

Generalized Bump-mapping with Surface Local Coordinates

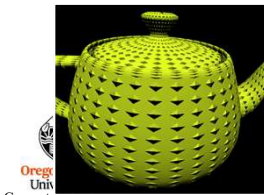


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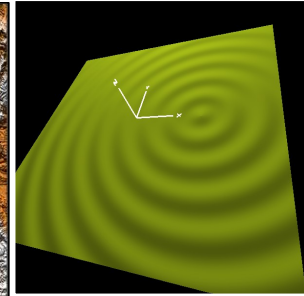
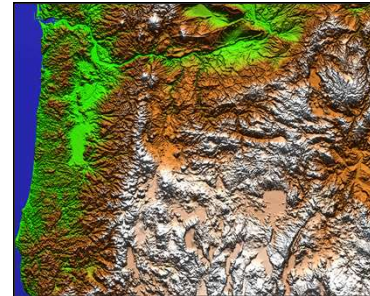


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SurfaceLocalCoordinates.pptb

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The Most Straightforward Types of Bump-Mapping are Height Fields

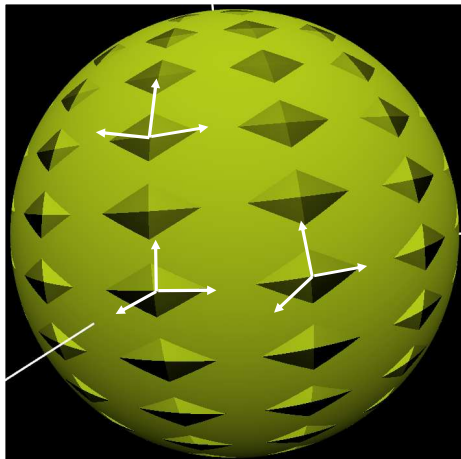


Height Field bump-mapping is straightforward because the underlying coordinate system is constant. Each fragment's Z points up, each fragment's X points right, etc. Thus, the tangent vectors always involve $\frac{dz}{dx}$ and $\frac{dz}{dy}$.

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What if that is not the case? Here, the coordinate system is constantly changing, depending on where you are on the sphere



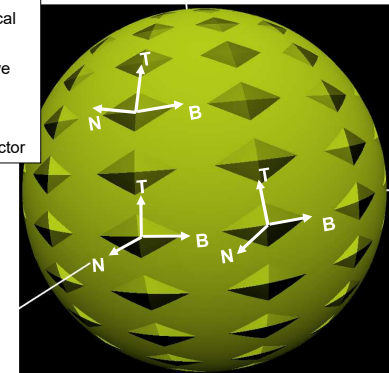
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This is referred to as *Surface Local Coordinates*

To call these moving axes X-Y-Z would be confusing. Rather than X-Y-Z, Surface Local Coordinates are **B-T-N**:

- N is the surface Normal vector, which we usually know already
- T is a Tangent vector
- B is the Bitangent, the other tangent vector



We will assume that we know the Normal everywhere because of how the shape was modeled. Now, how do we find T and B? And, how do we convert these to X-Y-Z?

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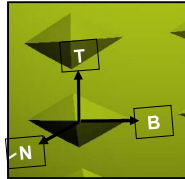
Generalized Bump Mapping: A Problem

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The problem is that we need to do lighting, but the lighting needs to be done in X-Y-Z, *but* the bump information is in B-T-N!

We need to:

1. Figure out how to determine T and B, and,
2. Figure out how to convert B-T-N coordinates to X-Y-Z for lighting



We will refer to the coordinates in the B-T-N system as **(b,t,n)**.



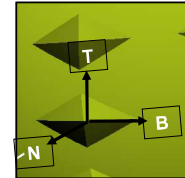
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Bump Mapping:
Establishing the Surface Local Coordinate System

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We need a second piece of information: Pick a general rule, e.g., "Tangent = up (0.,1.,0.)" We then have two choices:

- a. Use two cross-products to correctly orthogonalize it wrt the Normal
- b. Use the Gram-Schmidt rule to correctly orthogonalize it wrt the Normal



