


Geometric Modeling for Computer Graphics



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GeometricModeling.pdf

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What do we mean by "Modeling"?

How we model geometry depends on what we would like to use the geometry for:

- Looking at its appearance
- Will we need to interact with its shape?
- How does it interact with its environment?
- How does it interact with other objects?
- What is its surface area and volume?
- Will it need to be 3D-printed?
- Etc.

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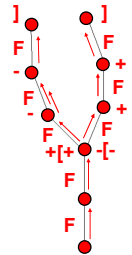
2

L-Systems as a Special Way to Model 3D Geometry

Introduced and developed in 1968 by Aristid Lindenmayer, L-systems are a way to apply grammar rules for generating fractal (self-similar) geometric shapes. For example, take the string:

"FF+[F-F-F]-[F+F+F]"

F move forward one step
+ turn right
- turn left
[push state
] pop state



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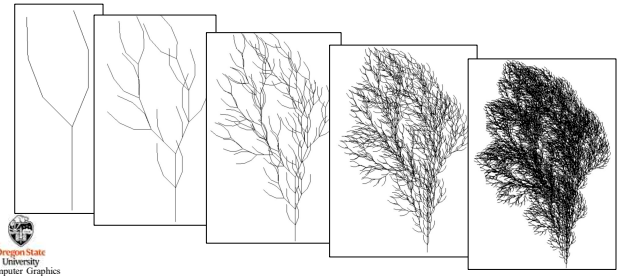
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L-Systems as a Special Way to Model 3D Geometry

But the *real* fun comes when you call that string recursively. For every F, replicate that string but with smaller geometry:

"F → FF+[F-F-F]-[F+F+F]"



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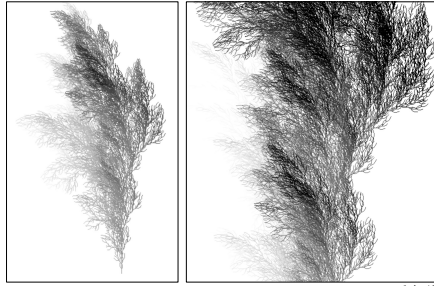
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L-Systems as a Special Way to Model 3D Geometry

And, of course we can introduce more grammar to swing it into 3D

"F → FF+[F-<F>F]-[F+^F+vF]"

+ rotate + about Z
- rotate - about Z
< rotate + about Y
> rotate - about Y
v rotate + about X
^ rotate - about X




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Another way to Model: Curve Sculpting – Bézier Curve Sculpting



