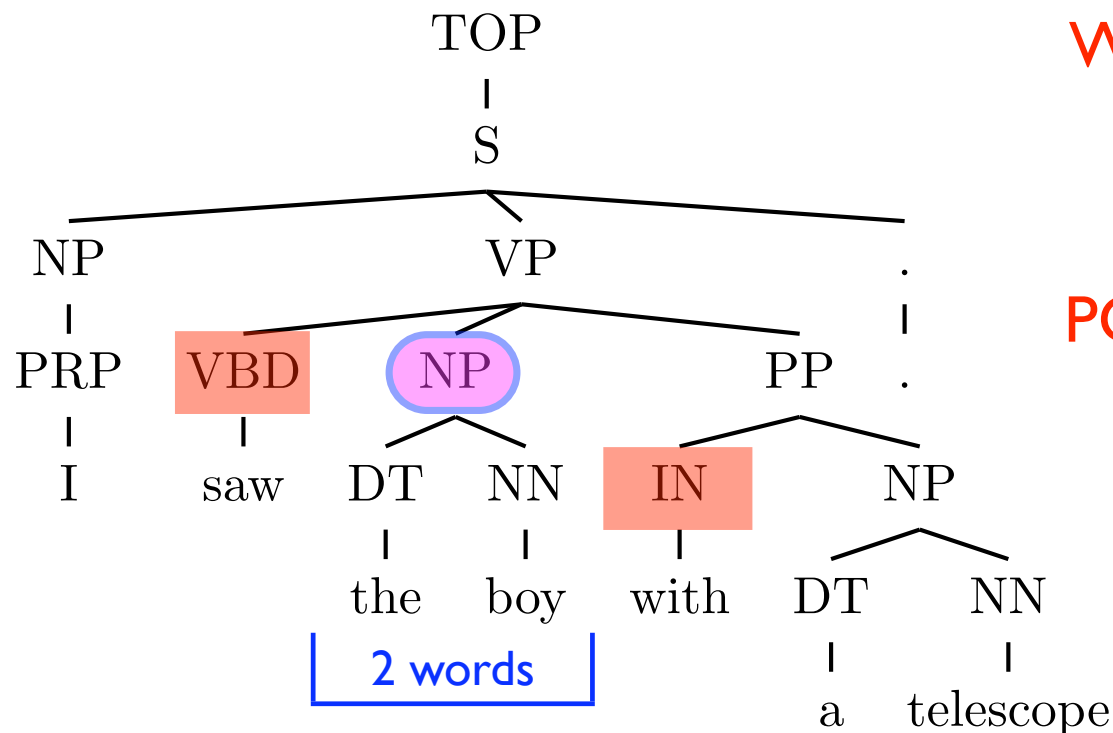
WordEdges is local

$$f_{400}(y) = f_{\text{NP 2 saw with}}(y) = 1$$



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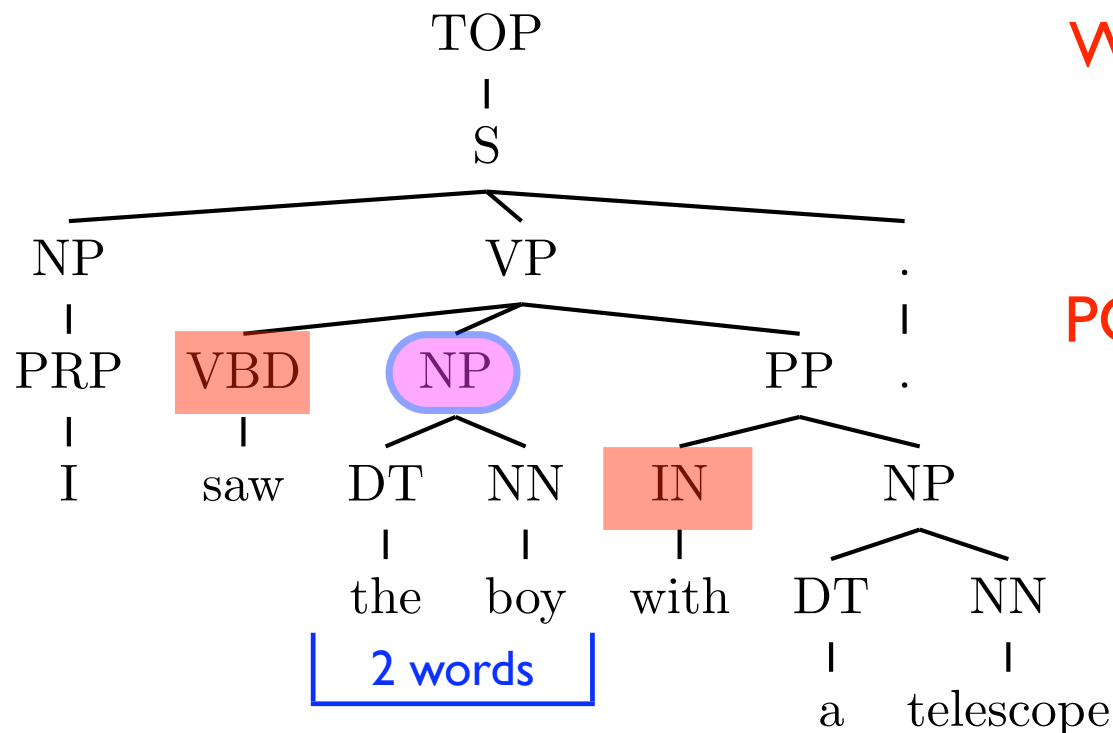