// the vectors B-T-N form an X-Y-Z looking
// right handed coordinate system:

```
vec3 N = normalize( gl_NormalMatrix * gl_Normal );
vec3 Tg, T;      // Tguess and corrected T
vec3 B;
```

```
#define CROSS_PRODUCT_METHOD
```

```
#ifdef CROSS_PRODUCT_METHOD
Tg = vec3( 0.,1.,0.); // guess at T
B = normalize( cross(Tg,N) ); // correct B
T = normalize( cross(N,B) ); // corrected T
#endif
```

```
#ifdef GRAM_SCHMIDT_METHOD
Tg = vec3( 0.,1.,0.); // guess at T
float d = dot( Tg, N );
T = normalize( Tg - d*N ); // corrected T
B = normalize( cross(T,N) ); // correct B
#endif
```



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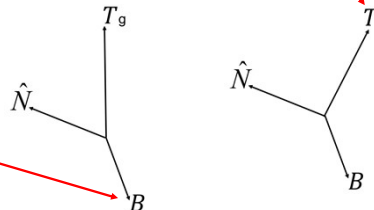
Cross Product Orthogonalization

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```
vec3 Tg = vec3( 0.,1.,0.); // initial guess
vec3 B = normalize(cross(Tg,N) );
vec3 T = normalize(cross(N,B) );
```

- 1 Given that **N** is correct, how do we change **Tg** to be exactly perpendicular to **N** ?

- 2 Take the cross product of **Tg** and **N** to get a **B**-vector that is perpendicular to both



- 3 Take the cross product of **N** and **B** to get a **T** vector that is perpendicular to both



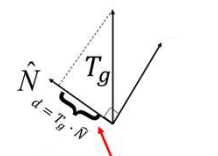
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Gram-Schmidt Orthogonalization

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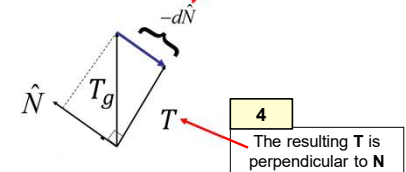
```
vec3 Tg = vec3( 0.,1.,0.); // initial guess
float d = dot( Tg, N );
vec3 T = normalize( Tg - d*N );
vec3 B = normalize(cross(T,N) );
```

- 1 Given that **N** is correct, how do we change **Tg** to be exactly perpendicular to **N** ?



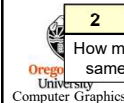
- 2 How much of **Tg** is in the same direction as **N** ?

- 3 How much of **Tg** do we need to get rid of so that *none* of it is in the same direction as **N** ?



- 4 The resulting **T** is perpendicular to **N**

$$T = Tg - d\hat{N} = Tg - (Tg \cdot \hat{N})\hat{N}$$



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Bump Mapping: Converting Between Coordinate Systems

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Converting from X-Y-Z to b-t-n:

$$\begin{Bmatrix} b \\ t \\ n \end{Bmatrix} = \begin{bmatrix} B_x & B_y & B_z \\ T_x & T_y & T_z \\ N_x & N_y & N_z \end{bmatrix} \begin{Bmatrix} x \\ y \\ z \end{Bmatrix}$$

Converting from b-t-n to X-Y-Z:

$$\begin{Bmatrix} x \\ y \\ z \end{Bmatrix} = \begin{bmatrix} B_x & T_x & N_x \\ B_y & T_y & N_y \\ B_z & T_z & N_z \end{bmatrix} \begin{Bmatrix} b \\ t \\ n \end{Bmatrix}$$



I prefer to use the second one so we can do lighting in X-Y-Z like we are used to doing.

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Generalized Bump Mapping:
Establishing the Surface Local Coordinate System

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Vertex shader:

```
#version 330 compatibility
uniform vec3 uLightPosition;

out vec2 vST;           // texture coords
out vec3 vN;           // normal vector
out vec3 vL;           // vector from point to light
out vec3 vE;           // vector from point to eye
out vec3 vBTNx, vBTNy, vBTnz;

void main()
{
    vN = normalize( gl_NormalMatrix * gl_Normal ); // normal vector
    vec3 Tg = vec3( 0., 1., 0. ); // guess
    vec3 B = normalize( cross(Tg, vN) );
    vec3 T = normalize( cross(vN, B) );

    // produce the transformation from Surface coords to Eye coords
    vBTNx = vec3( B.x, T.x, vN.x );
    vBTNy = vec3( B.y, T.y, vN.y );
    vBTnz = vec3( B.z, T.z, vN.z );
    vST = gl_MultiTexCoord0.st;

    vec4 ECposition = gl_ModelViewMatrix * gl_Vertex; // eye coordinate position
    vL = uLightPosition - ECposition.xyz; // vector from the point to the light position
    vE = vec3( 0., 0., 0. ) - ECposition.xyz; // vector from the point to the eye position
    gl_Position = gl_ModelViewProjectionMatrix * gl_Vertex;
}
```



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Generalized Bump Mapping:
Using the s-t-h to X-Y-Z Transform

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Fragment shader:

```
#version 330 compatibility
uniform vec3 uColor;
uniform vec3 uSpecularColor;
uniform float uKa, uKd, uKs;
uniform float uShininess;
uniform float uBumpDensity;

// coefficients of each type of lighting
// specular exponent
// density of bumps
```

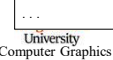
```
in vec2 vST;           // texture coords
in vec3 vN;           // normal vector
in vec3 vL;           // vector from point to light
in vec3 vE;           // vector from point to eye
in vec3 vBTNx, vBTNy, vBTnz;
```

```
vec3
ToXyz( vec3 btn )
```

```
{
    btn = normalize( btn );

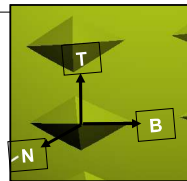
    vec3 xyz;
    xyz.x = dot( vBTNx, btn );
    xyz.y = dot( vBTNy, btn );
    xyz.z = dot( vBTnz, btn );

    return normalize( xyz );
}
```



Look at this closely. It is actually a matrix-multiply!

$$\begin{Bmatrix} x \\ y \\ z \end{Bmatrix} = \begin{bmatrix} B_x & T_x & N_x \\ B_y & T_y & N_y \\ B_z & T_z & N_z \end{bmatrix} \begin{Bmatrix} b \\ t \\ n \end{Bmatrix}$$



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Matrix Multiplication is Really Row-by-Row Dot Products

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The basic operation of matrix multiplication is to pair-wise multiply a single row by a single column

$$\begin{bmatrix} 1 & 2 & 3 \end{bmatrix} \begin{Bmatrix} 4 \\ 5 \\ 6 \end{Bmatrix} \rightarrow 4*1 + 5*2 + 6*3 \rightarrow 32$$

A B C

1x3 3x1 1x1



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Generalized Bump Mapping: Using the Surface Local Transform, I

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```

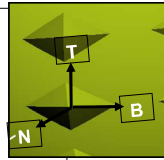
...
void
main( )
{
    vec3 Normal = normalize(vN);
    vec3 Light  = normalize(vL);
    vec3 Eye   = normalize(vE);
    vec3 myColor = uColor;           // default color

    // locate the bumps based on (s,t):
    float Swidth = (1.-0.) / uBumpDensity; // s distance between bumps
    float Theight = (1.-0.) / uBumpDensity; // t distance between bumps
    float numInS = int( vST.s / Swidth );   // which "checker" square we are in
    float numInT = int( vST.t / Theight );   // which "checker" square we are in

    vec2 center;
    center.s = numInS * Swidth + Swidth/2.; // center of that bump checker
    center.t = numInT * Theight + Theight/2.; // center of that bump checker
    vec2 st = vST - center;                  // st is now wrt the center of the bump

    float theta = atan( st.t, st.s );
    ...

```



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Generalized Bump Mapping: Using the Surface Local Transform, II

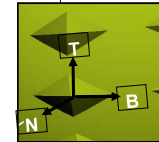
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```

