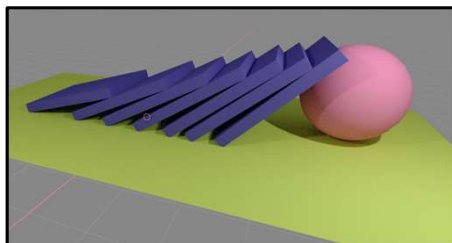
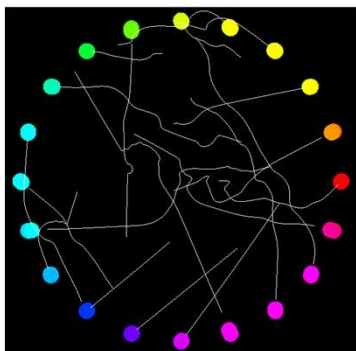


# Animation

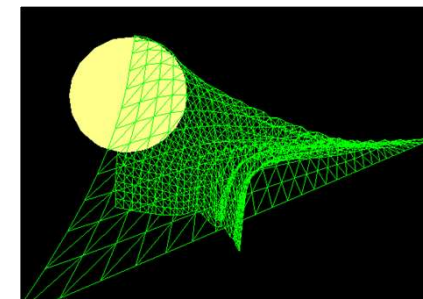
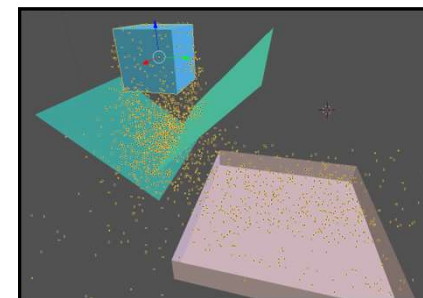


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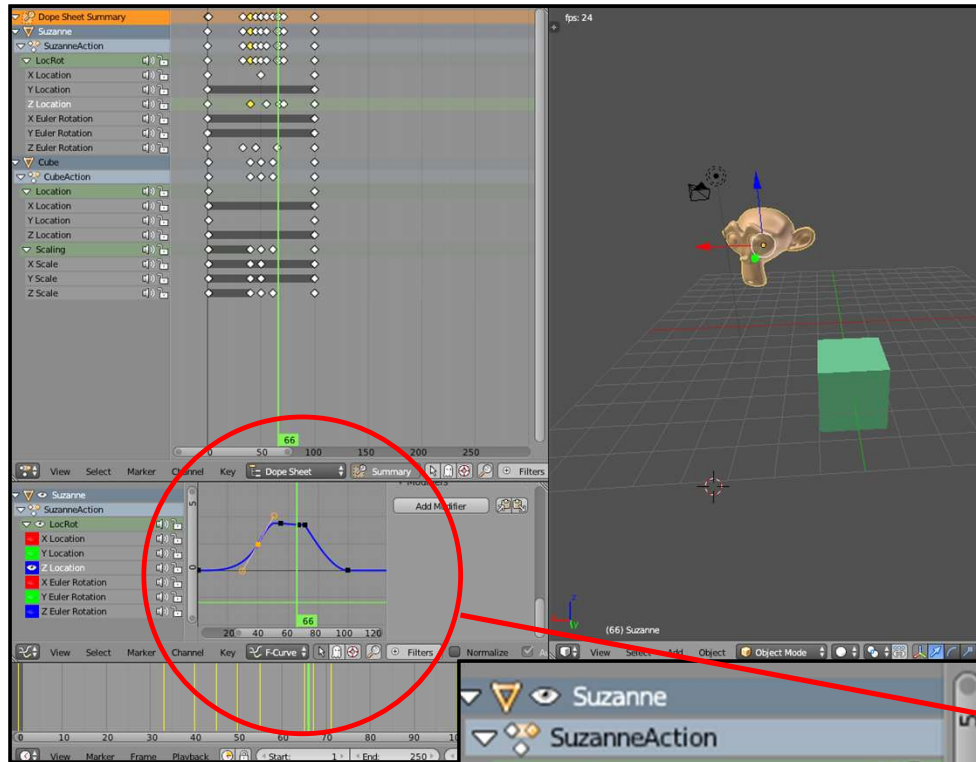
## Animation

Animation is the process of giving motion to your geometric models. Before animating, there are questions you need to ask first:

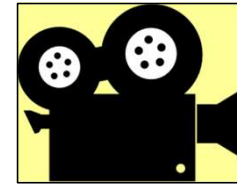
- Why am I doing this?
- Do I want the animation to obey the real laws of physics? Partially? Which elements?
- Am I willing to “fake” the physics to get the objects to *want* to move in a way that I tell it?
- Do I have specific key positions I want the objects to pass through no matter what?
- Do I want to simply record the motion of a real person, animal, etc., and then play it back?



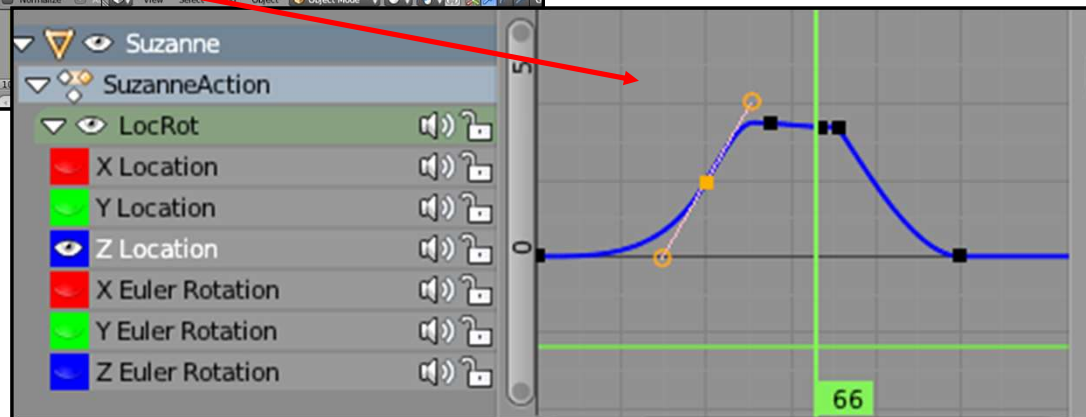
## Keyframe Animation



These icons refer to explanatory videos on the class web site



anim2.mp4

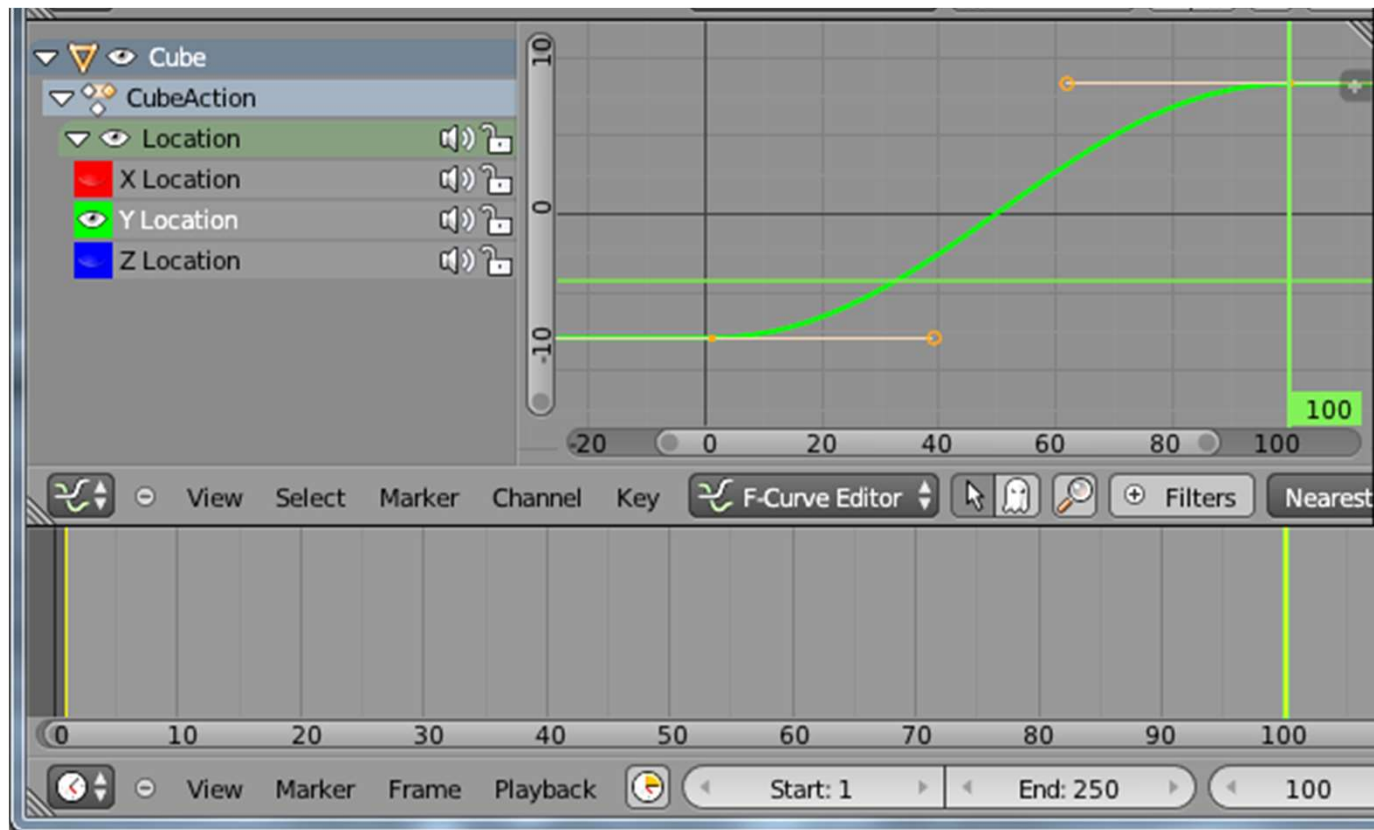


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# Keyframe Animation

4

Blender:



## Here's Some Code that Lets You Create DIY Keyframe Animations

For my own work, instead of *Key Frames*, I like specifying *Key Times* better.  
And, so, I created a C++ class to do it for you.

**class Keytimes:**

```
void AddTimeValue( float time, float value );  
float GetFirstTime( );  
float GetLastTime( );  
int GetNumKeytimes( );  
float GetValue( float time );  
void Init( );  
void PrintTimeValues( );
```



## Instead of Key Frames, I Like Specifying Key Times Better

```

Keytimes Xpos;
int
main( int argc, char *argv[ ] )
{
    Xpos.Init( );
    Xpos.AddTimeValue( 0.0, 0.000 );
    Xpos.AddTimeValue( 2.0, 0.333 );
    Xpos.AddTimeValue( 1.0, 3.142 );
    Xpos.AddTimeValue( 0.5, 2.718 );
    fprintf( stderr, "%d time-value pairs:\n", Xpos.GetNumKeytimes( ) );
    Xpos.PrintTimeValues( );

    fprintf( stderr, "Time runs from %8.3f to %8.3f\n", 0.0, 2.0 );
    for( float t = 0.; t <= 2.0; t += 0.1 )
    {
        float v = Xpos.GetValue( t );
        fprintf( stderr, "%8.3ft%8.3fn", t, v );
    }
}

```

← Declare one class per parameter you are animating. Here it wants to interpolate and animate the x-location of something.

Key-Time pairs (Time and Xlocation) can be specified in any order

← Just to demonstrate, this for-loop runs through a collection of time values and looks up the interpolate x-location at those values. Normally you would get the time from the system clock.



## Instead of Key Frames, I Like Specifying Key Times Better

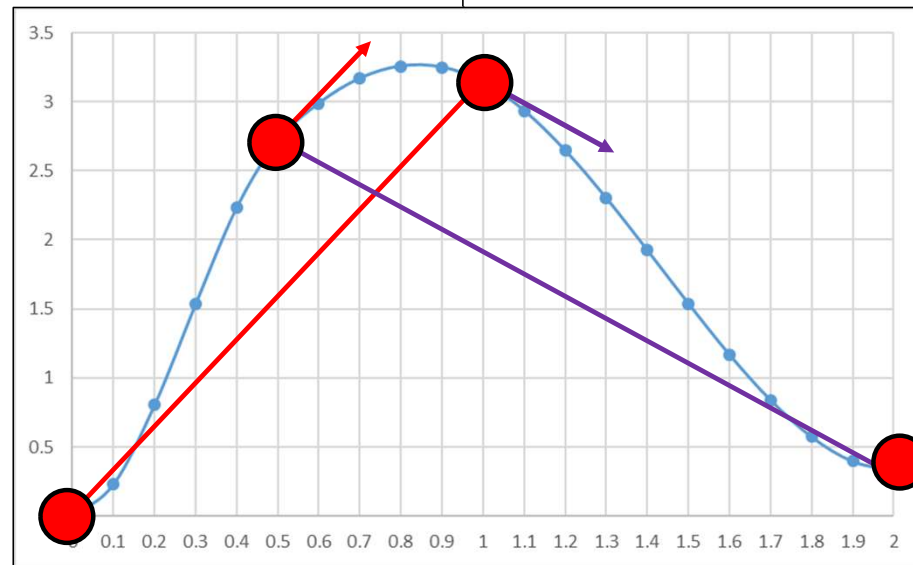
( 0.00, 0.000)  
 ( 0.00, 0.000) ( 2.00, 0.333)  
 ( 0.00, 0.000) ( 1.00, 3.142) ( 2.00, 0.333)  
 ( 0.00, 0.000) ( 0.50, 2.718) ( 1.00, 3.142) ( 2.00, 0.333)

4 time-value pairs

Time runs from 0.000 to 2.000

0.000	0.000
0.100	0.232
0.200	0.806
0.300	1.535
0.400	2.234
0.500	2.718
0.600	2.989
0.700	3.170
0.800	3.258
0.900	3.250
1.000	3.142
1.100	2.935
1.200	2.646
1.300	2.302
1.400	1.924
1.500	1.539
1.600	1.169
1.700	0.840
1.800	0.574
1.900	0.397
2.000	0.333

