



Vulkan Ray Tracing – 5 New Shader Types!



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Mike Bailey

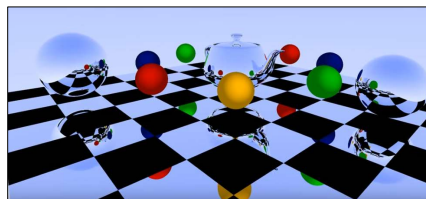
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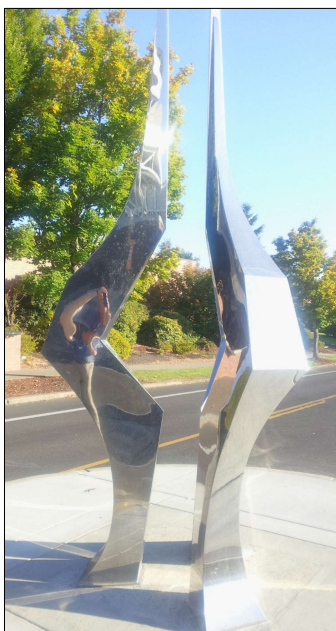
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VulkanRayTracing467557.pptx

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Analog Ray Tracing Example ☺

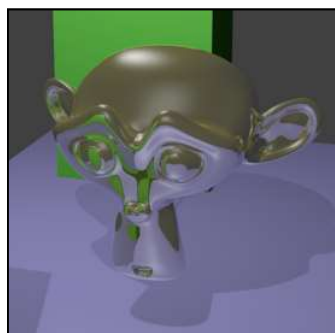


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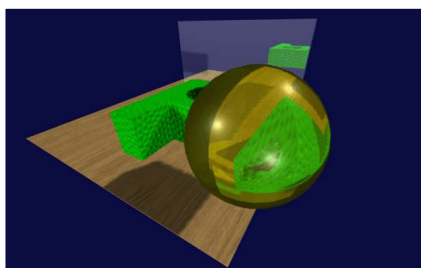
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Digital Ray Tracing Examples

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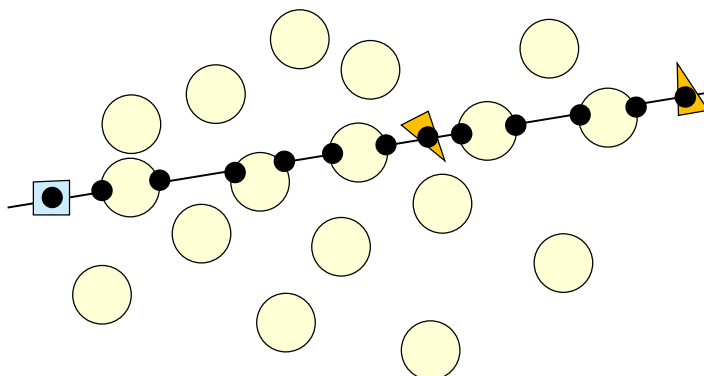
Blender



IronCad

In a Raytracing, each ray typically hits a lot of Things

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Parametrizing a Ray

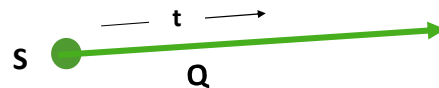
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Given:

S is the (x,y,z) starting point

Q is the (x,y,z) direction of travel

Then, the (x,y,z) position of a point **p** at some position along its direction of travel is:



$$p = S + tQ$$

$$t \geq 0.$$



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Example: The Ray Intersection Process for a Sphere

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Sphere equation: $(x-x_c)^2 + (y-y_c)^2 + (z-z_c)^2 = R^2$

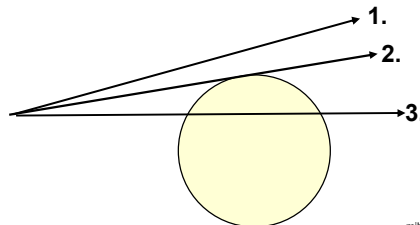
Ray equation: $(x,y,z) = (x_0,y_0,z_0) + t(dx,dy,dz)$

Plugging (x,y,z) from the second equation into the first equation and multiplying-through and simplifying gives:

$$At^2 + Bt + C = 0 \quad \rightarrow \quad t_1, t_2 = \frac{-B \pm \sqrt{B^2 - 4AC}}{2A}$$

Solve for t_1, t_2 and analyze the solution like this:

1. If both t_1 and t_2 are complex (i.e., have an imaginary component), then the ray missed the sphere completely.
2. If both t_1 and t_2 are real and identical, then the ray brushed the sphere at a tangent point.
3. If both t_1 and t_2 are real and different, then the ray entered and exited the sphere.