...
vec3 normal = ToXyz( Normal ); // un-bumped normal

if( abs(stp.s) > Swidth/4. || abs(stp.t) > Theight/4. )
{
    normal = ToXyz( vec3( 0., 0., 1. ) );
}
else
{
    if( PI/4. <= theta && theta <= 3.*PI/4. )
    {
        normal = ToXyz( vec3( 0., Height, Theight/4. ) );
    }
    else if( -PI/4. <= theta && theta <= PI/4. )
    {
        normal = ToXyz( vec3( Height, 0., Swidth/4. ) );
    }
    else if( -3.*PI/4. <= theta && theta <= -PI/4. )
    {
        normal = ToXyz( vec3( 0., -Height, Theight/4. ) );
    }
    else if( theta >= 3.*PI/4. || theta <= -3.*PI/4. )
    {
        normal = ToXyz( vec3( -Height, 0., Swidth/4. ) );
    }
}
...

```



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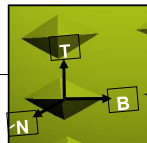
Generalized Bump Mapping: Using the Surface Local Transform, III

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```

...
vec3 ambient = uKa * myColor;
float d = 0.;
float s = 0.
if( dot(normal,Light) > 0. // only do specular if the light can see the point
{
    d = dot(normal,Light);
    vec3 R = normalize( reflect( -Light, normal ) ); // reflection vector
    s = pow( max( dot(Eye,R), 0. ), uShininess );
}
vec3 diffuse = uKd * d * myColor;
vec3 specular = uKs * s * uSpecularColor;
gl_FragColor = vec4( ambient + diffuse + specular, 1. );
}

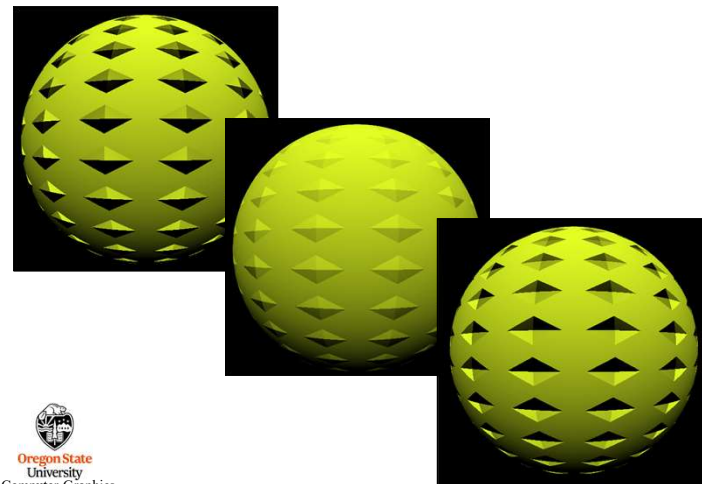
```



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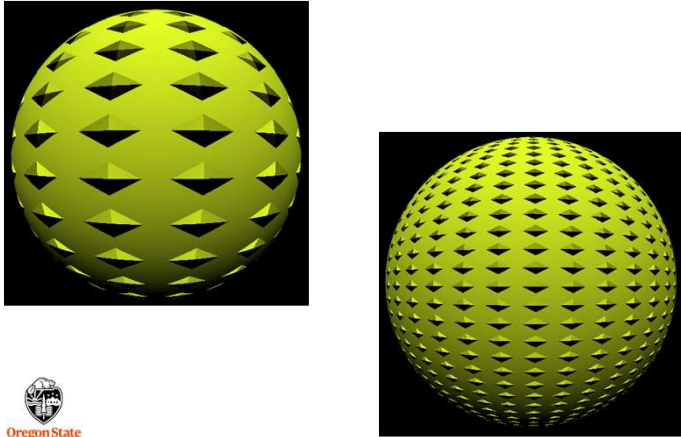
Changing the Bump Height

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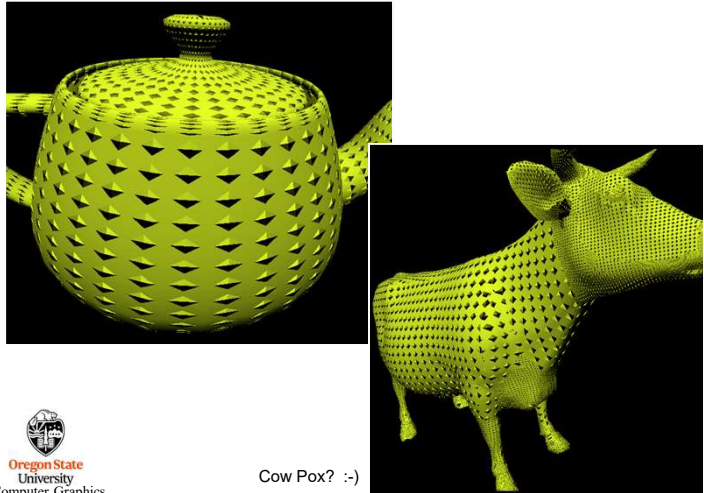
Changing the Bump Density 17



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Different Objects 18



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Cow Pox? :-)

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Combining Bump and Cube Mapping:
A Good Reason to Work in X-Y-Z instead of B-T-N 19



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Combining Bump and Cube Mapping:
A Good Reason to Work in X-Y-Z instead of B-T-N 20



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