$$P(t) = (1-t)^3P_0 + 3t(1-t)^2P_1 + 3t^2(1-t)P_2 + t^3P_3$$

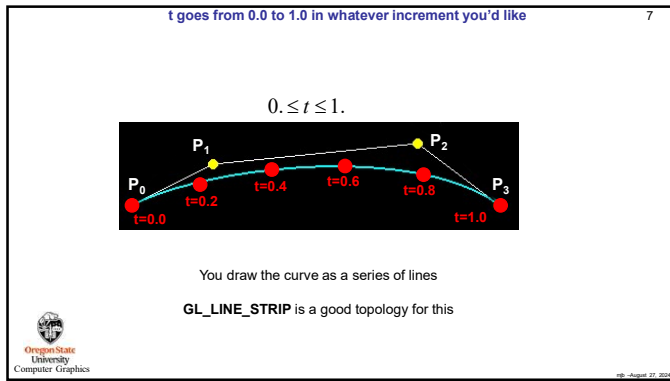
$$0 \leq t \leq 1.$$

where P represents $\begin{Bmatrix} x \\ y \\ z \end{Bmatrix}$

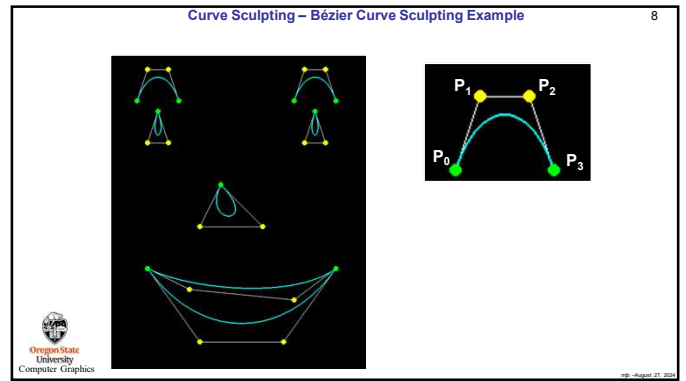
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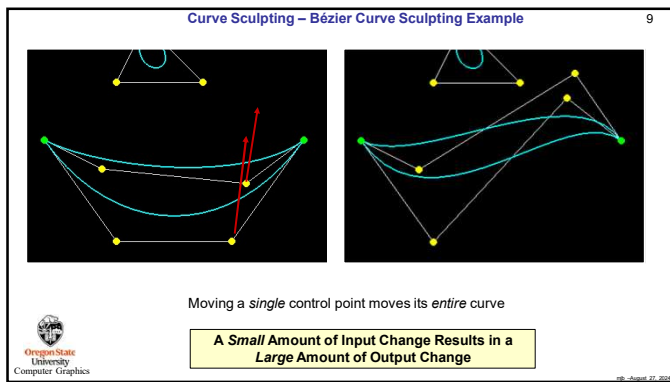
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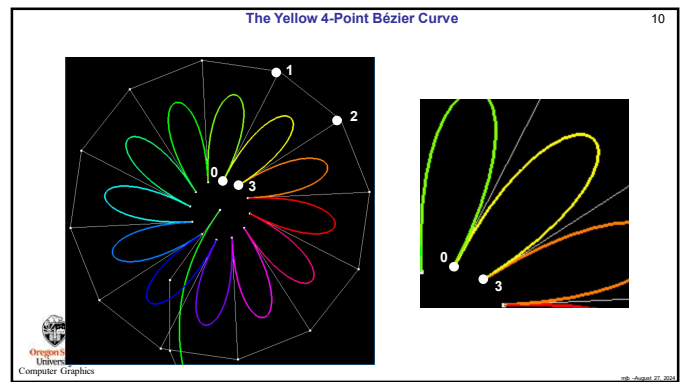
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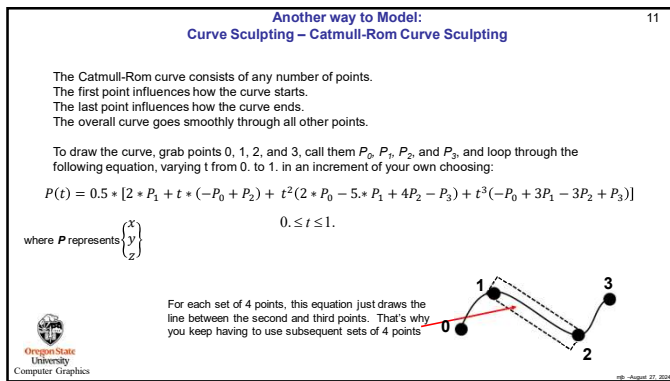
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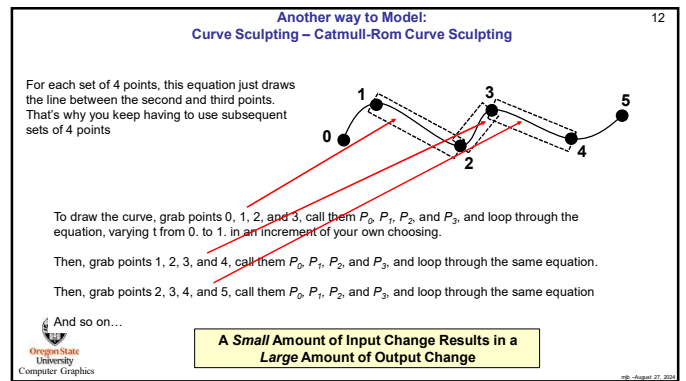