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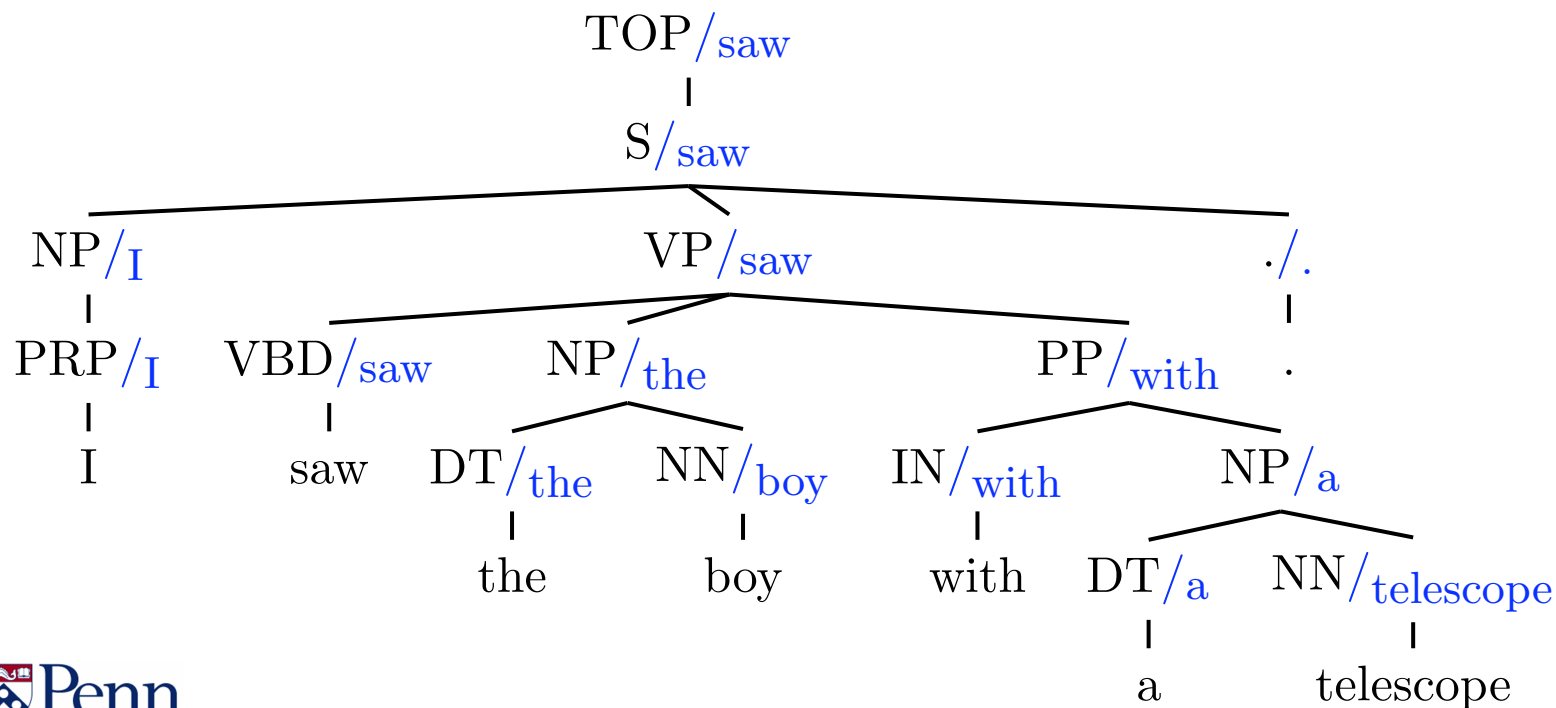
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local features comprise
~70% of all instances!