● = the originally-specified key-time pairs



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## Using the System Clock in Display( ) for Timing

```

#define MSEC      10000           // i.e., 10 seconds
Keytimes Xpos, Ypos, Zpos;
Keytimes ThetaX, ThetaY, ThetaZ;

...

if( AnimationIsOn )
{
    // # msec into the cycle ( 0 - MSEC-1 ):
    int msec = glutGet( GLUT_ELAPSED_TIME ) % MSEC;

    // turn that into a time in seconds:
    float nowTime = (float)msec / 1000.;
    glPushMatrix( );
        glTranslatef( Xpos.GetValue( nowTime ), Ypos.GetValue( nowTime ), Zpos.GetValue( nowTime )
    );
        glRotatef( ThetaX.GetValue( nowTime ), 1., 0., 0. );
        glRotatef( ThetaY.GetValue( nowTime ), 0., 1., 0. );
        glRotatef( ThetaZ.GetValue( nowTime ), 0., 0., 1. );
        << draw the object >>
    glPopMatrix( );
}

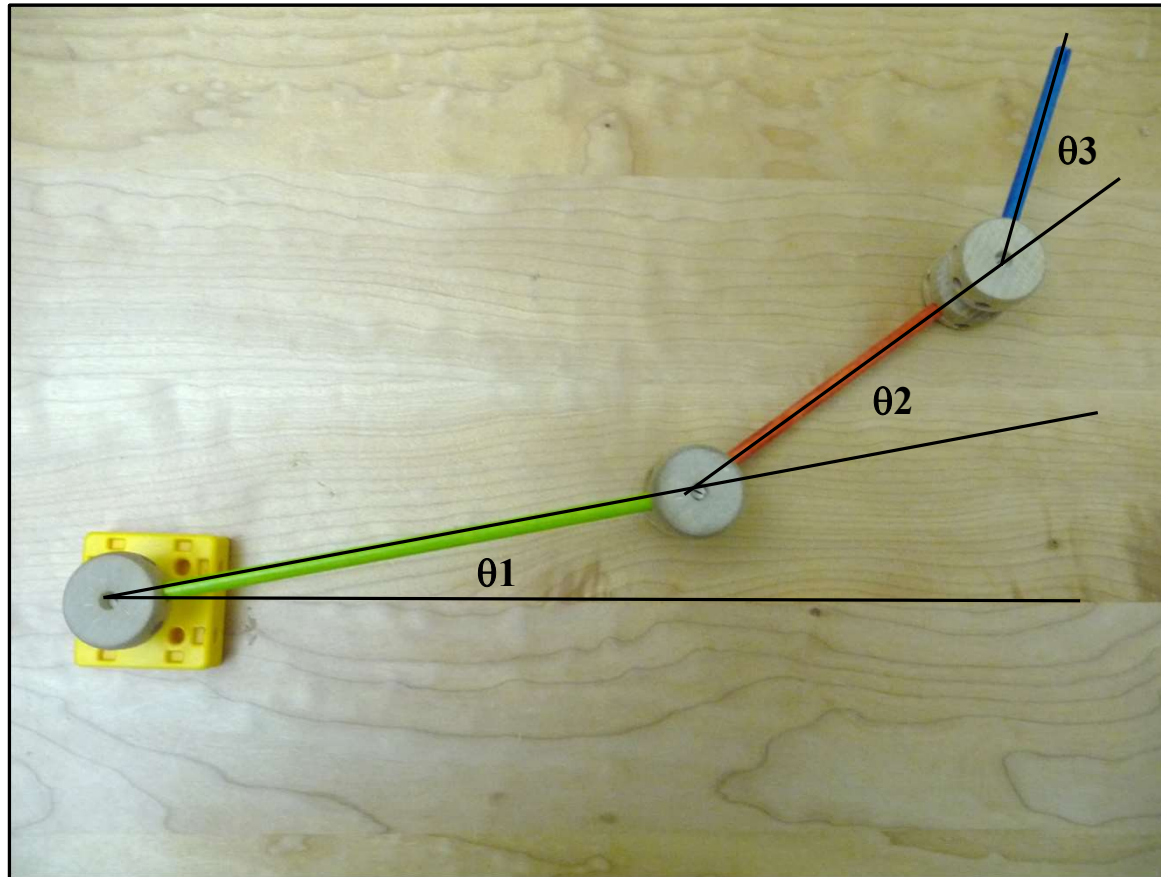
```

Number of msec in the animation cycle

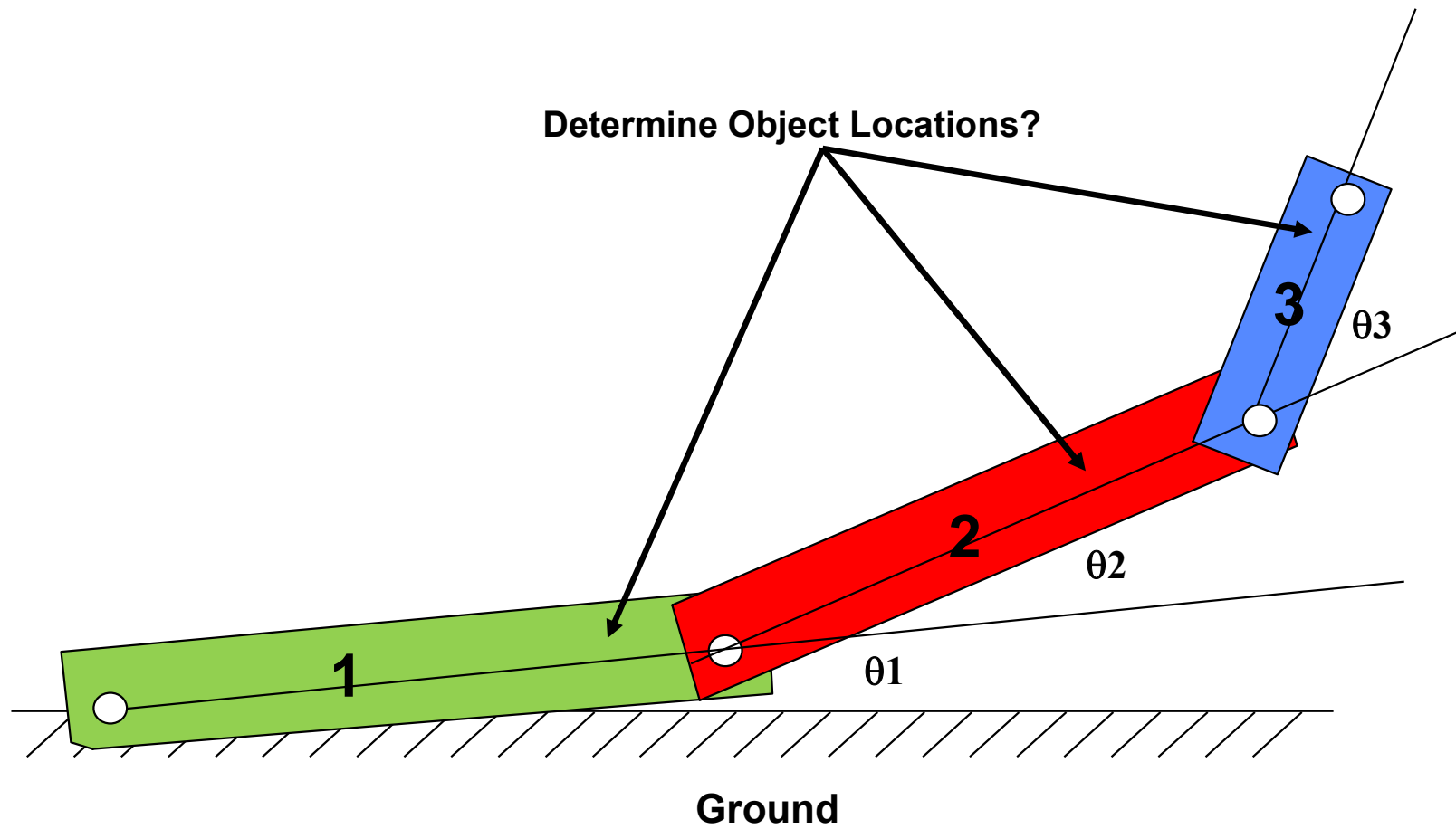




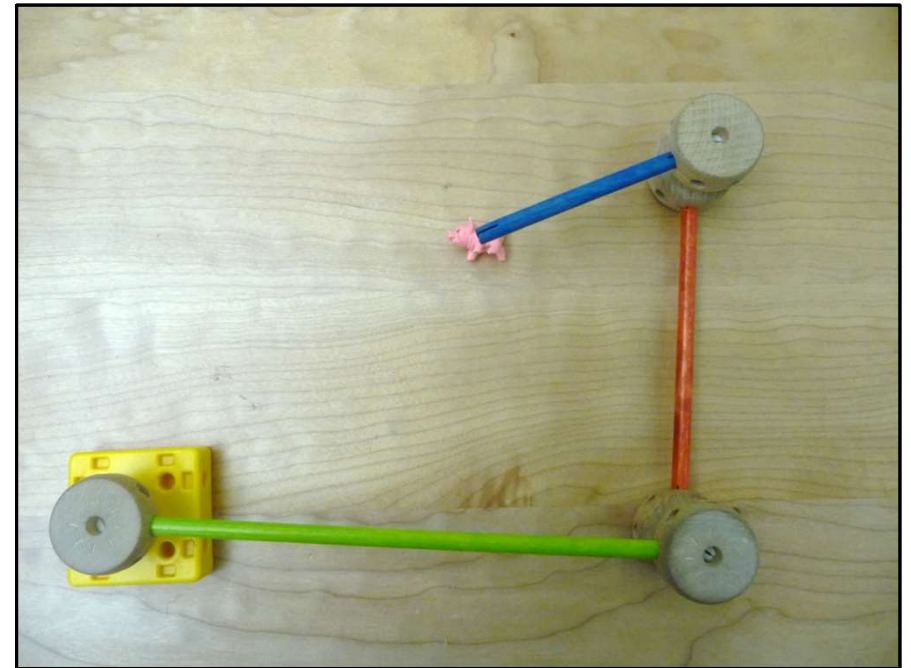
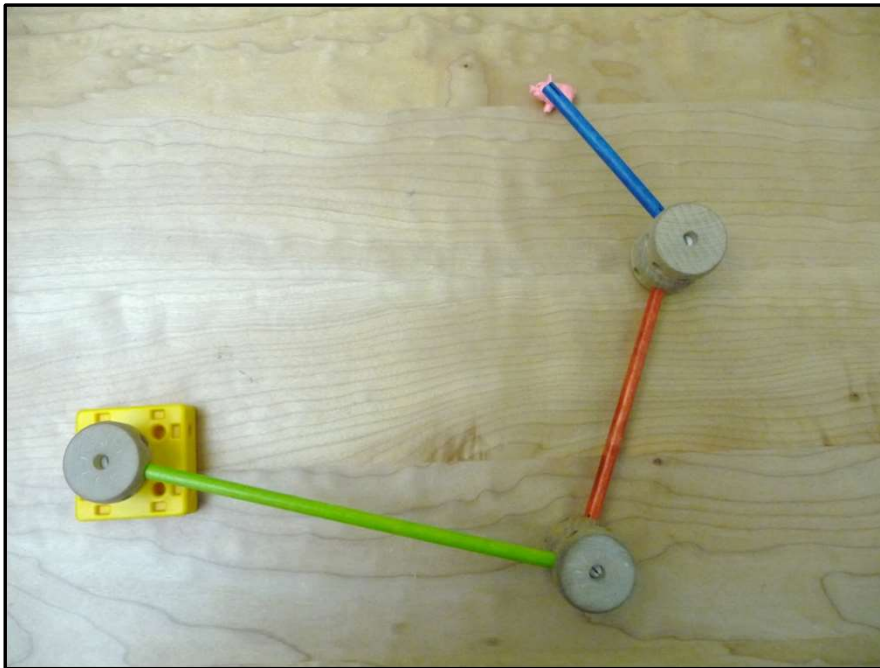
**Forward Kinematics:  
Change Parameters – Connected Things Move  
(All children understand this)**



## Forward Kinematics: Transformation Hierarchies



## Inverse Kinematics (IK): Things Need to Move to a Particular Location – What Parameters Will Make Them Do That?



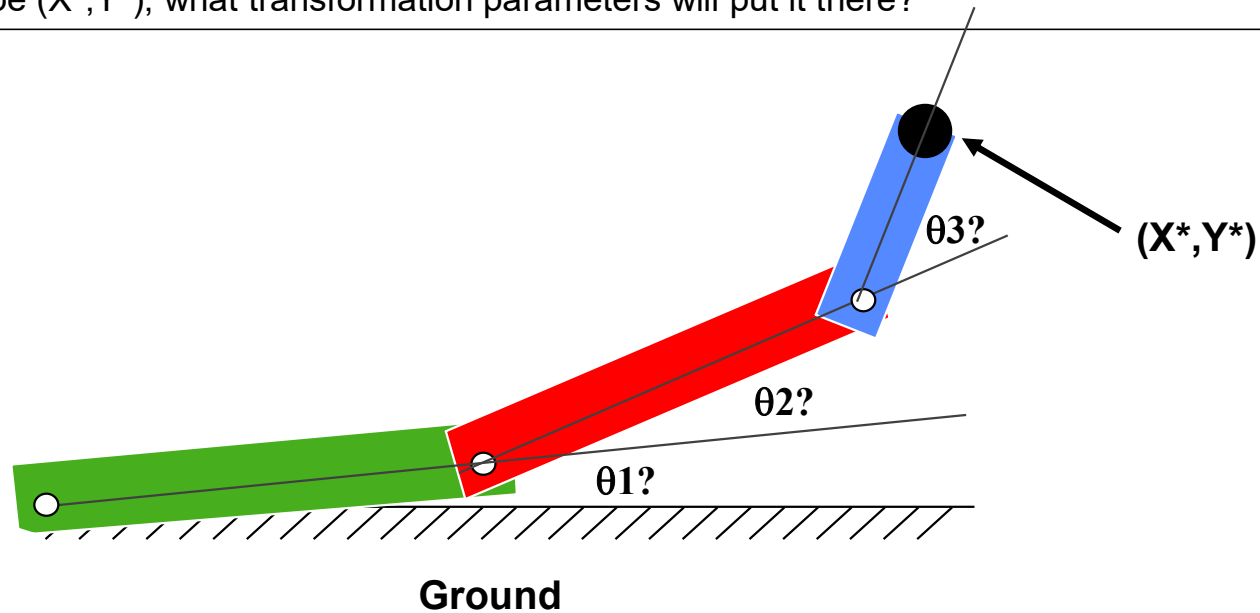
Of course, there will always be target locations that can *never* be reached.  
Think about that spot in the middle of your back that you can never scratch! 😊