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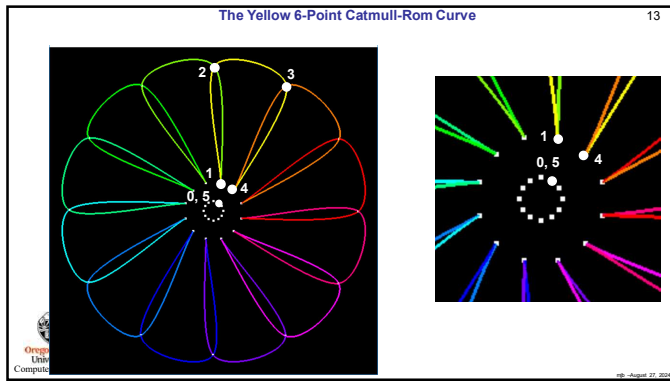
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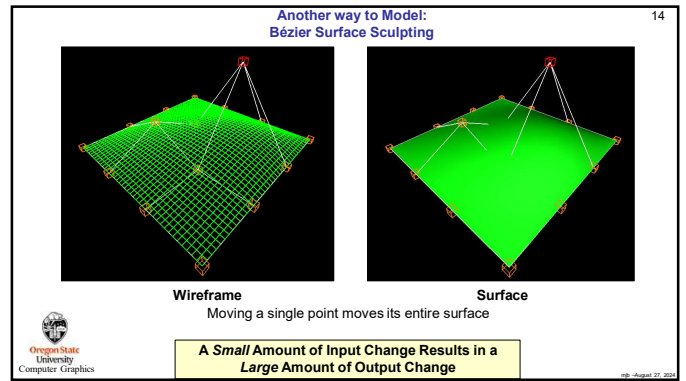
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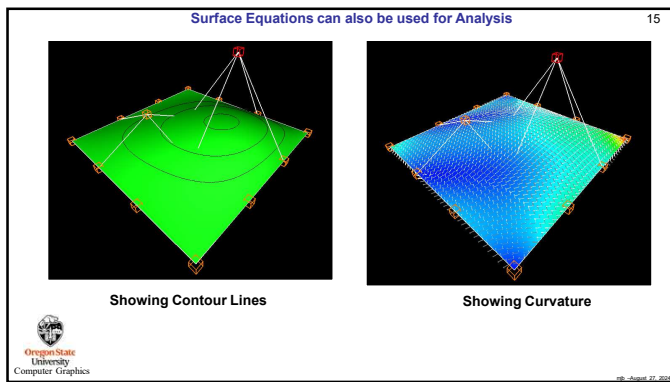
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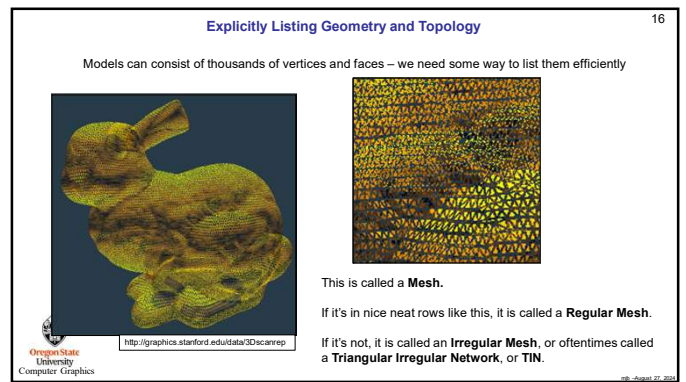
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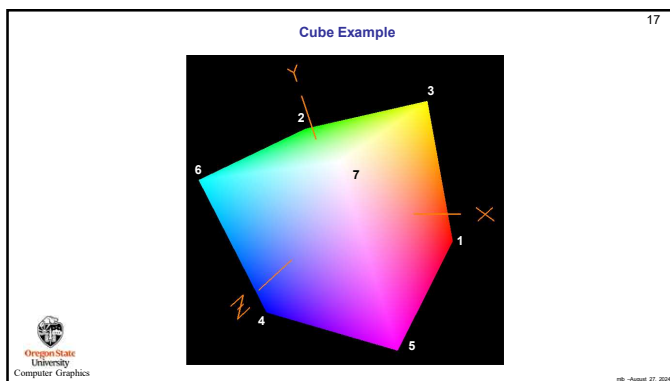
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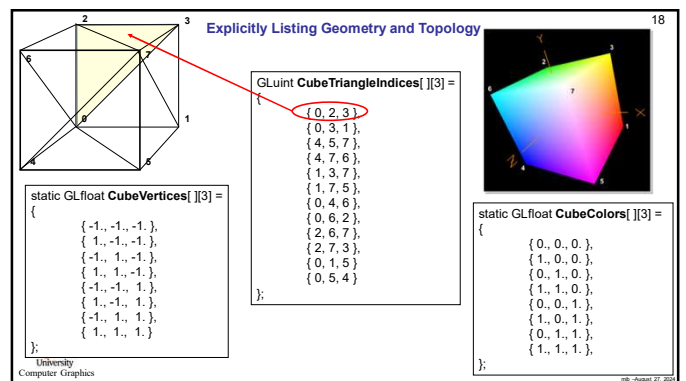