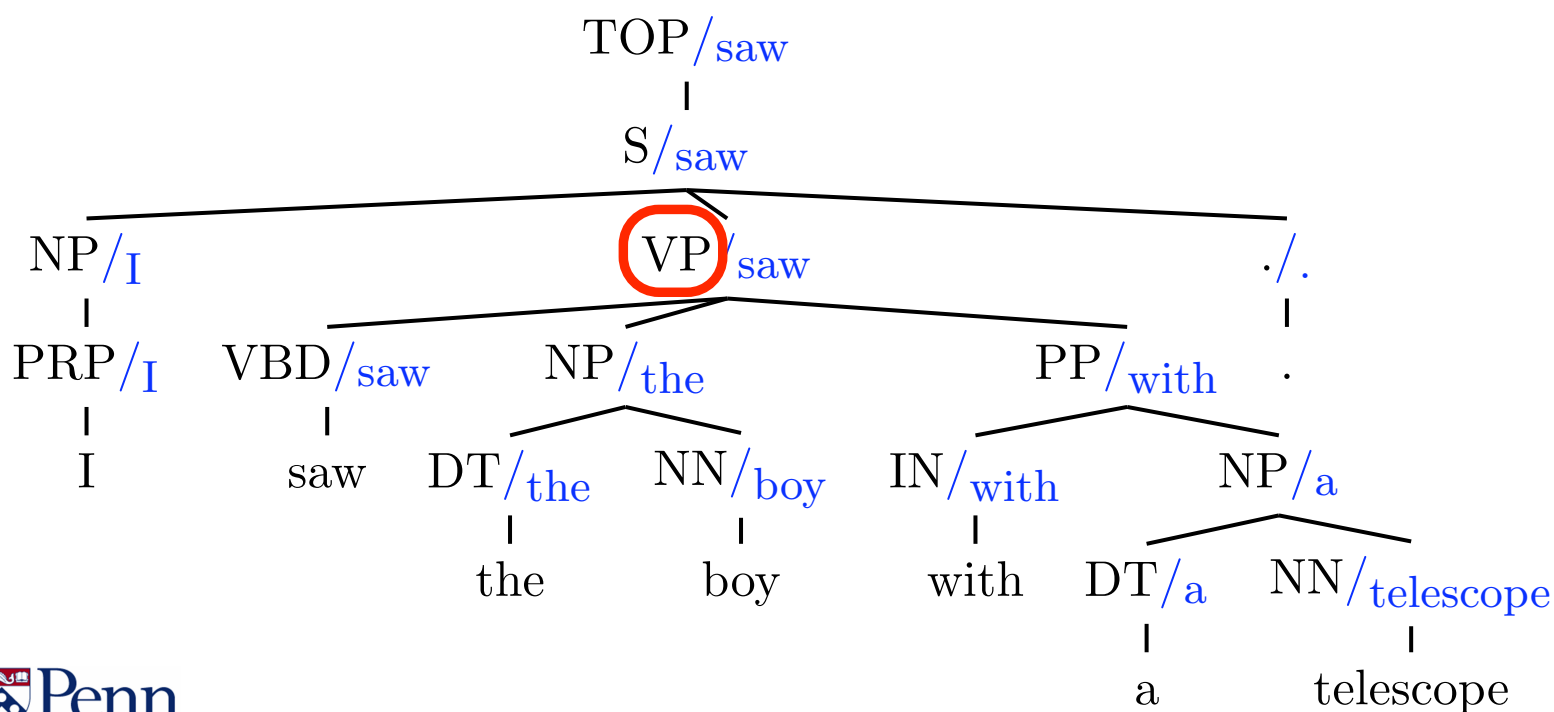
Heads (C&J 05, Collins 00)

