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## Bump Mapping



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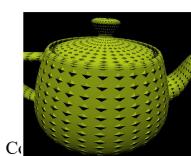
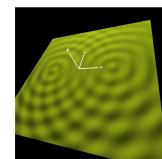
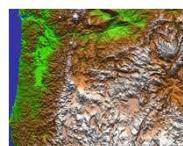


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bumpmapping.pptx

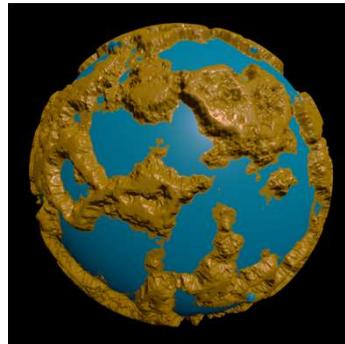
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## What is Bump-Mapping?

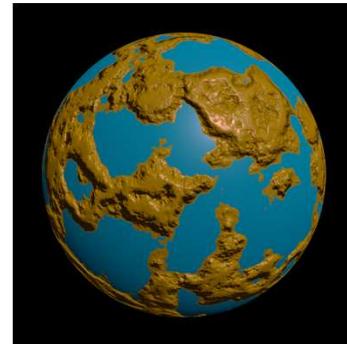
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Bump-mapping is the process of creating the illusion of 3D depth by using a manipulated surface normal in the lighting, rather than actually creating the extra surface detail.

Displacement-mapped

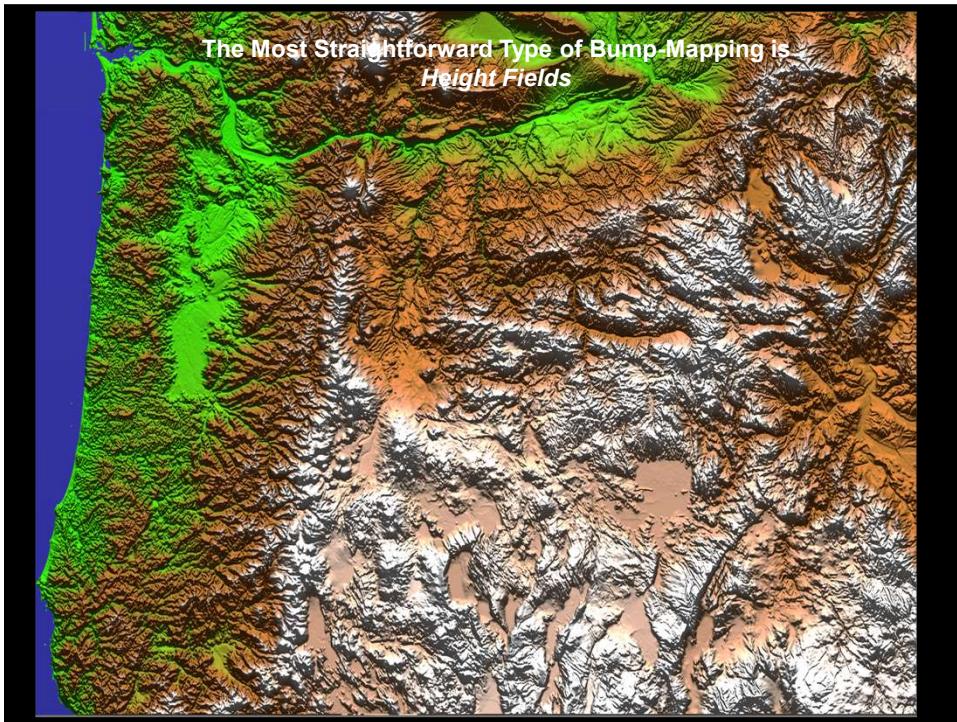


Bump-mapped



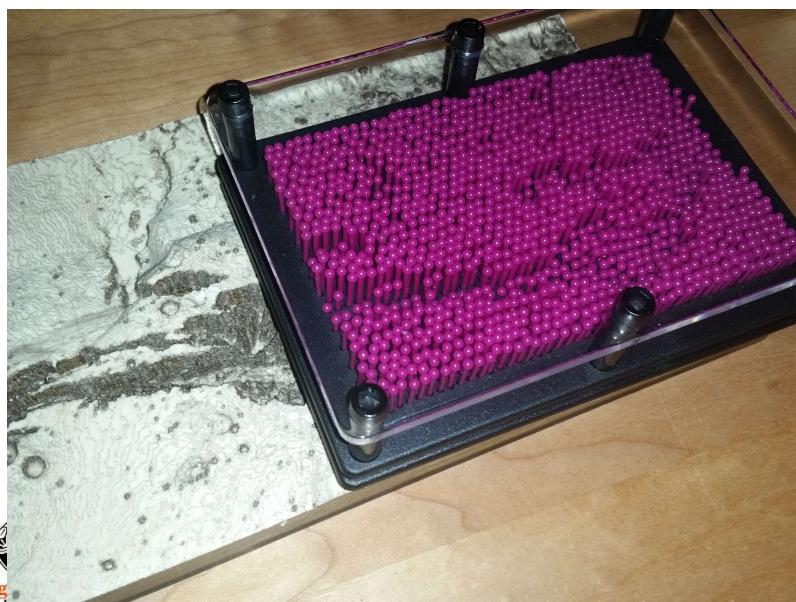
This is a good trick!  
Displacement-mapping is **per-vertex** and requires a lot of triangles.  
Bump-mapping is **per-fragment** and since you needed to process all those fragments anyway, you might as well do slightly more.

