




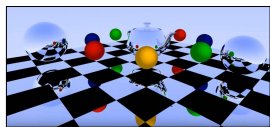
Vulkan.

Vulkan Ray Tracing – 5 New Shader Types!


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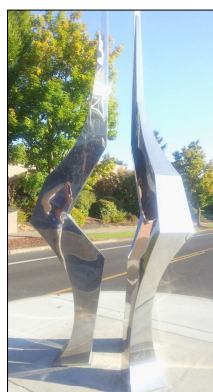

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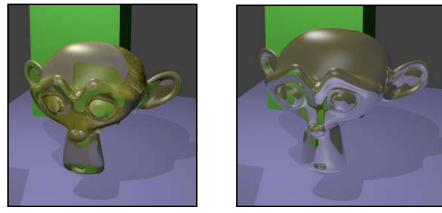
Analog Ray Tracing Example



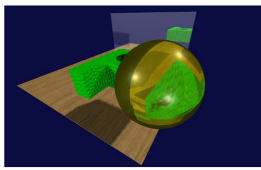

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Digital Ray Tracing Examples



Blender

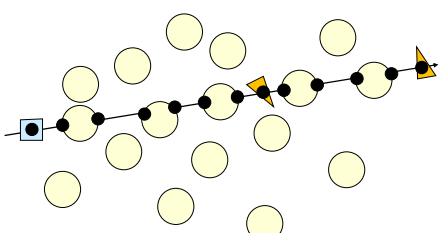



IronCad


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In a Raytracing, each ray typically hits a lot of Things



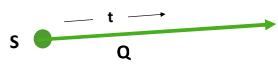

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Parametrizing a Ray


Given:
S is the (x,y,z) starting point
Q is the (x,y,z) direction of travel

Then, the (x,y,z) position of a point **p** at some position along its direction of travel is:



$$p = S + tQ$$

$$t \geq 0.$$


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Example: The Ray Intersection Process for a Sphere

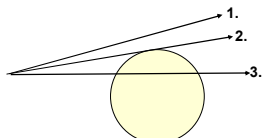
Sphere equation: $(x-x_c)^2 + (y-y_c)^2 + (z-z_c)^2 = R^2$
 Ray equation: $(x,y,z) = (x_0,y_0,z_0) + t(dx,dy,dz)$


Plugging (x,y,z) from the second equation into the first equation and multiplying-through and simplifying gives:

$At^2 + Bt + C = 0 \quad \rightarrow \quad t_1, t_2 = \frac{-B \pm \sqrt{B^2 - 4AC}}{2A}$

Solve for t_1, t_2 and analyze the solution like this:

1. If both t_1 and t_2 are complex (i.e., have an imaginary component), then the ray missed the sphere completely.
2. If both t_1 and t_2 are real and identical, then the ray brushed the sphere at a tangent point.
3. If both t_1 and t_2 are real and different, then the ray entered and exited the sphere.




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Parameterizing a Triangle

It's often useful to be able to parameterize a triangle into (u,v) , like this:

Note! There is no place in this triangle where $u = 1$ and $v = 1$.

$$p = P_0 + u*(P_1 - P_0) + v*(P_2 - P_0)$$

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The Setup

We want to find out where the ray intersects the triangle.
That is, where is the point P that is common to both the ray and the triangle?

Such that:

$$\begin{aligned} t &\geq 0. \\ 0 &\leq u \leq 1. \\ 0 &\leq v \leq 1-u. \end{aligned}$$

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Equation Setup

Triangle: $p = P_0 + u*(P_1 - P_0) + v*(P_2 - P_0)$
Ray: $p = S + tQ$

Re-arranging:
 $P_0 + u*(P_1 - P_0) + v*(P_2 - P_0) = S + tQ$

Re-arranging some more:
 $-tQ + u*(P_1 - P_0) + v*(P_2 - P_0) = S - P_0$

Then collecting terms, we get:
 $At + Bu + Cv = D$

where:

$$\begin{aligned} A &= -Q \\ B &= P_1 - P_0 \\ C &= P_2 - P_0 \\ D &= S - P_0 \end{aligned}$$

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Three Equations, Three Unknowns

Remembering that this equation is really 3 equations in (x,y,z) :

$$At + Bu + Cv = D$$

we have 3 equations with 3 unknowns, which can be cast into a matrix form

$$\begin{bmatrix} A_x & B_x & C_x \\ A_y & B_y & C_y \\ A_z & B_z & C_z \end{bmatrix} \begin{bmatrix} t \\ u \\ v \end{bmatrix} = \begin{bmatrix} D_x \\ D_y \\ D_z \end{bmatrix}$$

Our goal is to solve this for t^* , u^* , and v^*

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Solve for (t^*, u^*, v^*) using Cramer's Rule

$$\begin{bmatrix} A_x & B_x & C_x \\ A_y & B_y & C_y \\ A_z & B_z & C_z \end{bmatrix} \begin{bmatrix} t \\ u \\ v \end{bmatrix} = \begin{bmatrix} D_x \\ D_y \\ D_z \end{bmatrix}$$

$$D_0 = \det \begin{bmatrix} A_x & B_x & C_x \\ A_y & B_y & C_y \\ A_z & B_z & C_z \end{bmatrix}$$

$$D_t = \det \begin{bmatrix} D_x & B_x & C_x \\ D_y & B_y & C_y \\ D_z & B_z & C_z \end{bmatrix} \quad t^* = \frac{D_t}{D_0}$$

$$D_u = \det \begin{bmatrix} A_x & D_x & C_x \\ A_y & D_y & C_y \\ A_z & D_z & C_z \end{bmatrix} \quad u^* = \frac{D_u}{D_0}$$

$$D_v = \det \begin{bmatrix} A_x & B_x & D_x \\ A_y & B_y & D_y \\ A_z & B_z & D_z \end{bmatrix} \quad v^* = \frac{D_v}{D_0}$$

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The Steps

1. Compute D_0
2. If $D_0 \approx 0$, then the ray is *parallel* to the plane of the triangle **STOP**
3. Compute D_t
4. Compute t^*
5. If $t^* < 0$, the ray goes away from the triangle **STOP**
6. Compute D_u
7. Compute u^*
8. If $u^* < 0$ or $u^* > 1$, then the ray hits outside the triangle **STOP**
9. Compute D_v
10. Compute v^*
11. If $v^* < 0$ or $v^* > 1 - u^*$, then the ray hits outside the triangle **STOP**
12. The intersection is at the point $p = S + Qt^*$

This is known as the **Möller-Trumbore Triangle Intersection Algorithm**

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