- head-to-head lexical dependencies
- we percolate heads bottom-up
- unit instances are between the head word of the head child and the head words of non-head children



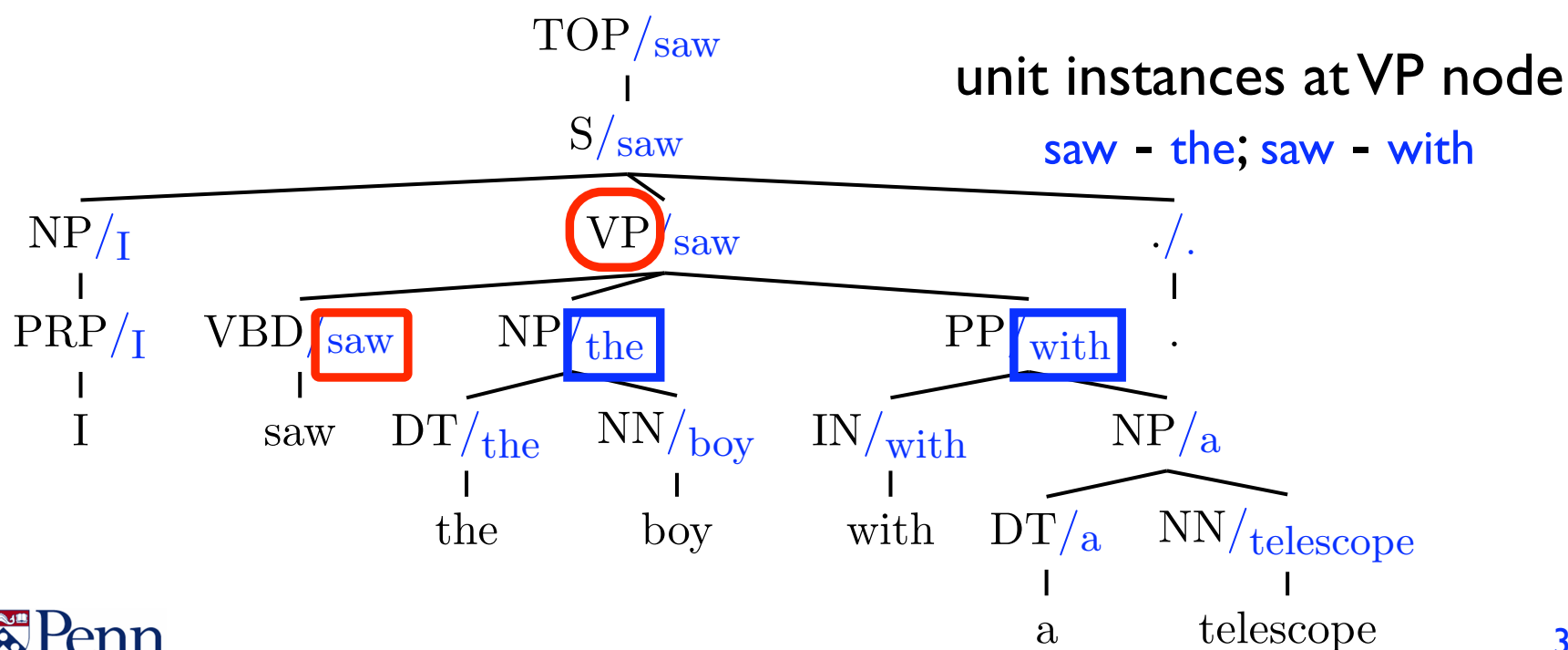
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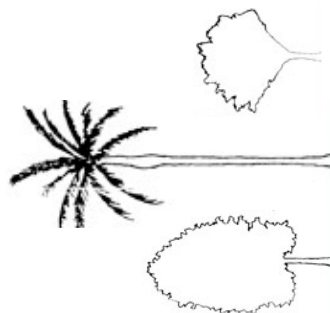
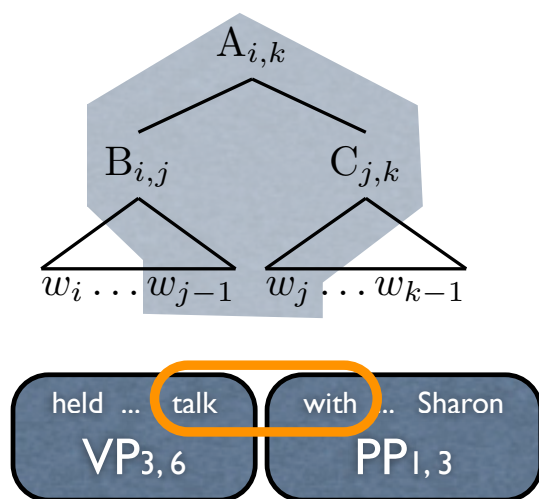
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Approximate Decoding