## Inverse Kinematics (IK)

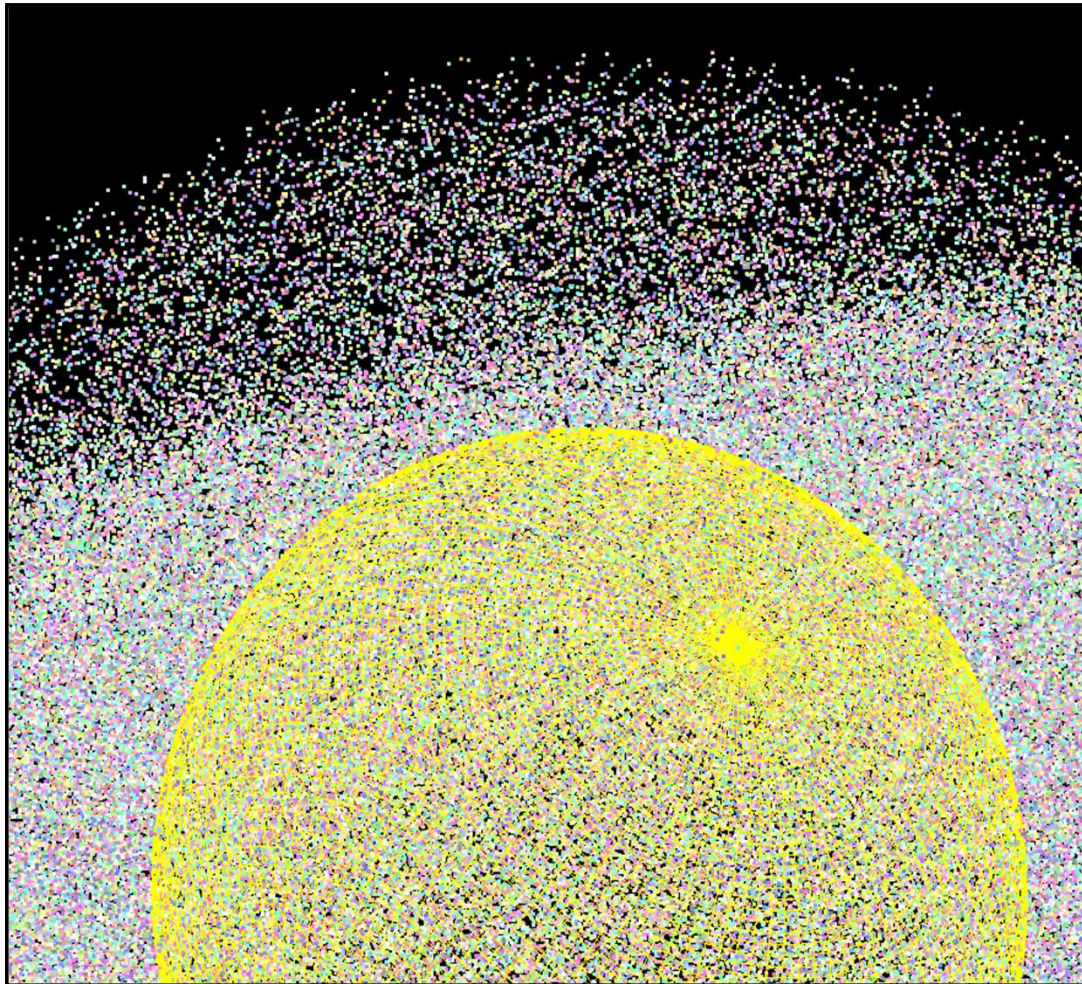
**Forward Kinematics** solves the problem “if I know the link transformation parameters, where are the links?”.

**Inverse Kinematics (IK)** solves the problem “If I know where I want the end of the chain to be  $(X^*, Y^*)$ , what transformation parameters will put it there?”



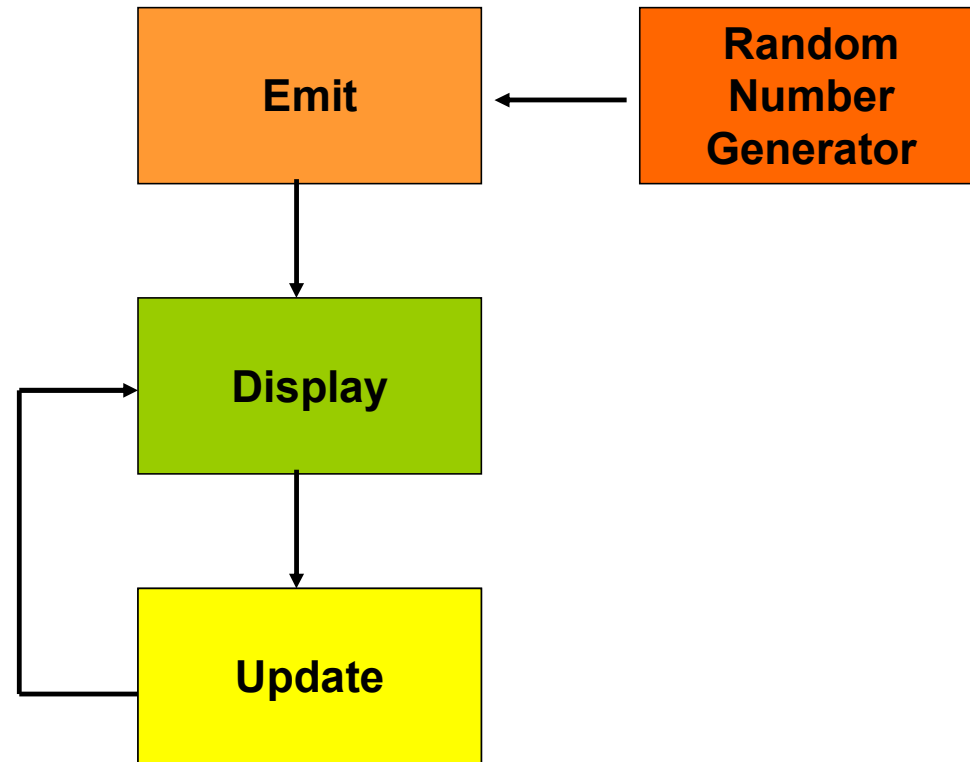


## Particle Systems: A Cross Between Modeling and Animation?

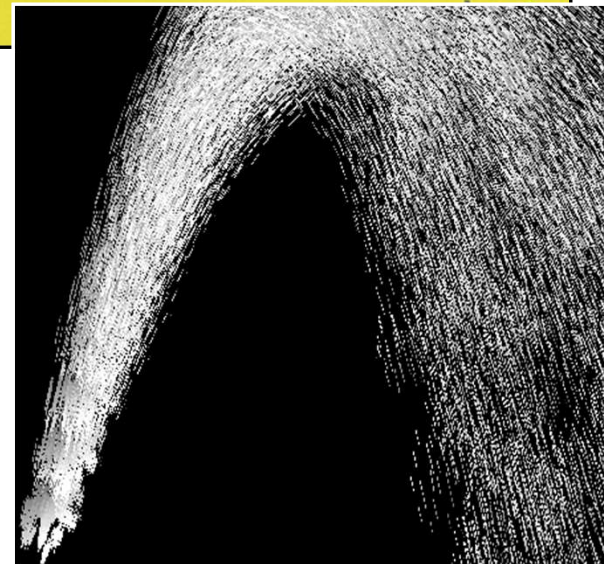
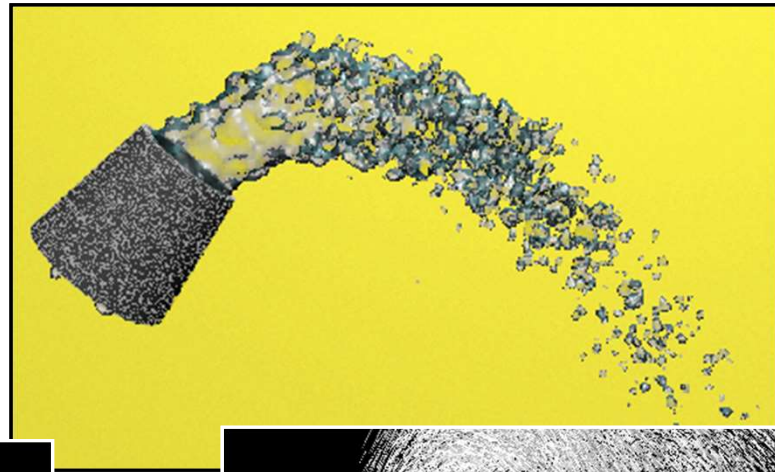
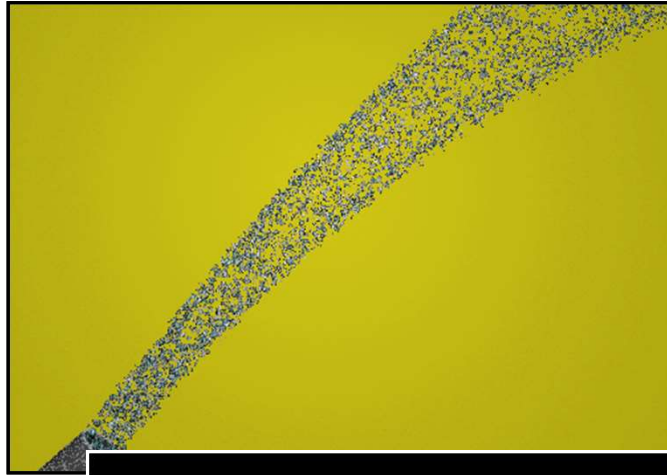


## Particle Systems: A Cross Between Modeling and Animation?

The basic process is:



## Particle Systems Examples

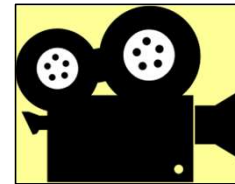
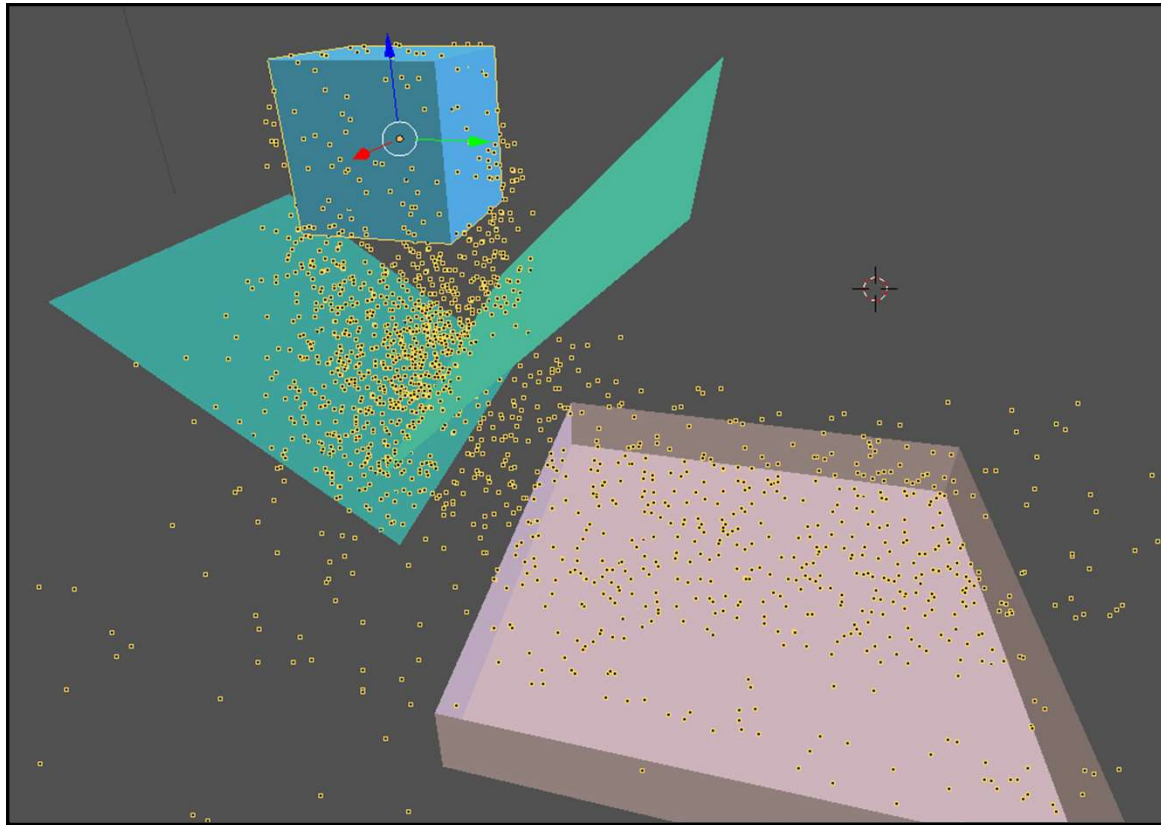


Chuck Evans





## Particle Systems Examples



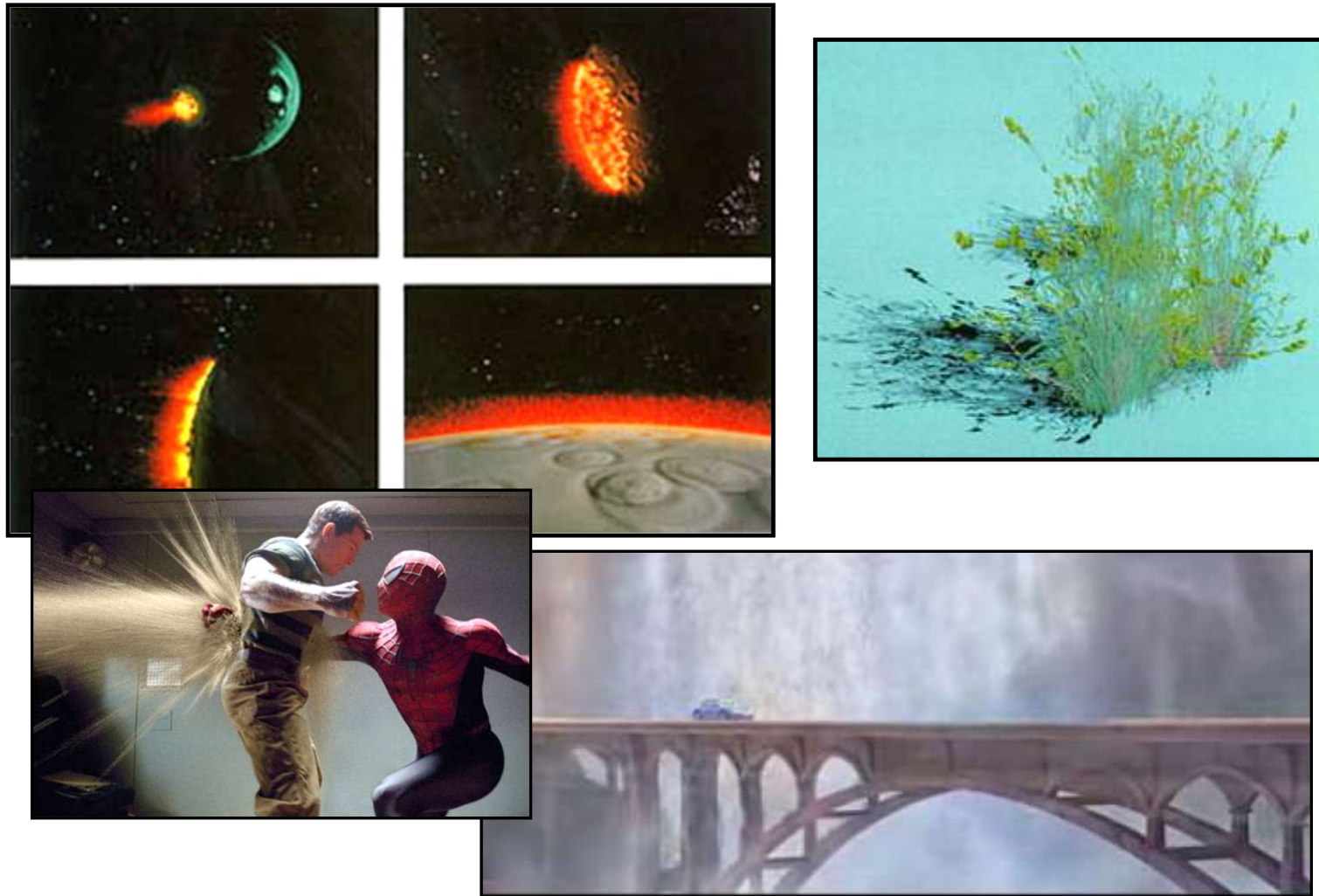
particles.mp4



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## Particle Systems Examples