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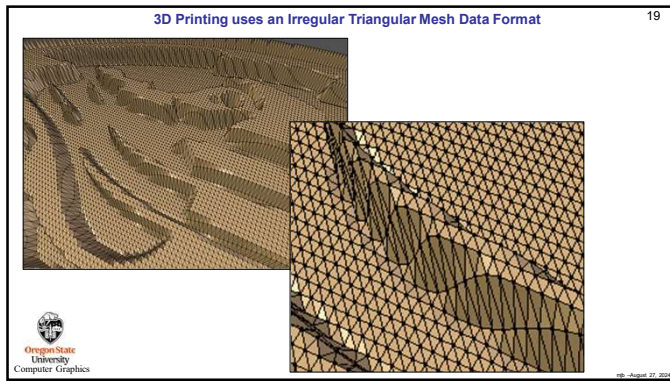
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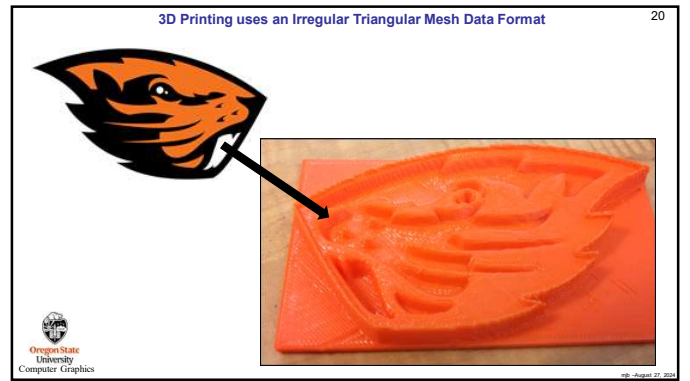
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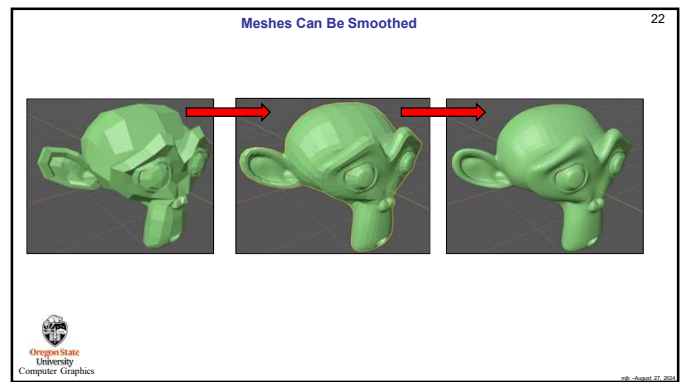
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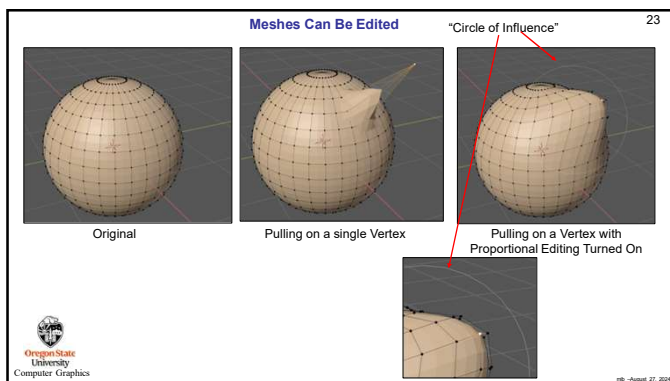
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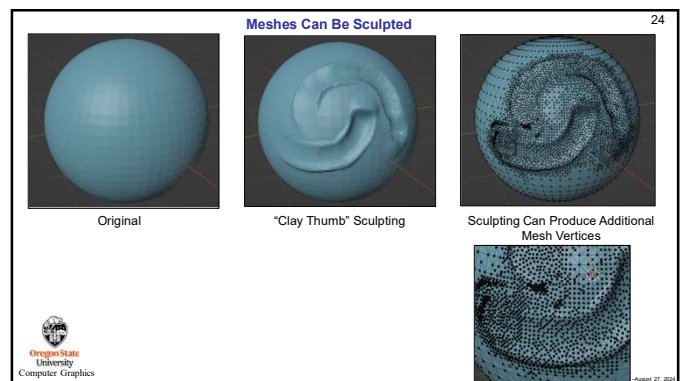
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Remember Venn Diagrams (2D Boolean Operators) from High School?