- bottom-up, keeps top k derivations at each node
- forest rescoring from MT (Chiang 2007; Huang and Chiang 07)
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 - each iteration pops the best and pushes successors
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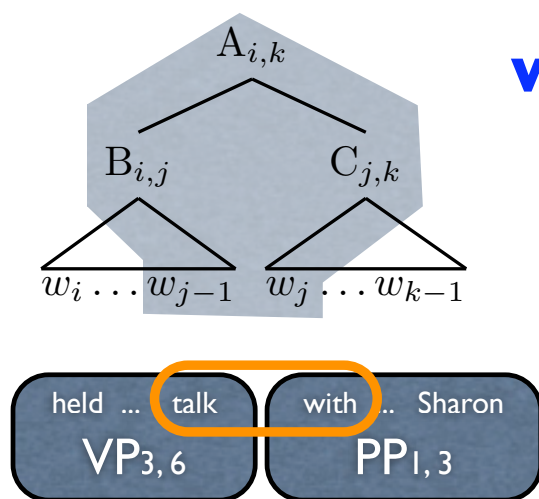


Three line drawings of different tree shapes are shown above the cost matrix: a tall, thin tree, a rounded tree, and a bushy tree.

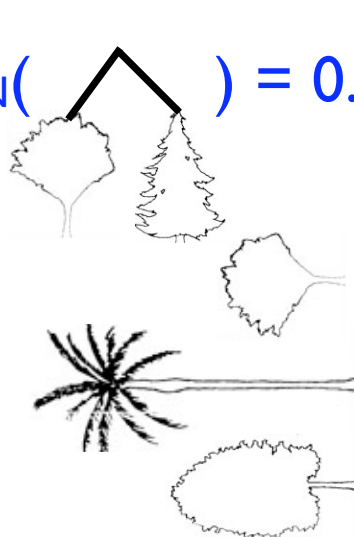
	1.0	3.0	8.0
1.0	2.5	9.0	9.5
1.1	2.4	9.5	9.4
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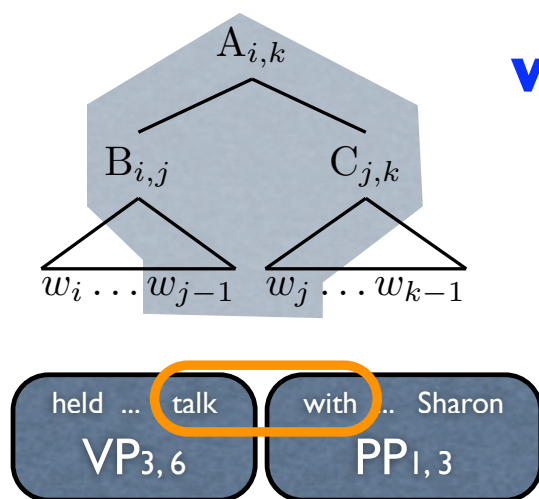
$$\mathbf{w} \cdot \mathbf{f}_N(\text{tree}) = 0.5$$