## Particle Systems Examples



*The Lion King* (2019) -- Disney



## A Particle System to Simulate Colliding Galaxies in *Cosmic Voyage*



*Cosmic Voyage*



## Particles Don't Actually Have to Be “Particles”



*Avatar*



*The Lion King*

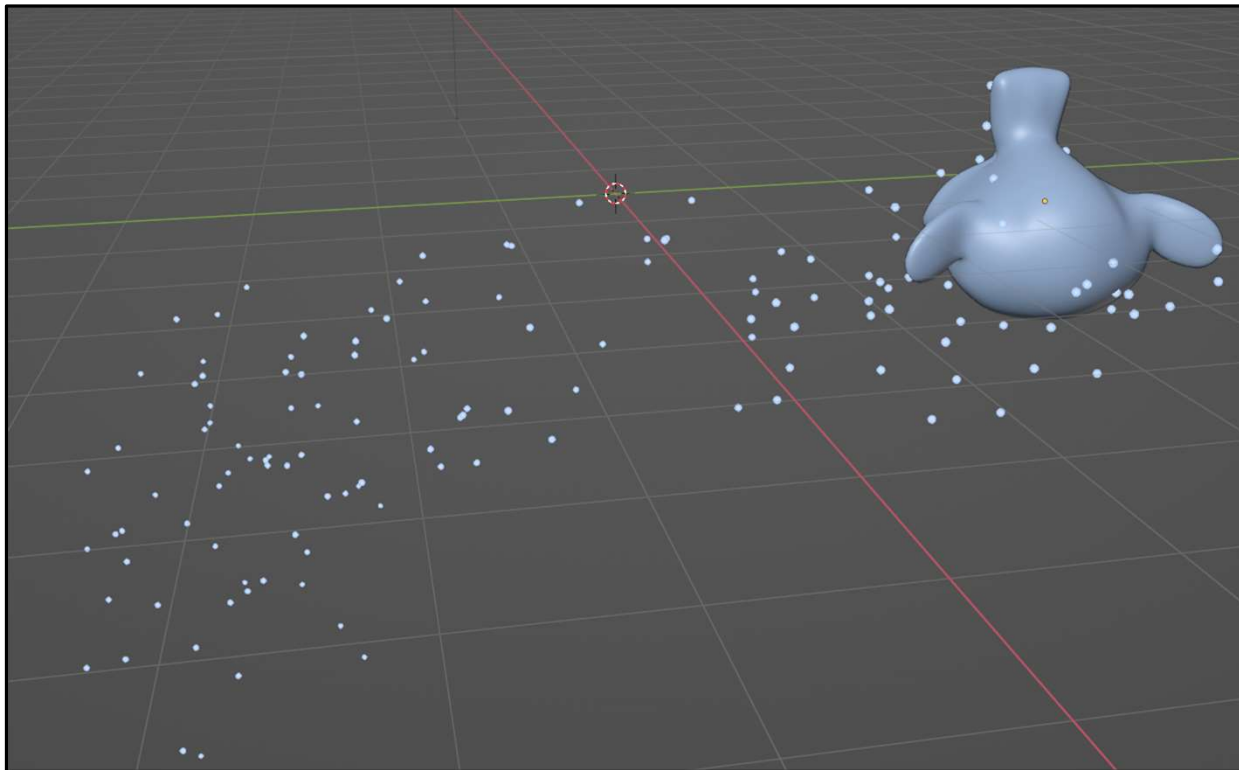


*Mulan*



## Multiple Animation Techniques Can Be Combined

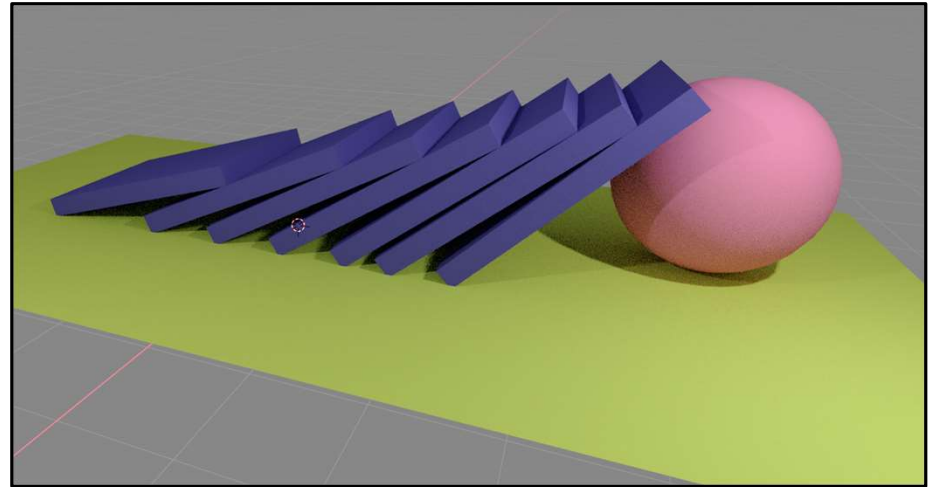
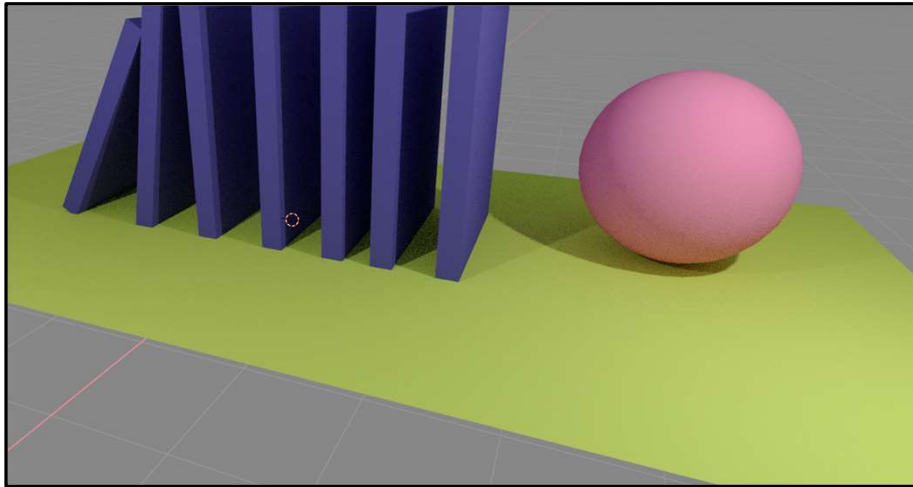
A Particle System coming from a moving keyframed object in Blender:





## Animating using Rigid-body Physics

22



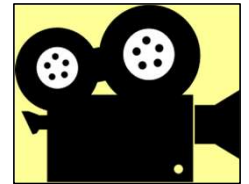
Newton's second law:

force = mass \* acceleration

or

$\ddot{x}$  = acceleration = force / mass

$$x(T) = \iint_{t=0}^{t=T} \ddot{x} dt \approx \sum \sum \ddot{x} \Delta t$$



dominos.mp4

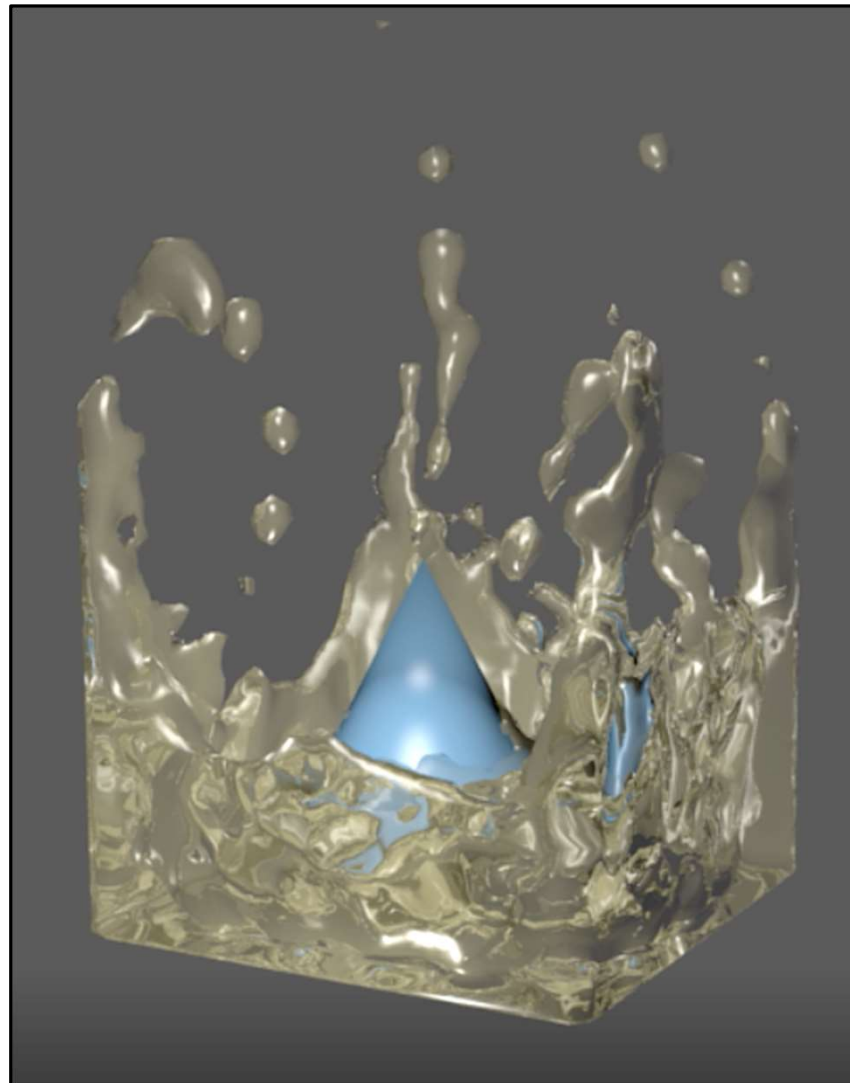


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In order to make this work, you need to supply physical properties such as mass, center of mass, moment of inertia, coefficients of friction, coefficients of restitution, etc.

## Animating using Fluid Physics

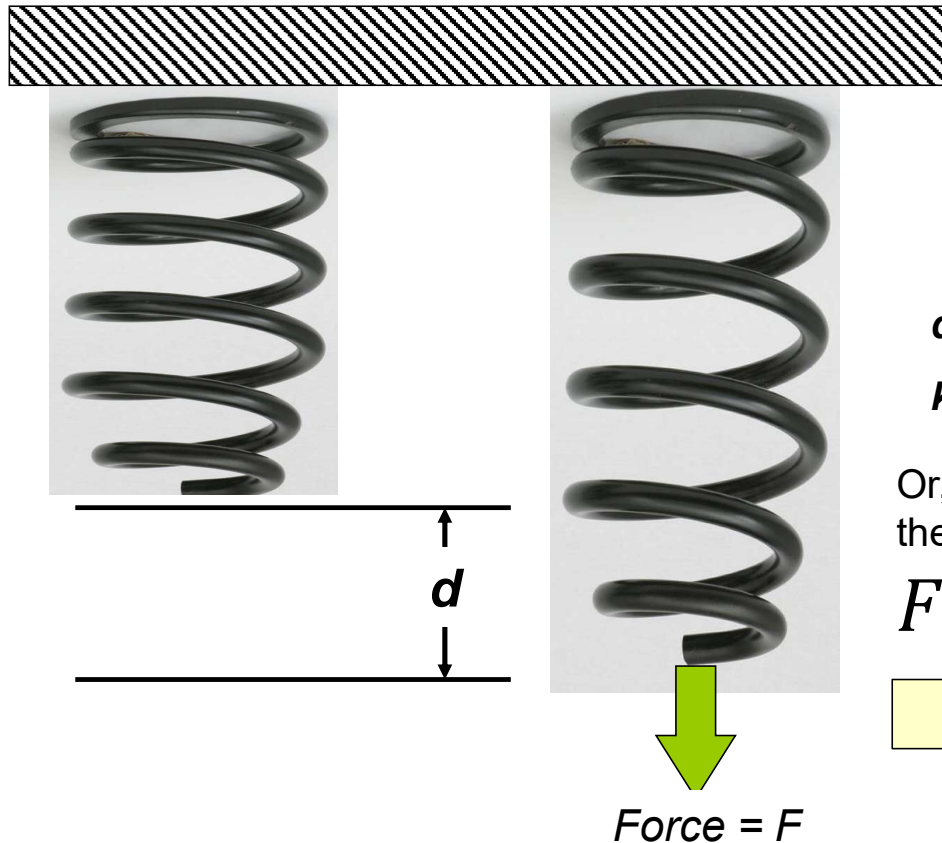
23



fluid.avi



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$$d = \frac{-F}{k}$$

$d$  = **spring displacement** in inches

$k$  = **spring stiffness** in pounds/inch

Or, if you know the displacement,  
the force exerted by the spring is:

$$F = -kd$$

This is known as **Hooke's Law**

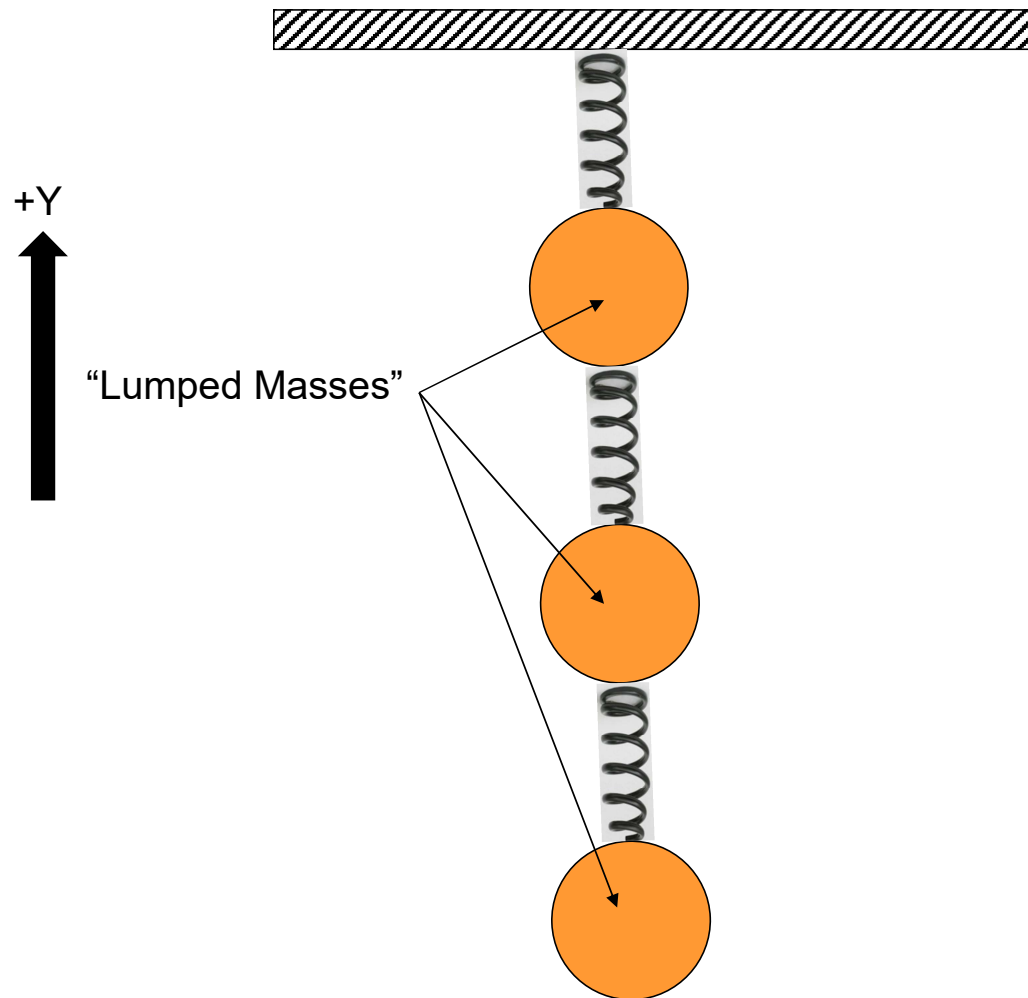
Why the minus sign? Because a spring's force acts in a direction opposite the displacement. In other words, a spring's force tries to correct its displacement.