Two Overlapping Shapes

Union: $A \cup B$

Intersection: $A \cap B$

Difference: $A - B$

I thought I left Venn Diagrams behind in High School !

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Well, Welcome to Venn Diagrams in 3D

Two Overlapping Solids

Union: $A \cup B$

Intersection: $A \cap B$

Difference: $A - B$

This is often called **Constructive Solid Geometry, or CSG**

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Geometric Modeling Using 3D Boolean Operators on Meshes

Two Overlapping Solids

Union: $A \cup B$

Intersection: $A \cap B$

Difference: $A - B$

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Procedural Geometric Modeling Using TinkerCad/Codeblocks

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3D Boolean Operators are Important in 3D Printing as well as General Modeling

Two Overlapping Solids – Cannot Be 3D Printed

Two Overlapping Solids Unioned – Now Can Be 3D Printed

Intersected and Differenced Solids Can be 3D Printed as Well

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Another Way to Edit Meshes: Lattice Sculpting

This is often called a "Lattice" or a "Cage".

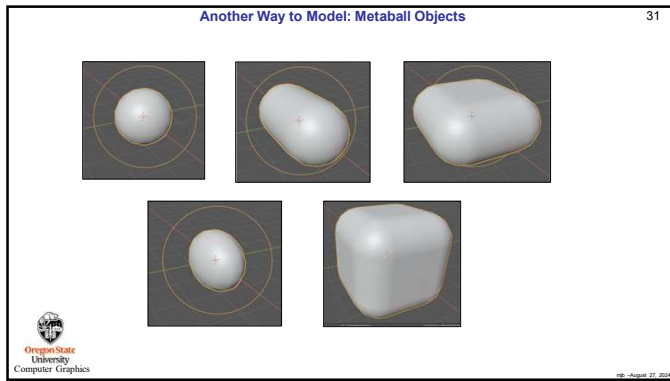
Slip a simpler object (e.g., a subdivided cube) around some of the object's vertices. As you sculpt the simpler object, all those object vertices get sculpted too.