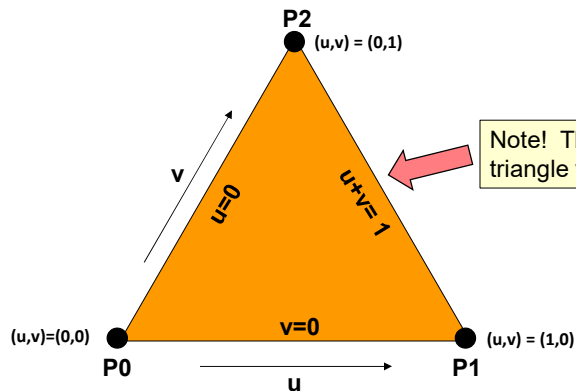


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Parameterizing a Triangle

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It's often useful to be able to parameterize a triangle into (u,v) , like this:



Note! There is *no* place in this triangle where $u = 1$ and $v = 1$.



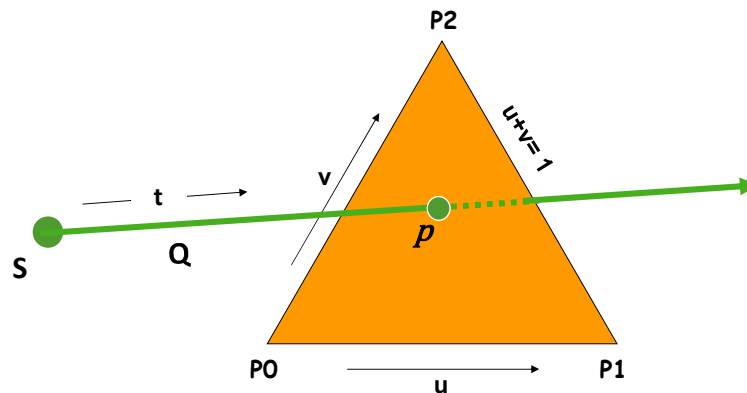
$$p = P0 + u*(P1-P0) + v*(P2-P0)$$

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The Setup

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We want to find out where the ray intersects the triangle.
That is, where is the point p that is common to both the ray and the triangle?



Such that:

$$\begin{aligned} t &\geq 0. \\ 0 &\leq u \leq 1. \\ 0 &\leq v \leq 1-u \end{aligned}$$



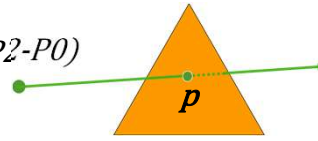
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Equation Setup

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Triangle: $p = P0 + u*(P1-P0) + v*(P2-P0)$

Ray: $p = S + tQ$



Re-arranging:

$$P0 + u*(P1-P0) + v*(P2-P0) = S + tQ$$

Re-arranging some more:

$$-tQ + u*(P1-P0) + v*(P2-P0) = S - P0$$

Then collecting terms, we get:

$$At + Bu + Cv = D$$

where:

$$A = -Q$$

$$B = P1-P0$$

$$C = P2-P0$$

$$D = S - P0$$



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Three Equations, Three Unknowns

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Remembering that this equation is really 3 equations in (x,y,z):

$$At + Bu + Cv = D$$

we have 3 equations with 3 unknowns, which can be cast into a matrix form

$$\begin{bmatrix} A_x & B_x & C_x \\ A_y & B_y & C_y \\ A_z & B_z & C_z \end{bmatrix} \begin{Bmatrix} t \\ u \\ v \end{Bmatrix} = \begin{Bmatrix} D_x \\ D_y \\ D_z \end{Bmatrix}$$

Our goal is to solve this for t^* , u^* , and v^*



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Solve for (t^*, u^*, v^*) using Cramer's Rule

