

# Animating Wave Motion using Gerstner Waves

## How Do Waves Work?

**Gerstner Wave Equations**

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Horizontal Motion → $x' = x - \sum_{m=0}^{M-1} A_m \cos \gamma_m \sin \theta_m$	$(x, y, z) = \text{original vertex coordinates}$ $(x', y', z') = \text{displaced vertex coordinates}$
Vertical Motion → $y' = \sum_{m=0}^{M-1} A_m \cos \theta_m$	
Horizontal Motion → $z' = z - \sum_{m=0}^{M-1} A_m \sin \gamma_m \sin \theta_m$	

  

$$\theta_m = k_m \cos \gamma_m x + k_m \sin \gamma_m y - \omega_m t - \phi_m$$

$$A_m = \text{Amplitude}$$

$$\omega_m = \sqrt{gk_m}$$
  


$\gamma_m = \text{Wave propagation angle}$

$k_m = \text{Wave density}$

$t = \text{time}$

$\phi_m = \text{Wave phase shift}$

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```

##OpenGL GLIB
Perspective 70
LookAt 0 0 7 0 0 0 0 1 0
Timer 60

Vertex gerstner.vert
Fragment gerstner.frag
Program Gerstner
    uTimeScale <1.2. 100.>
    \ uM0d <0. 2.1>
    \ uM0d <0.1.1.5>
    \ uGammaM <1.57080 0. 1.57080>
    \ uM1t <0. 0.1>
    \ uM1t <0.1.2.5>
    \ uPhM1 <0. 6.28>
    \ uGammaM <1.57080 0. 1.57080>
    \ uLightX <-20. 0.20>
    \ uLightY <1. 10.20>
    \ uLightZ <-20. -20.20>
    \ uKd <0. 6.1>
    \ uKs <0. 3.1>
    \ uShininess <1.2. 200>
    \ uColor {11. 8.1}
    \ uhbaseAmp <0. 1.1>
    \ uhisurfreq <.1.1.2>
\

QuadXZ -0.2 3. 300 300

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gerstner.vert, I

gerstner.vert, II

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```

// m = 0
{
    float phIM0 = 0.; // m=0 is the phase baseline
    float wmt0 = sqrt(G*mu0*lambda0);
    float theta0 = g*Vertex.x*uKm0*cos(uGamma0) + g*Vertex.z*uKm0*sin(uGamma0) - wmt0*Time*uTimeScale - phiM0;
    newx = uKm0*cos(uGamma0)*sin(uTheta0);
    newy += uKm0*cos(uTheta0);
    newz += uKm0*(uGamma0)*sin(uTheta0);

    float dtheta0m0 = uKm0*cos(uGamma0);
    float dtheta0mt0 = uKm0*uGamma0;
    ddata = uKm0*cos(uGamma0)*cos(uTheta0)/dtheta0m0;
    dyda = uKm0*sin(uTheta0)/dtheta0m0;
    dzda = uKm0*uGamma0*cos(uTheta0)/dtheta0m0;
    ddata2 = uKm0*cos(uGamma0)*cos(uTheta0)/dtheta0mt0;
    dyda2 = uKm0*sin(uTheta0)/dtheta0mt0;
    dzda2 := uKm0*uGamma0*cos(uTheta0)/dtheta0mt0;

    jacob0 = dtheta0m0*dtheta0mt0;
}

// m = 1
{
    float wmt1 = sqrt(G*mu1*lambda1);
    float theta1 = g*Vertex.x*uKm1*cos(uGamma1) + g*Vertex.z*uKm1*sin(uGamma1) - wmt1*Time*uTimeScale - phiM1;
    newx = uKm1*cos(uGamma1)*sin(uTheta1);
    newy += uKm1*cos(uTheta1);
    newz += uKm1*(uGamma1)*sin(uTheta1);

    float dtheta1m1 = uKm1*cos(uGamma1);
    float dtheta1mt1 = uKm1*uGamma1;
    ddata = uKm1*cos(uGamma1)*cos(uTheta1)/dtheta1m1;
    dyda = uKm1*sin(uTheta1)/dtheta1m1;
    dzda = uKm1*uGamma1*cos(uTheta1)/dtheta1m1;
    ddata2 = uKm1*cos(uGamma1)*cos(uTheta1)/dtheta1mt1;
    dyda2 = uKm1*sin(uTheta1)/dtheta1mt1;
    dzda2 := uKm1*uGamma1*cos(uTheta1)/dtheta1mt1;

    jacob1 = dtheta1m1*dtheta1mt1;
}

```

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**gerstner.vert, III** 7

```

vec3 newVertex = vec3( newx, newy, newz );
uMC = newVertex;

vec3 ta = vec3( dxa, dyta, dza );
vec3 tb = vec3( dxb, dytb, dzb );
vNs = normalize( gl_NormalMatrix*cross( tb, ta ) );
// surface normal vector

vec4 ECposition = gl_ModelViewMatrix * vec4( newVertex, 1. );
vLs = normalize( eyeLightPosition - ECposition.xyz );
vEs = normalize( vec3( 0., 0., 0. ) - ECposition.xyz );
gl_Position = gl_ModelViewProjectionMatrix * vec4( newVertex, 1. );
}

```

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**gerstner.frag, I** 8

```

#version 330 compatibility
in vec3
in vec3
in vec3
in vec3
uniform float
uniform vec4
uniform float
uniform int
uniform float
uniform float
uniform float
uniform float
const vec4 WHITE = ( 1., 1., 1., 1. );

vec3 RotateNormal( float angx, float angy, vec3 n )
{
    float cx = cos( angx );
    float sx = sin( angx );
    float cy = cos( angy );
    float sy = sin( angy );

    // rotate about x:
    float px = n.y*cx - n.z*sx;    // y
    float nx = n.x;
    float ny = n.y;
    float nz = n.z;
    // rotate about y:
    float xp = n.x*cy + n.z*sy;    // x
    float xz = n.z;
    float xp = n.x;
    float ny = n.y;
    float nz = n.z;
    return normalize( n );
}

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**gerstner.frag, II** 9

```

void main()
{
    vec4 nvx = texture3D( Noise3, uNoiseFreq*uMC );
    vec4 nvy = texture3D( Noise3, uNoiseFreq*vec3(uMC.xy,uMC.z+0.5) );
    float angx = nvx.r + nvx.g + nvx.b + nvx.a; // 1. > 3.
    angy = angy - 2.; // -1. > 1.
    angx *= uNoiseAmp;
    float angy = myr + my.g + my.b + my.a; // 1. > 3.
    angy = angy - 2.; // -1. > 1.
    angy *= uNoiseAmp;
    vec3 normal = normalize(vNs);
    vec3 light = normalize(vLs);
    vec3 eye = normalize(vEs);
    normal = RotateNormal( angx, angy, normal );
    vec4 ambient = uKa * uColor;
    float d = max( dot(normal.light), 0. );
    d = abs( dot(normal.light) );
    vec4 diffuse = uKd * d * uColor;
    float s = 0;
    if( dot(normal.light) > 0. ) // only do specular if the light can see the point
    {
        vec3 ref = normalize( 2. * normal * dot(normal.light) - light );
        s = pow( max( dot(eye.ref), 0. ), uShininess );
    }
    vec4 specular = uKs * s * WHITE;
    gl_FragColor = vec4( ambient.rgb + diffuse.rgb + specular.rgb, 1. );
}

```

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