A Small Amount of Input Change Results in a Large Amount of Output Change

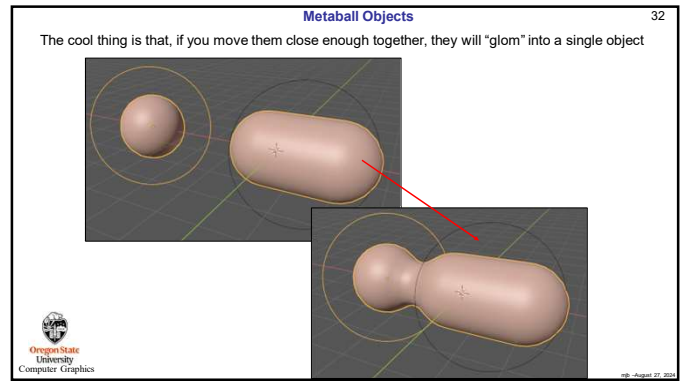
lattice.mp4

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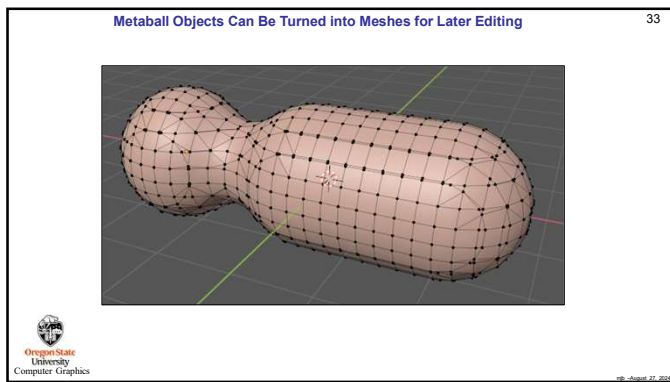
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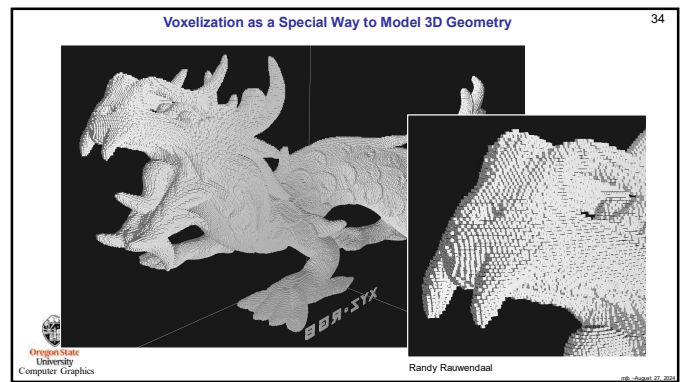
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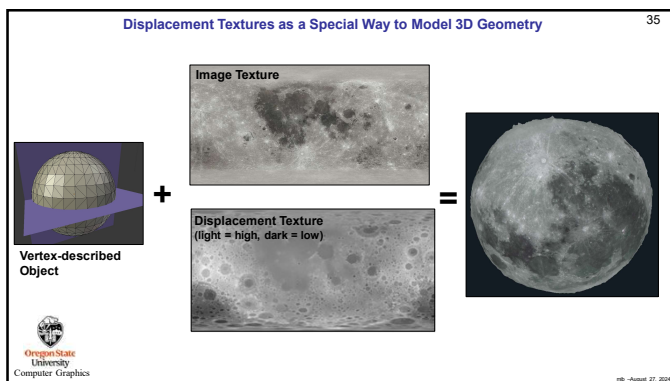
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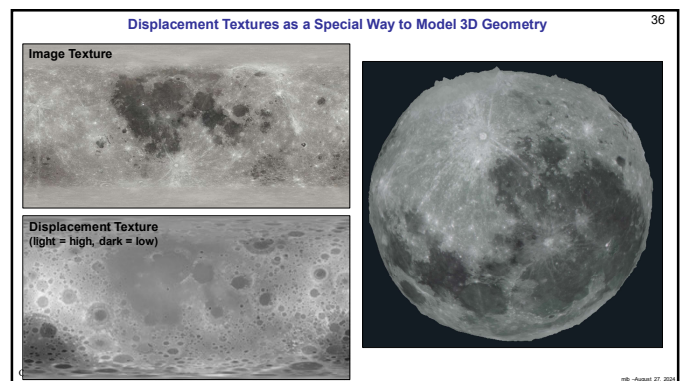
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Displacement Textures as a Special Way to Model 3D Geometry