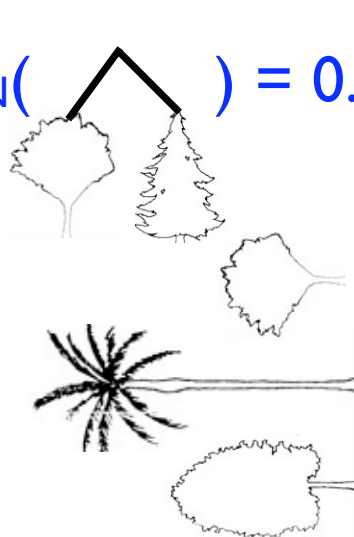
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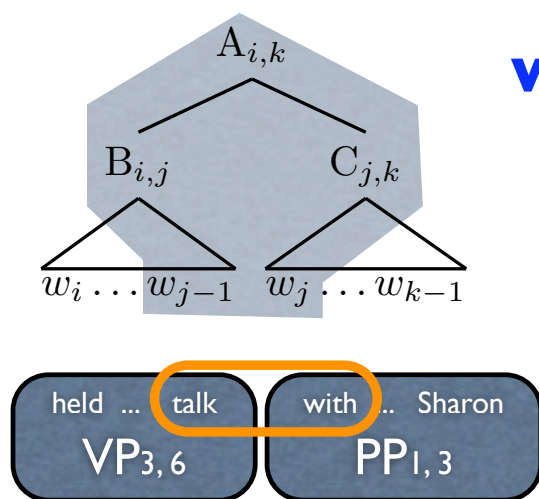
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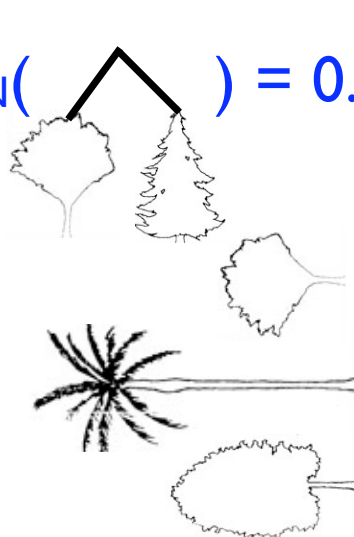
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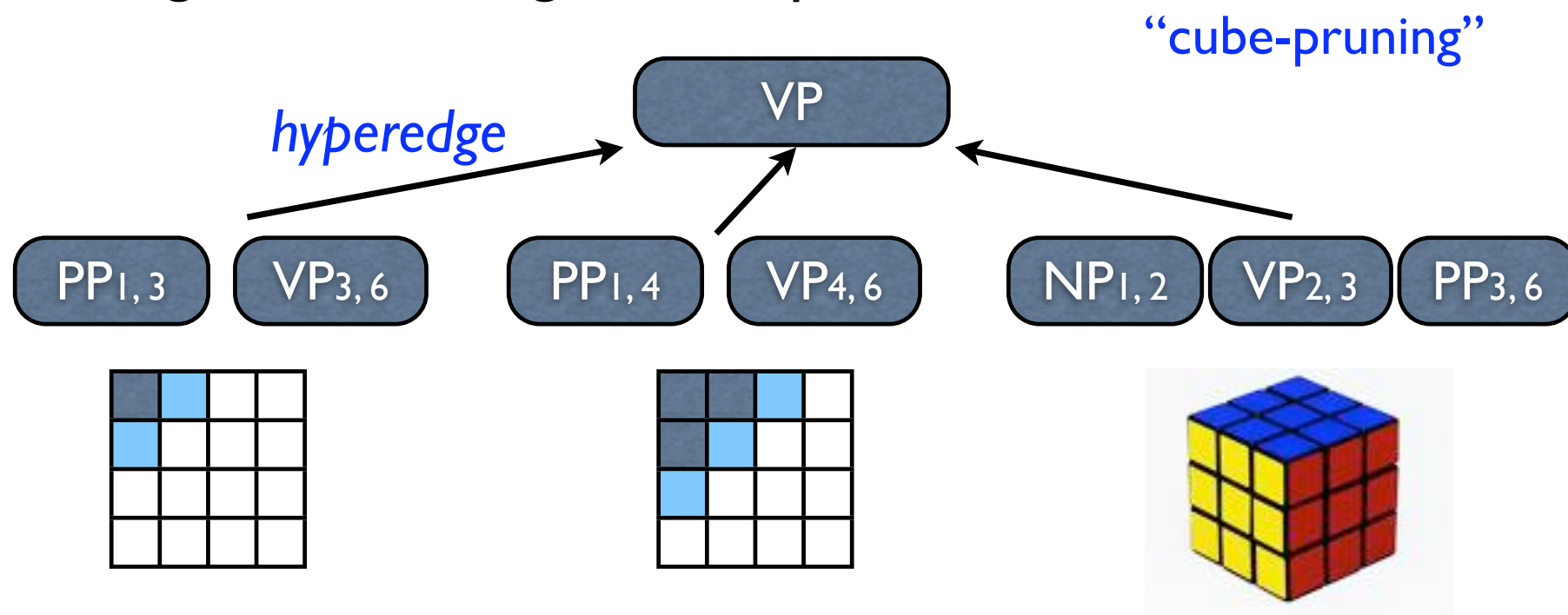
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Approximate Decoding