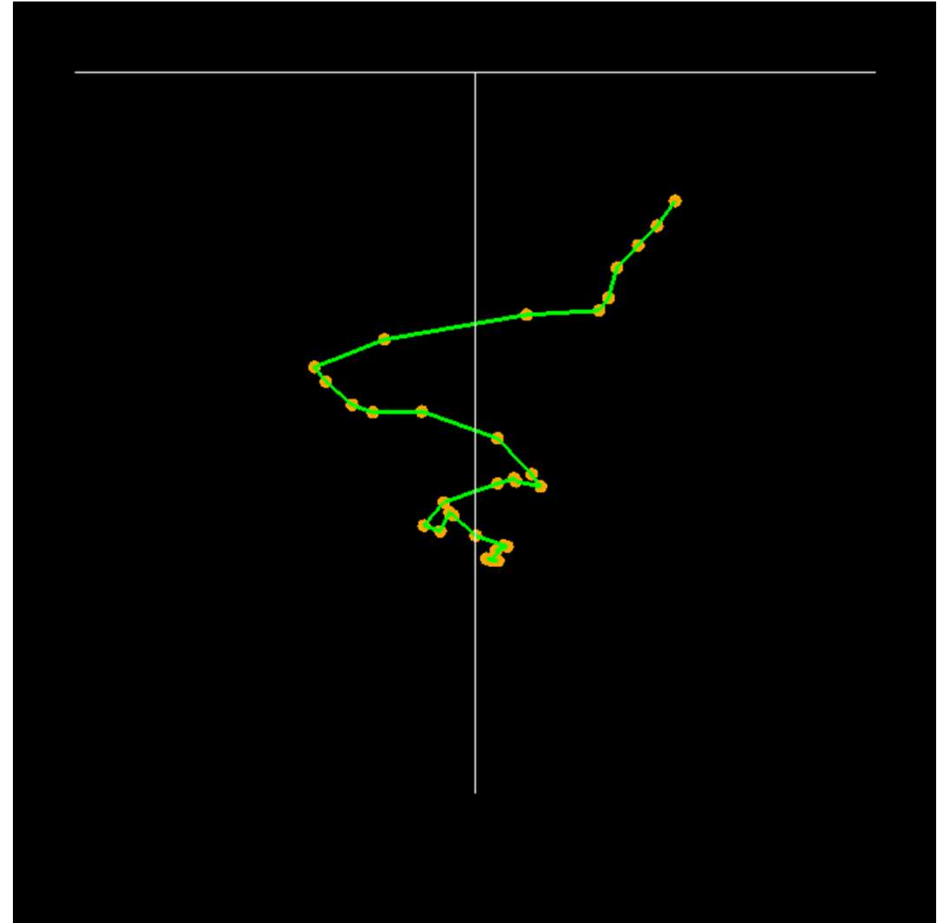
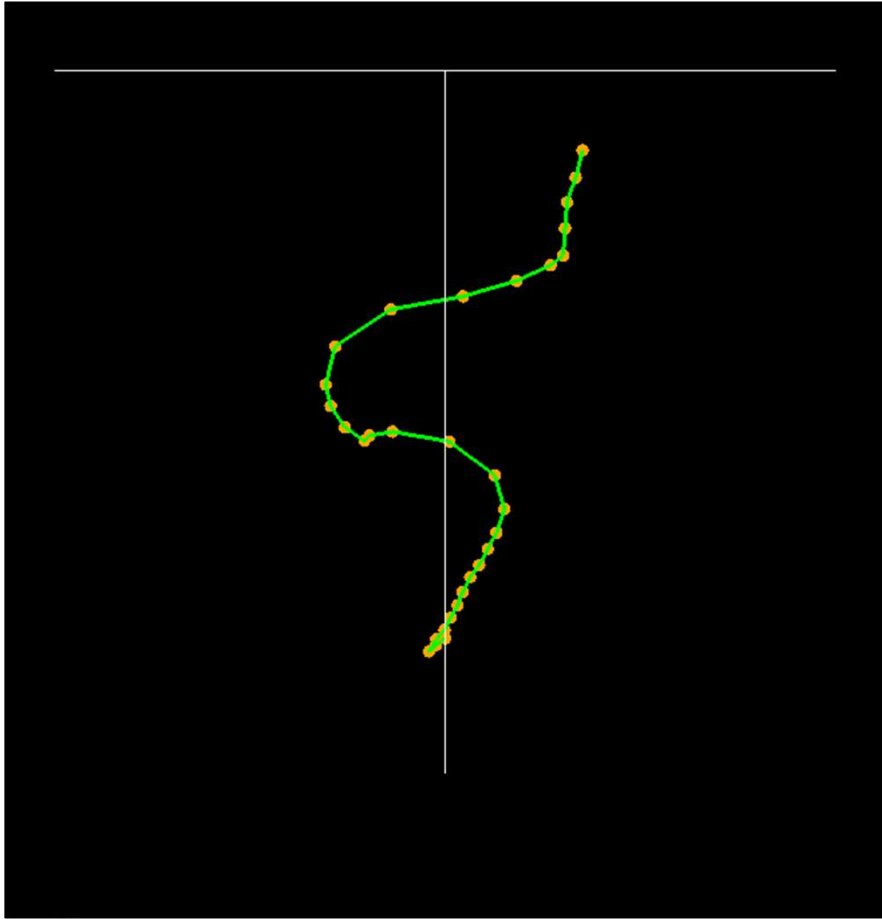


## Animating using the Physics of a Mesh of Springs

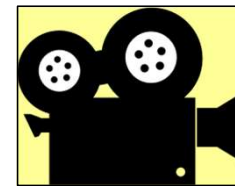
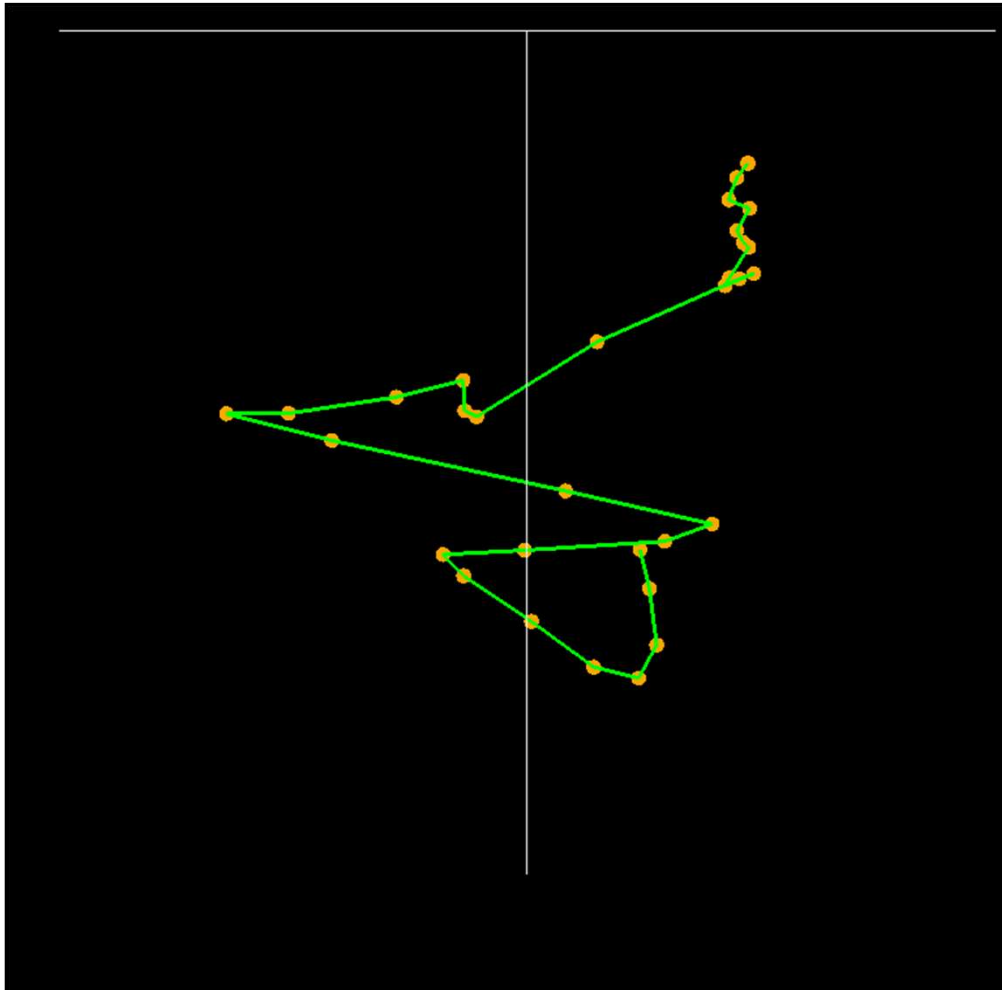
25



## Simulating a Bouncy String or a Chain



## Simulating a Bouncy String or a Chain

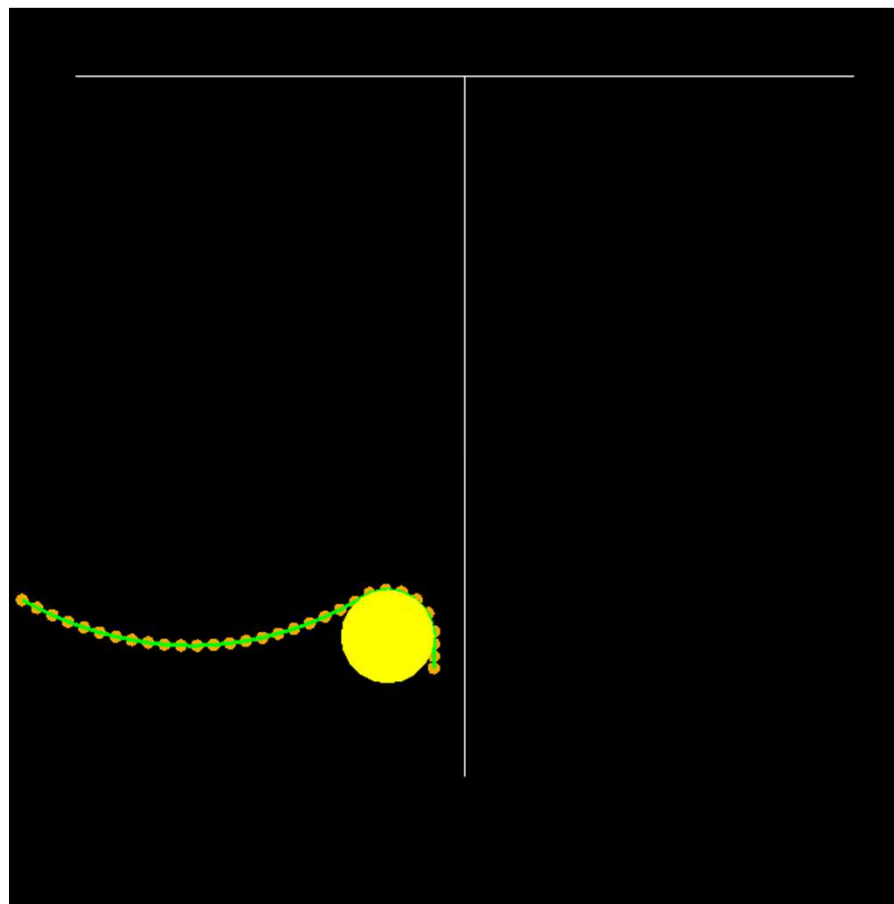
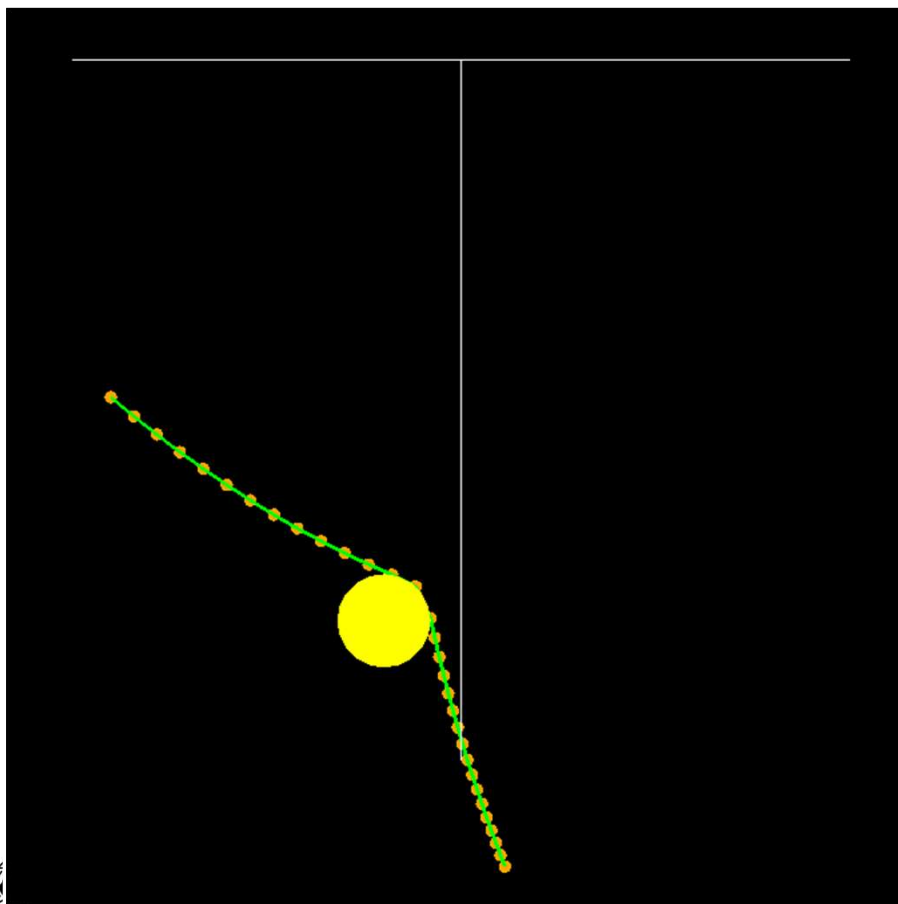