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moondisp.vert

```
#version 330 compatibility
uniform float uLightX, uLightY, uLightZ;
uniform float uHeightScale;
uniform float uSeaLevel;
uniform sampler2D uDispUnit;
uniform bool uDoElevations;

out vec2 vST;
out vec3 vN;
out vec3 vL;

// normal vector
// vector from point to light

void main()
{
    vec2 st = gl_MultiTexCoord0.st;
    vST = st;

    vec3 norm = normalize( gl_NormalMatrix * gl_Normal );
    vN = norm;

    vec3 LightPos = normalize( vec3( uLightX, uLightY, uLightZ ) );
    vec3 EyePos = gl_ModelViewMatrix * gl_Vertex;
    vL = LightPos - EyePos;
    // eye coordinate position
    // vector from the point to the light position

    vec3 vert = gl_Vertex.xyz;
    if( uDoElevations )
    {
        float disp = texture( uDispUnit, st ).r;
        disp -= uSeaLevel;
        vert += uHeightScale * disp;
        vert += normalize( gl_Normal ) * disp;
    }

    gl_Position = gl_ModelViewProjectionMatrix * vec4( vert, 1. );
}
```

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Displacement Textures as a Special Way to Model 3D Geometry

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moondisp.frag, I

```
#version 330 compatibility
uniform bool uDoBumpMapping;
uniform float uKa, uKd;
uniform float uHeightScale;
uniform float uNormalScale;
uniform sampler2D uColorUnit;
uniform sampler2D uDispUnit;

in vec2 vST;
in vec3 vN;
in vec3 vL;
#define DELTA 0.01

void main()
{
    vec3 newColor = texture( uColorUnit, vST ).rgb;
    gl_FragColor = vec4( newColor, 1. );
    if( uDoBumpMapping )
    {
        ... // see next slide
    }
}
```

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Displacement Textures as a Special Way to Model 3D Geometry

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moondisp.frag, II

```
if( uDoBumpMapping )
{
    vec2 stp0 = vec2( DELTA, 0. );
    vec2 stp1 = vec2( 0. , DELTA );
    float west = texture2D( uDispUnit, vST-stp0 ).r;
    float east = texture2D( uDispUnit, vST+stp0 ).r;
    float south = texture2D( uDispUnit, vST-stp1 ).r;
    float north = texture2D( uDispUnit, vST+stp1 ).r;
    vec3 stangent = vec3( 2.*DELTA, 0., uNormalScale * ( east - west ) );
    vec3 tangent = vec3( 0., 2.*DELTA, uNormalScale * ( north - south ) );
    vec3 Normal = normalize( cross( stangent, tangent ) );
    vec3 Light = normalize( vL );

    vec3 ambient = uKa * newColor;
    float d = 0.;
    if( dot( Normal, Light ) > 0. ) // only do diffuse if the light can see the point
    {
        d = dot( Normal, Light );
    }
    vec3 diffuse = uKd * d * newColor;
    gl_FragColor = vec4( ambient+diffuse, 1. );
}
```

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Displacement Textures as a Special Way to Model 3D Geometry

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Just the image texture

Lighting only, no displacements

Displacements only, no lighting

Displacements + Lighting

Note: as you can imagine, static images do not do this justice. Being able to dynamically rotate the Moon and change the height exaggeration and light position makes a big difference!

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Modeling as an Initial Step in Simulation (Explosion)

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Object Modeling Rules for 3D Printing

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The object must be a legal solid. It must have a definite inside and a definite outside. It can't have any missing face pieces.

Missing face

"Definite inside and outside" is sometimes called "Two-manifold" or "Watertight"

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The Simplified Euler's Formula* for Legal Solids
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*sometimes called the Euler-Poincaré formula

$$F - E + V = 2$$

F Faces
E Edges
V Vertices

For a cube, $6 - 12 + 8 = 2$

We will talk more about this in the 3D Printing notes!

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Object Modeling Rules for 3D Printing
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Objects cannot pass through other objects. If you want two shapes together, do a Boolean union on them so that they become one complete object.

Overlapped in 3D -- bad

Boolean union -- good

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