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$$\begin{bmatrix} A_x & B_x & C_x \\ A_y & B_y & C_y \\ A_z & B_z & C_z \end{bmatrix} \begin{Bmatrix} t \\ u \\ v \end{Bmatrix} = \begin{Bmatrix} D_x \\ D_y \\ D_z \end{Bmatrix}$$

$$D_0 = \det \begin{bmatrix} A_x & B_x & C_x \\ A_y & B_y & C_y \\ A_z & B_z & C_z \end{bmatrix}$$

$$D_t = \det \begin{bmatrix} D_x & B_x & C_x \\ D_y & B_y & C_y \\ D_z & B_z & C_z \end{bmatrix}$$

$$t^* = \frac{D_t}{D_0}$$

$$D_u = \det \begin{bmatrix} A_x & D_x & C_x \\ A_y & D_y & C_y \\ A_z & D_z & C_z \end{bmatrix}$$





$$u^* = \frac{D_u}{D_0}$$

$$D_v = \det \begin{bmatrix} A_x & B_x & D_x \\ A_y & B_y & D_y \\ A_z & B_z & D_z \end{bmatrix}$$

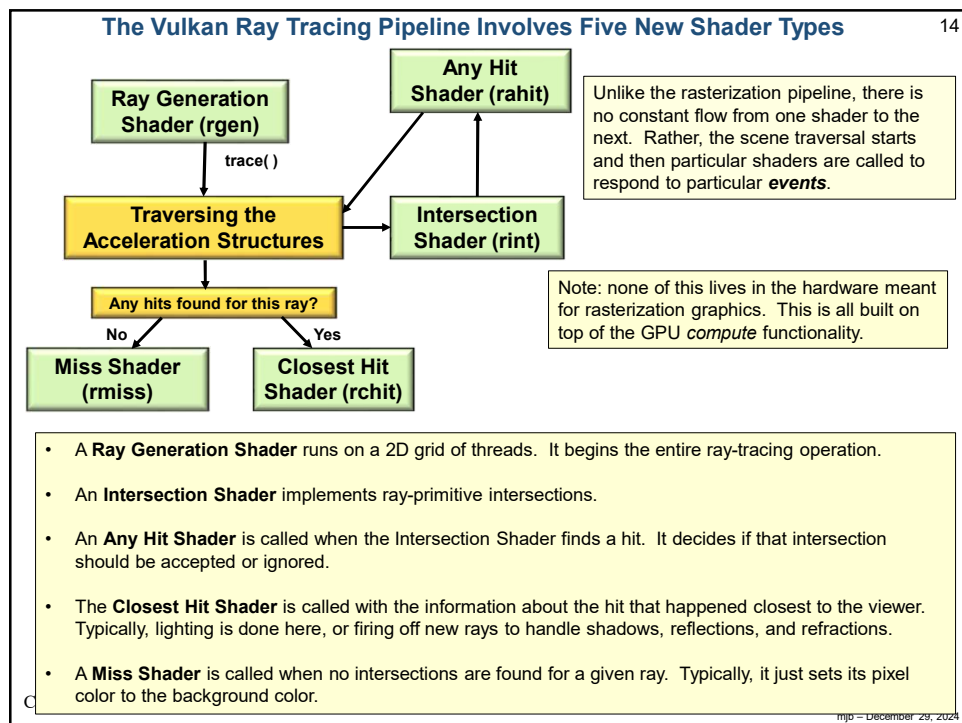
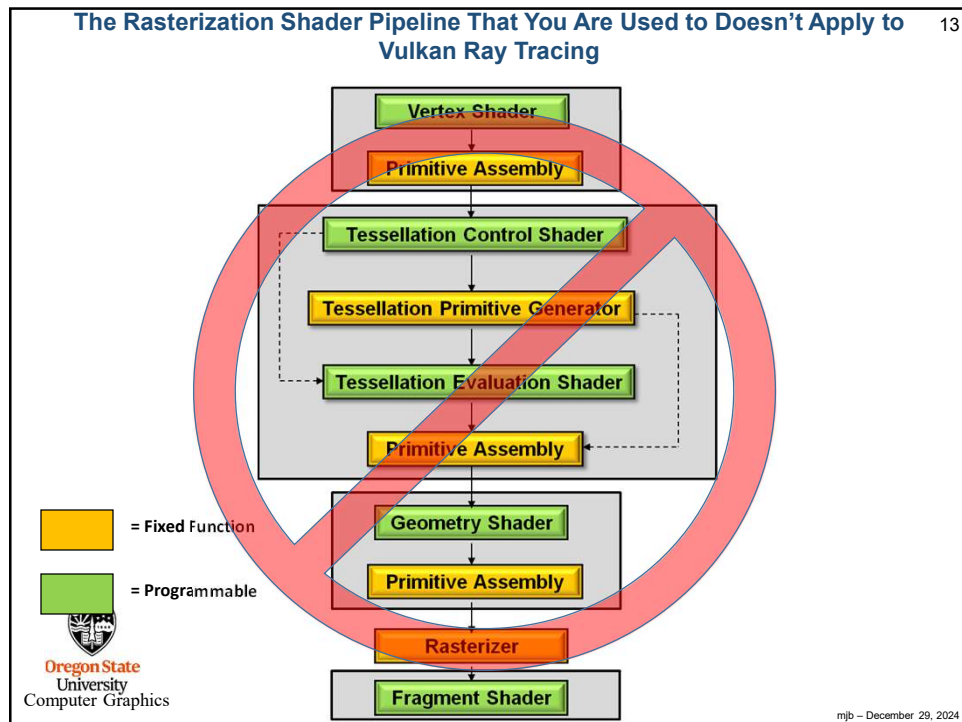
$$v^* = \frac{D_v}{D_0}$$