string.mp4

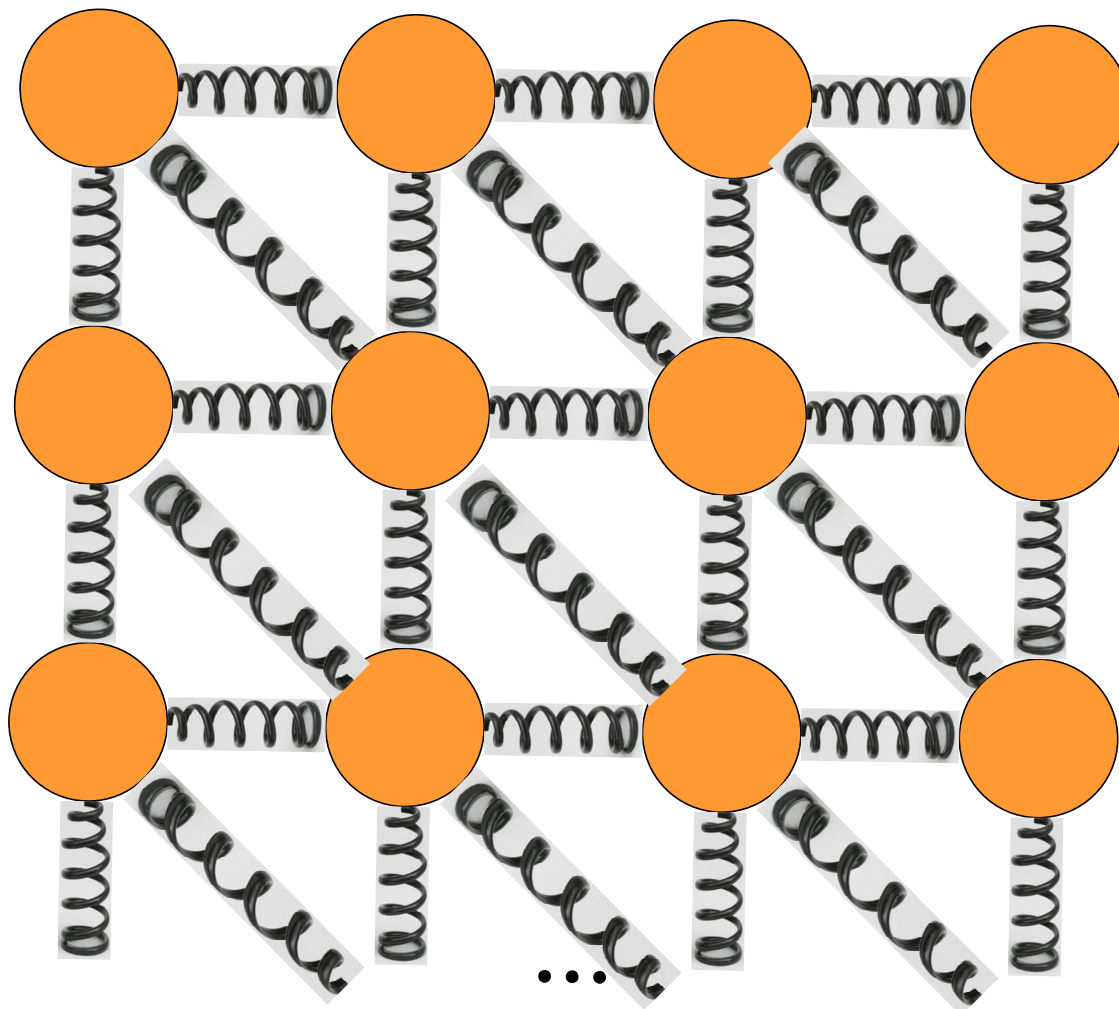


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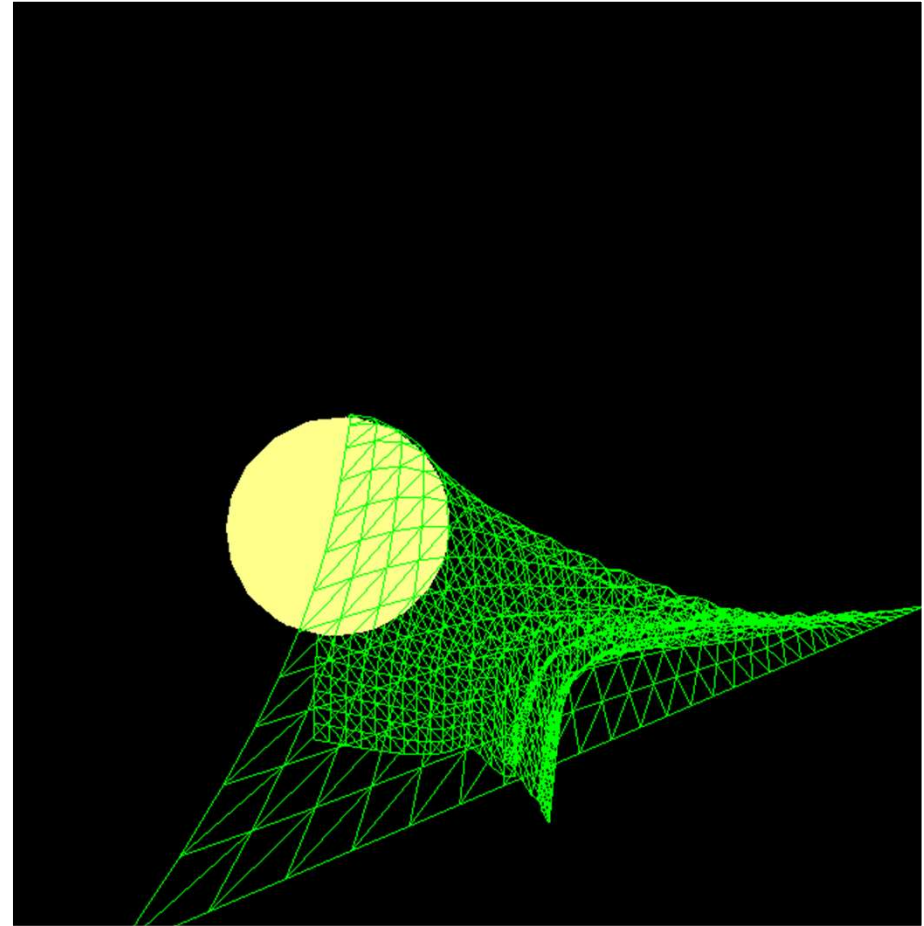
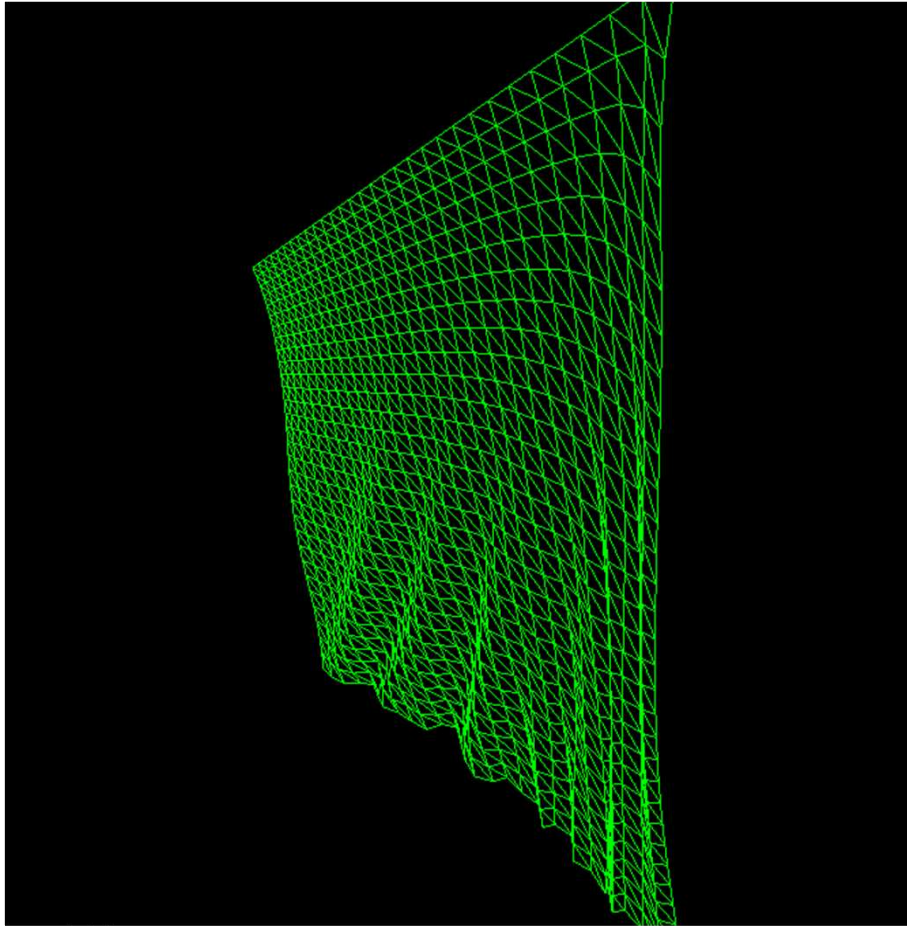
## Placing a Physical Barrier in the Scene



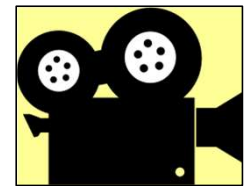
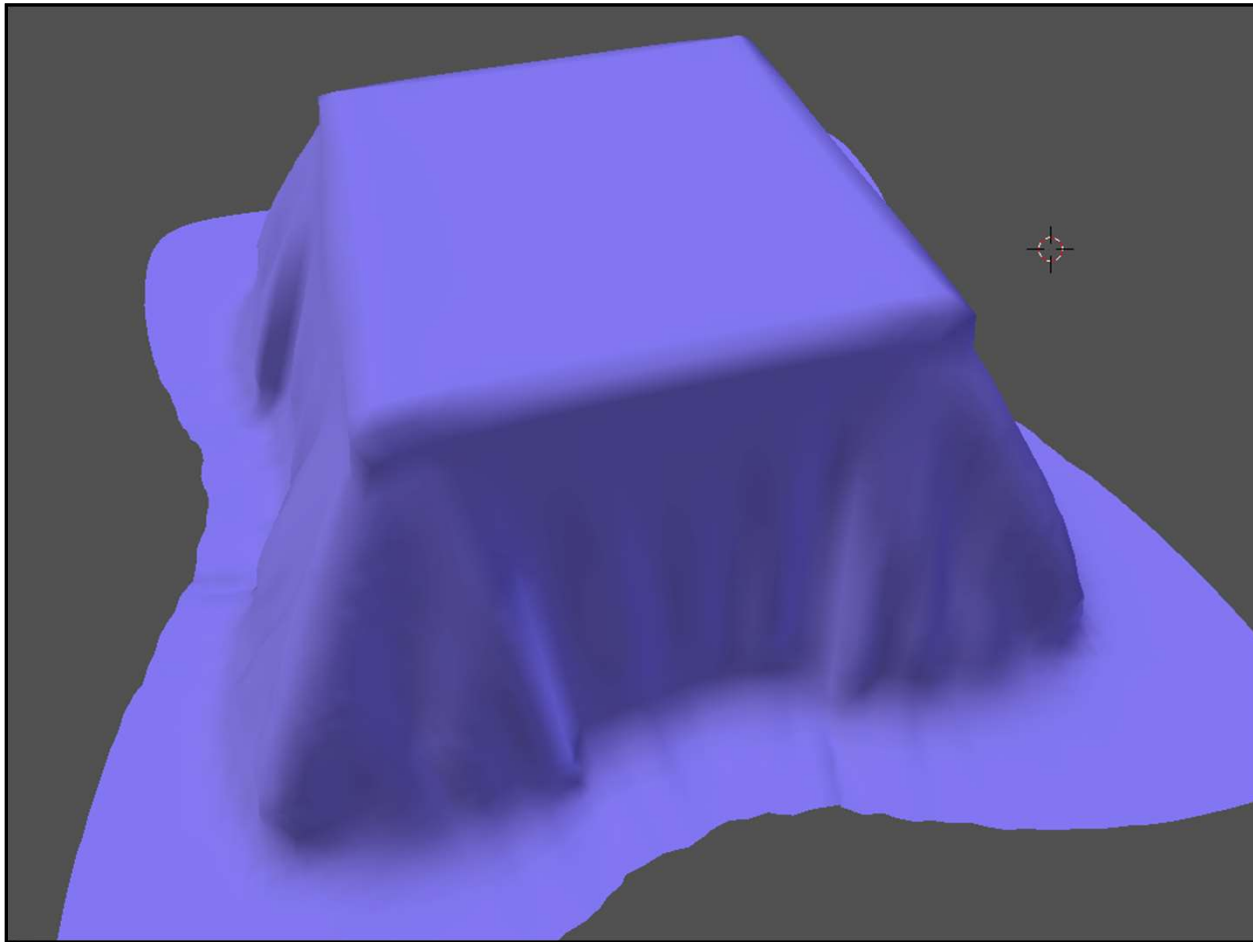
## Animating Cloth