- process all hyperedges **simultaneously!**
significant savings of computation



complexity: $O(E + V \mathbf{U} k \log k)$,

bottom-neck: the time for on-the-fly extraction

Forest Oracle

the candidate tree that is closest to gold-standard

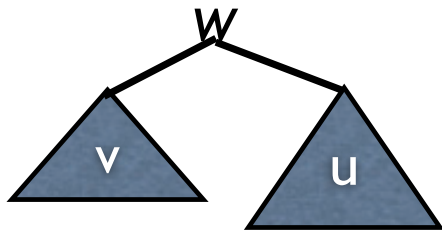
Optimal Parseval F-score

- find the tree in the forest with highest F-score
- Parseval F_1 -score is the harmonic mean between labeled precision and labeled recall
 - can not optimize F-scores on sub-forests separately
 - can not optimize precision and recall simultaneously
- we instead use **dynamic programming**
 - optimizes the number of matched brackets per given number of test brackets
 - “when the test (sub-) parse has 5 brackets, what is the max. number of matched brackets?”

Combining Oracle Functions

- to combine two nodes along a hyperedge, we need to **distribute** test brackets between the two, and **optimize** the number of matches

$$(f \otimes g)(t) \triangleq \max_{t_1+t_2=t} f(t_1) + g(t_2)$$



t	f(t)
2	1
3	2

\otimes

t	g(t)
4	4
5	4

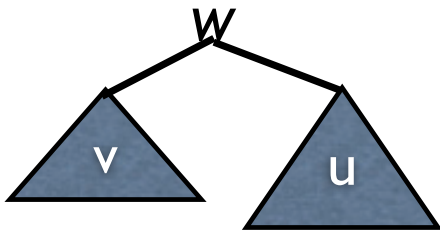
=

t	$(f \otimes g)(t)$
6	5
7	6
8	6

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6	5
7	6
8	6

N

t	$(f \otimes g)^{\uparrow(1,0)}(t)$
7	5
8	6
9	6

ora[w]

this node matched?

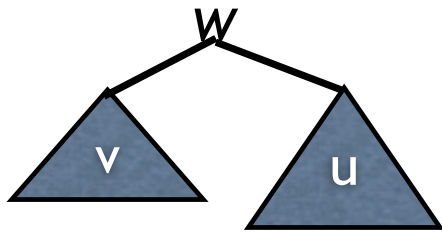
Y

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8	7
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final answer:

$$F(y^+, y^*) = \max_t \frac{2 \cdot \text{ora}[\text{TOP}](t)}{t + |y^*|}$$

N

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9	6

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