The Steps

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1. Compute D_0
2. If $D_0 \approx 0.$, then the ray is *parallel* to the plane of the triangle 
3. Compute D_t
4. Compute t^*
5. If $t^* < 0.$, the ray goes away from the triangle 
6. Compute D_u
7. Compute u^*
8. If $u^* < 0.$ or $u^* > 1.$, then the ray hits outside the triangle 
9. Compute D_v
10. Compute v^*
11. If $v^* < 0.$ or $v^* > 1 - u^*$, then the ray hits outside the triangle 
12. The intersection is at the point $p = S + Qt^*$

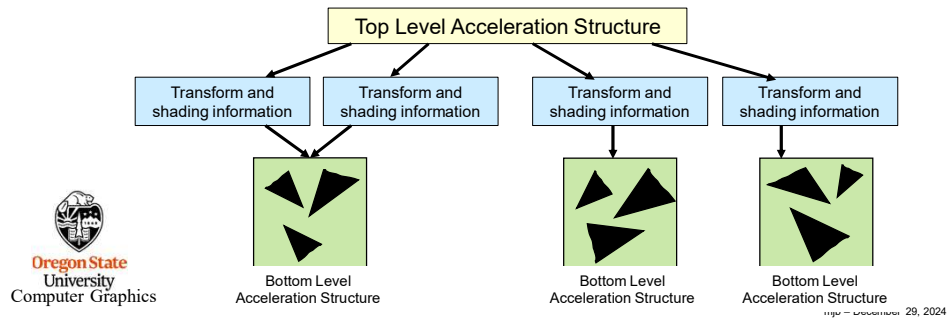
This is known as the **Möller-Trumbore Triangle Intersection Algorithm**



Acceleration Structures

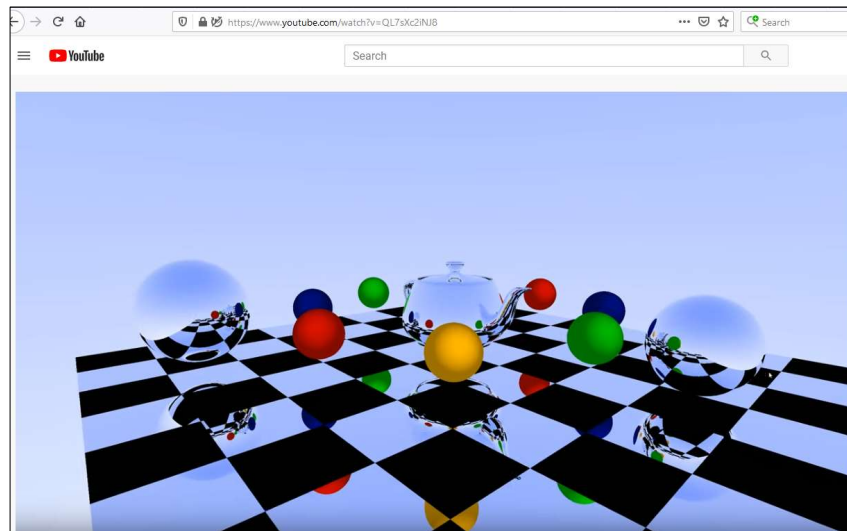
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- A Bottom-level Acceleration Structure (BLAS) reads the vertex data from vertex and index VkBuffers to determine bounding boxes.
- You can also supply your own bounding box information to a BLAS.
- A Top-level Acceleration Structure (TLAS) holds transformations and pointers to multiple BLASes.
- The BLAS is essentially used as a Model Coordinate bounding box, while the TLAS is used as a World Coordinate bounding box.



Check This Out!

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<https://www.youtube.com/watch?v=QL7sXc2iNJ8>



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