## Cloth Examples



## Cloth Example



cloth.mp4



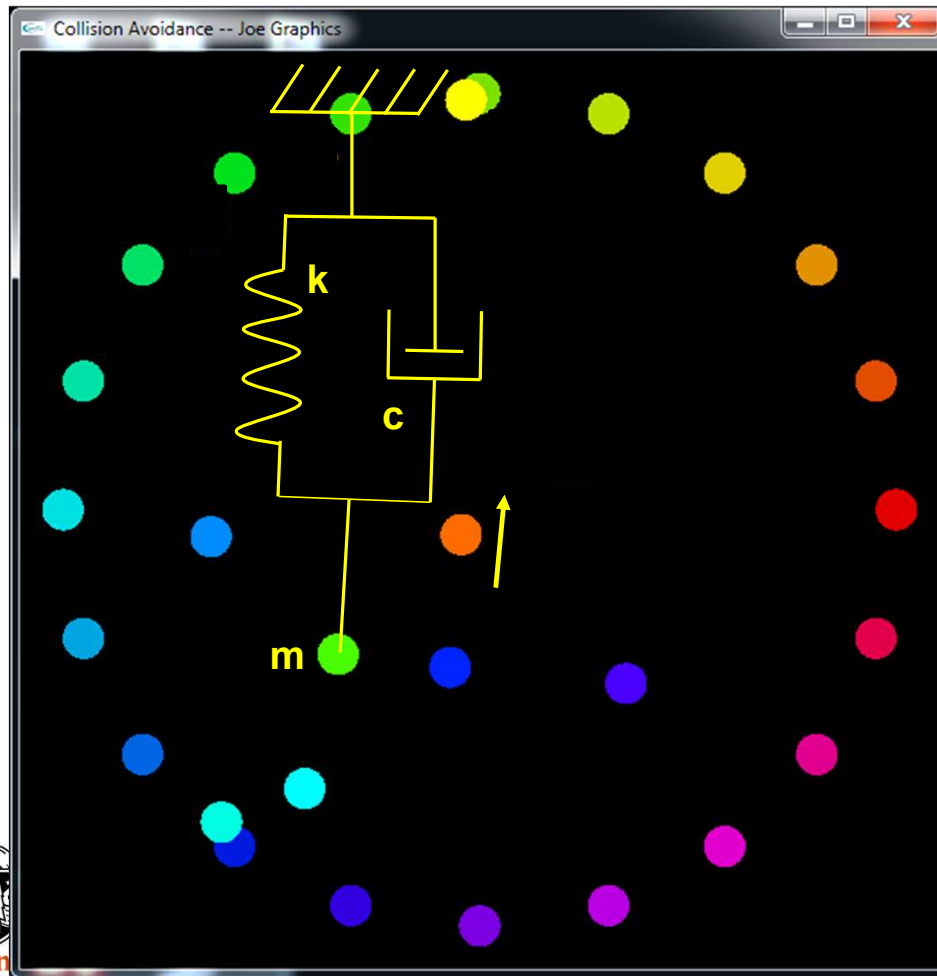
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## Cloth Example





## Functional Animation: Setup Imaginary Physics to Make the Object *Want* to Move Towards a Goal Position



Newton's second law:

$$\text{force} = \text{mass} * \text{acceleration}$$

or

$$\ddot{x} = \text{acceleration} = \text{force} / \text{mass}$$

$$\ddot{x} = \frac{-c\dot{x} - kx}{m}$$

- The **k** is an imaginary spring.
- The **c** is an imaginary “damper”, which you can think of as a shock absorber which absorbs energy. (Your car has these to soften bouncing.)



## Functional Animation: Setup Imaginary Physics to Make the Object *Want* to Move Away from all other Objects

Newton's second law:

$$\text{force} = \text{mass} * \text{acceleration}$$

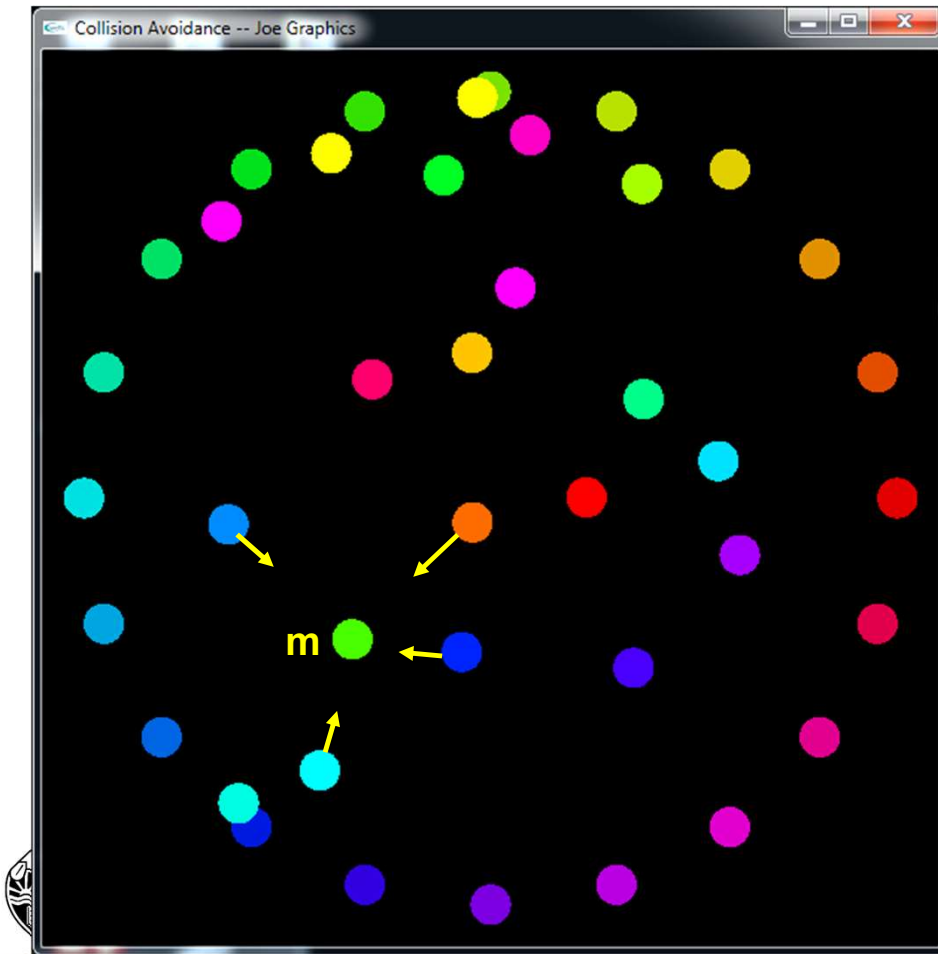
or

$$\ddot{x} = \text{acceleration} = \text{force} / \text{mass}$$

$$\ddot{x} = \frac{F_{\text{repulsive}}}{m}$$

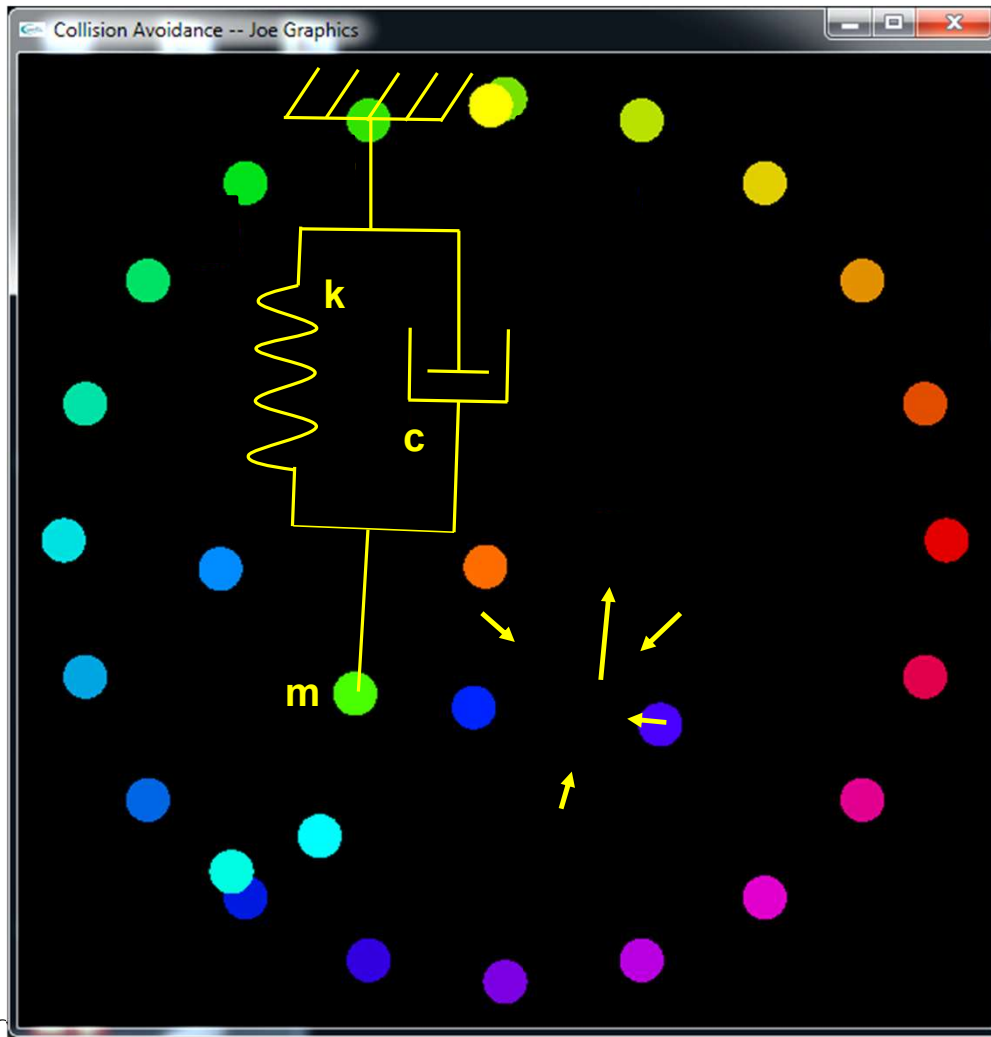
$$F_{\text{repulsive}} = \frac{\overset{\substack{\text{Repulsion Coefficient} \\ \downarrow}}{C_{\text{repulse}}}}{d^{\overset{\substack{\text{Repulsion Exponent} \\ \nwarrow}}{\text{Power}}}}$$

Distance between the boundaries of the 2 bodies



This isn't from a book. I just made this up. It seemed like a good idea.

**Total Goal – Make the Free Body Move Towards its Final Position  
While Being Repelled by the Other Bodies**



Newton's second law:

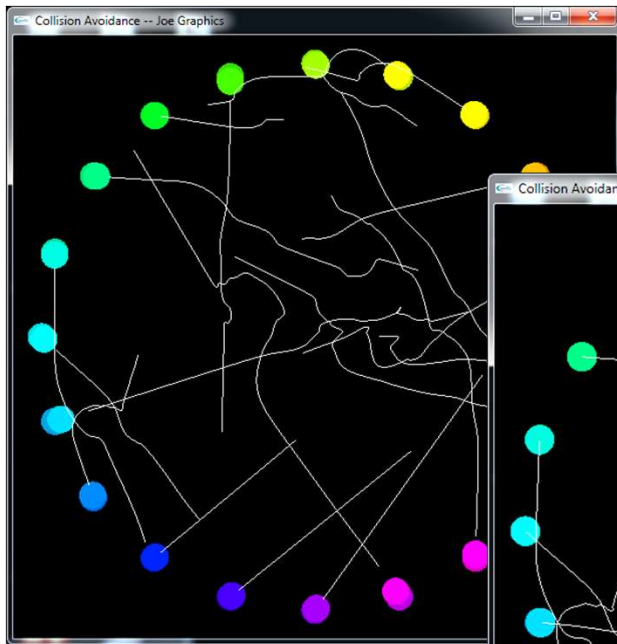
force = mass \* acceleration

or

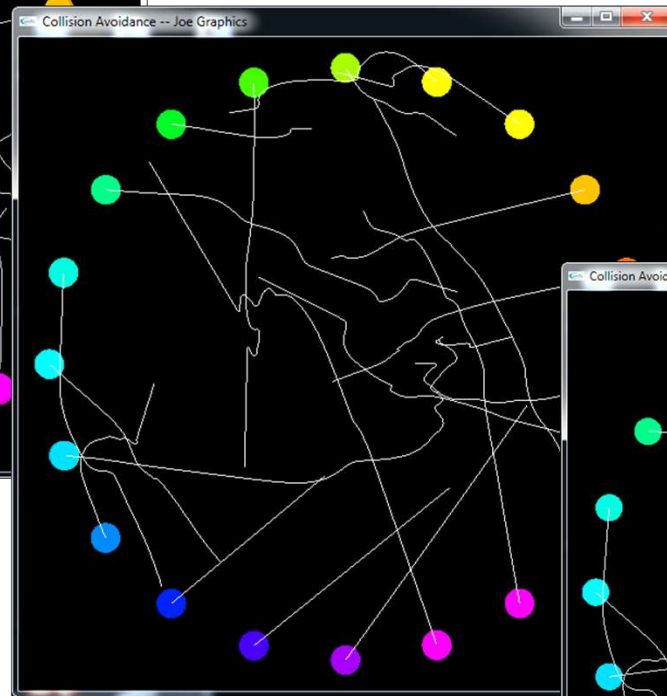
$\ddot{x} = \text{acceleration} = \text{force} / \text{mass}$

$$\ddot{x} = \frac{-c\dot{x} - kx + \sum F_{repulsive}}{m}$$

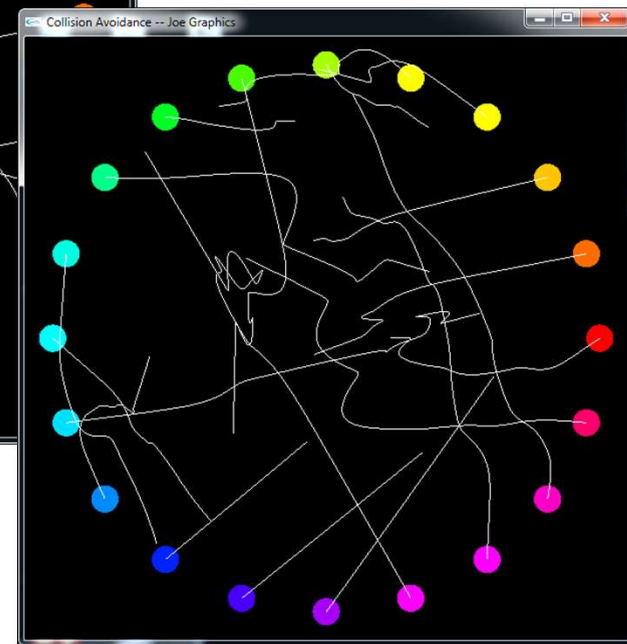
## Increasing the Stiffness



Stiffness = 3



Stiffness = 6

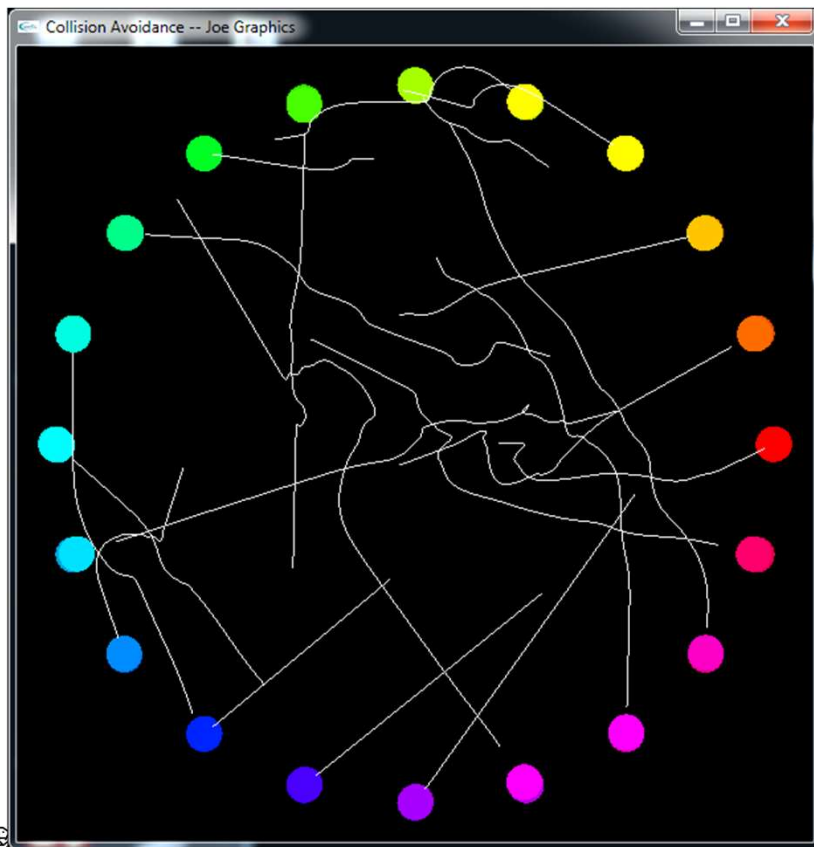


Stiffness = 9

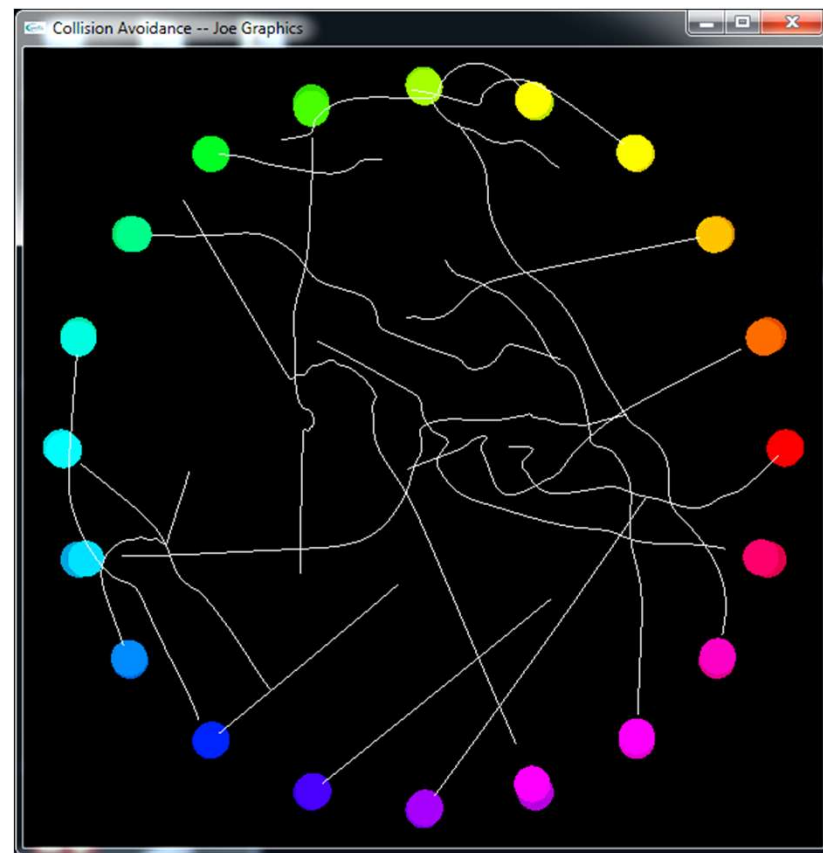


## Increasing the Repulsion Coefficient

37



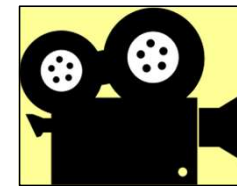
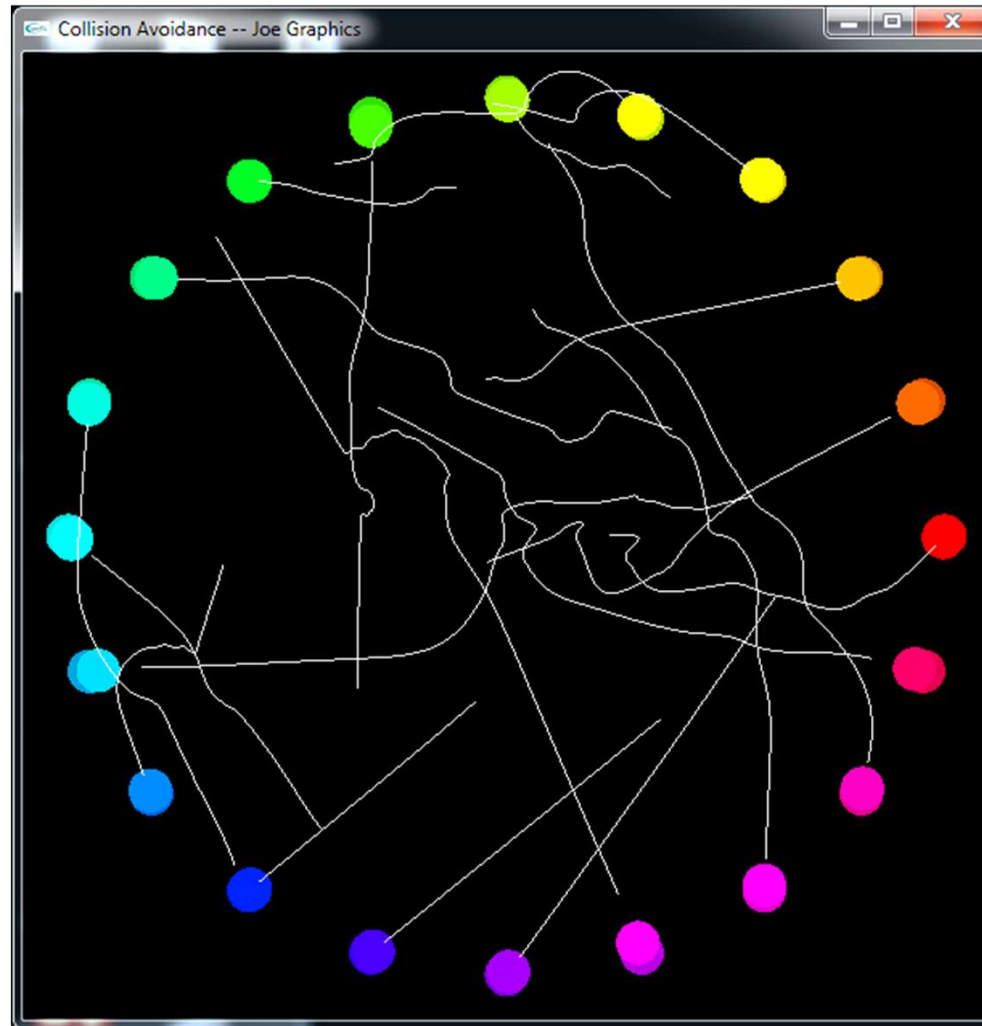
Repulse = 10



Repulse = 30



## Functional Animation: Setup Imaginary Physics to Make the Object *Want* to Move Like We Want it To



avoid.mp4



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## Motion Capture (“MoCap”) as an Input for Animation



Natural Point





## Motion Capture is for Hands and Faces Too



Natural Point





## Even Animals can be MoCapped

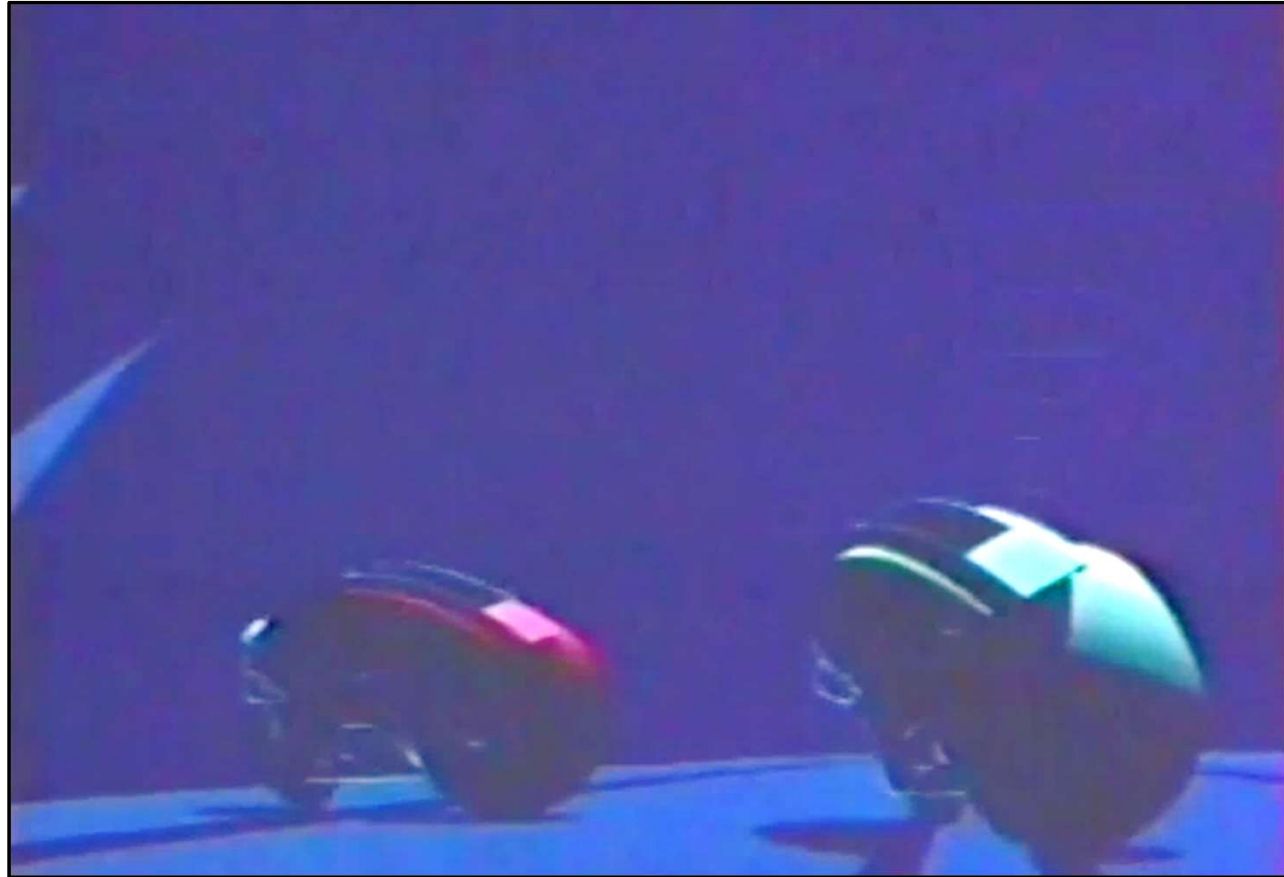


My cats would never have put up with this...

[https://www.youtube.com/watch?v=zyq\\_LQrHpoo](https://www.youtube.com/watch?v=zyq_LQrHpoo)



Tron I –  
They probably should have used physics, but didn't



MAGI

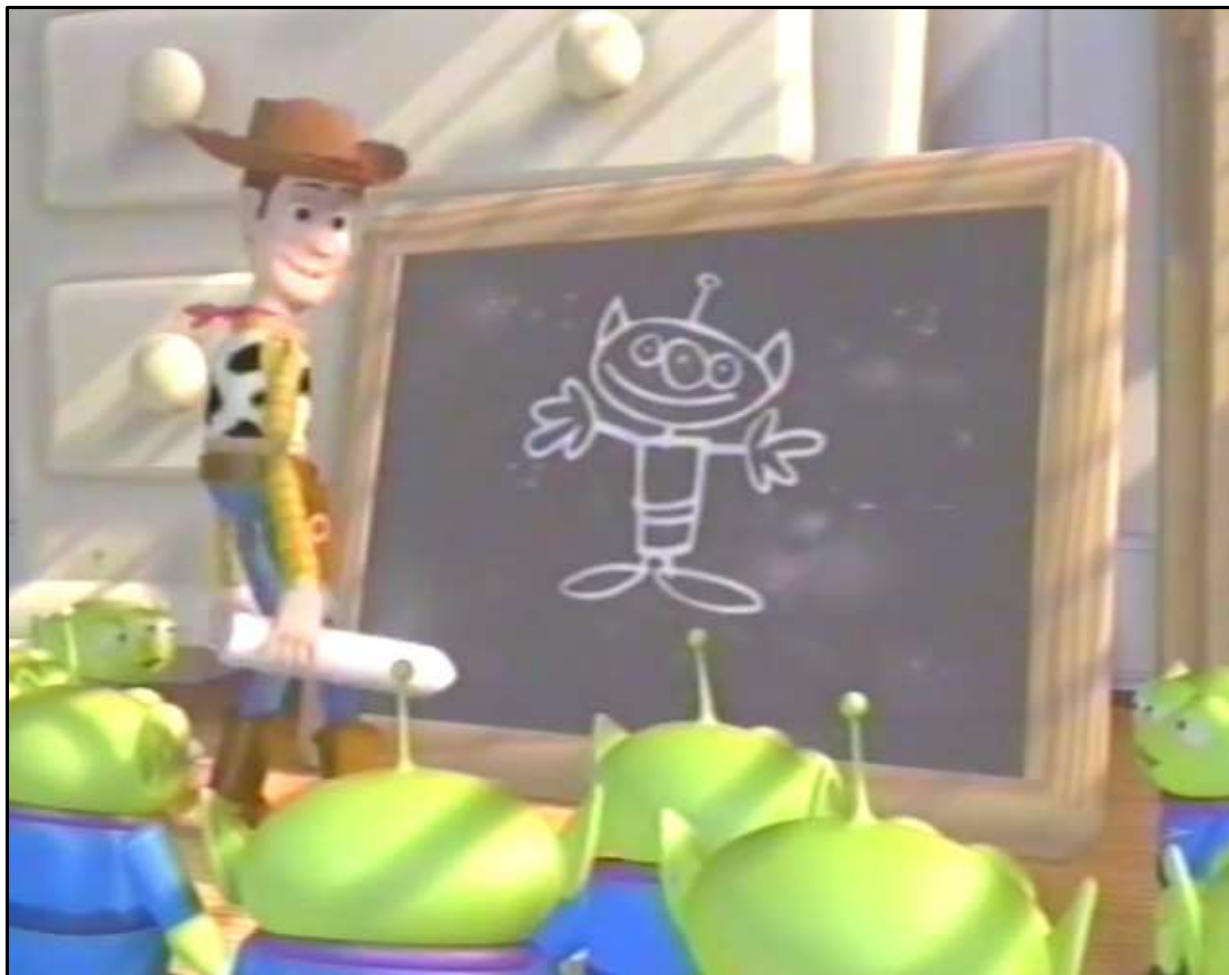


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## Card Trick



## Pixar Animated Shorts



Pixar



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mjb – August 30, 2024