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Definition of Height Fields -- Think of the Pin Box!

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```

terrain.vert
#version 330 compatibility
out vec3 vMCposition;
out vec3 vECposition;
out vec2 vST;

void
main( )
{
    vST = gl_MultiTexCoord0.st;
    vMCposition = gl_Vertex.xyz;
    vECposition = ( gl_ModelViewMatrix * gl_Vertex ).xyz;
    gl_Position = gl_ModelViewProjectionMatrix * gl_Vertex;
}

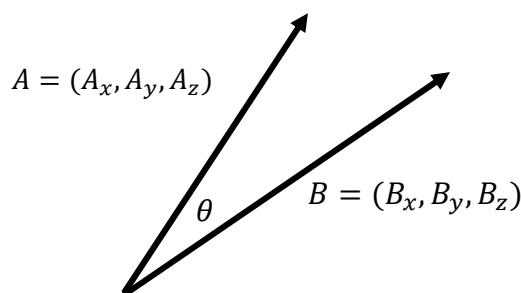
```



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### The Vector Cross Product

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$$A \times B = (A_y B_z - A_z B_y, A_z B_x - A_x B_z, A_x B_y - A_y B_x)$$

$$\|A \times B\| = \|A\| \|B\| \sin \theta$$



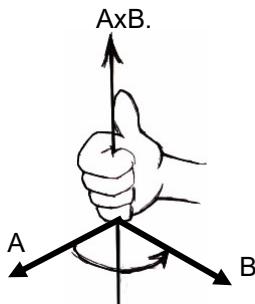
Because it produces a vector result (i.e., three numbers),  
this is also called the *Vector Product*

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## The Perpendicular Property of the Vector Cross Product

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The vector  $A \times B$  is both perpendicular to A and perpendicular to B



### The Right-Hand-Rule Property of the Cross Product

Curl the fingers of your right hand in the direction that starts at A and heads towards B. Your thumb points in the direction of AxB.



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## terrain.frag, I

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```
#version 330 compatibility

uniform float      uLightX, uLightY, uLightZ;
uniform float      uExag;
uniform vec4       uColor;
uniform sampler2D  uHgtUnit; ←
uniform bool       uUseColor;
uniform float      uLevel1;
uniform float      uLevel2;
uniform float      uTol;
uniform float      uDelta;

in vec3            vMCposition;
in vec3            vECposition;
in vec2            vST;

const float        DELTA = 0.001;

const vec3 BLUE = vec3( 0.1, 0.1, 0.5 );
const vec3 GREEN = vec3( 0.0, 0.8, 0.0 );
const vec3 BROWN = vec3( 0.6, 0.3, 0.1 );
const vec3 WHITE = vec3( 1.0, 1.0, 1.0 );

const float LNGMIN = -579240./2.;           // in meters, same as heights
const float LNGMAX = 579240./2.;
const float LATMIN = -419949./2.;
const float LATMAX = 419949./2.;
```

Floating-point texture whose **.r** component actually contains the heights (in meters)

It turns out that textures are a great place to "hide" data. They are allowed to be very large and they are fast to lookup values in.



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**terrain.frag, II**

```

void main( )
{
    vec2 stp0 = vec2( DELTA, 0. );
    vec2 st0p = vec2( 0. , DELTA );
    float west = texture2D( uHgtUnit, vST-stp0 ).r;
    float east = texture2D( uHgtUnit, vST+stp0 ).r;
    float south = texture2D( uHgtUnit, vST-st0p ).r;
    float north = texture2D( uHgtUnit, vST+st0p ).r;

    vec3 stangent = vec3( 2.*DELTA*(LNGMAX-LNGMIN), 0., uExag * ( east - west ) );
    vec3 ttangent = vec3( 0., 2.*DELTA*(LATMAX-LATMIN), uExag * ( north - south ) );
    vec3 normal = normalize( CROSS( stangent, ttangent ) );

    float LightIntensity = dot( normalize( vec3(uLightX,uLightY,uLightZ) - vMCposition ), normal );
    if( LightIntensity < 0.1 )
        LightIntensity = 0.1;
    if( uUseColor )
    {
        float here = texture2D( uHgtUnit, vST ).r;
        vec3 color = BLUE;
        if( here > 0. )
        {
            float t = smoothstep( uLevel1-uTol, uLevel1+uTol, here );
            color = mix( GREEN, BROWN, t );
        }
        if( here > uLevel1+uTol )
        {
            float t = smoothstep( uLevel2-uTol, uLevel2+uTol, here );
            color = mix( BROWN, WHITE, t );
        }
        gl_FragColor = vec4( LightIntensity*color, 1. );
    }
    else
    {
        gl_FragColor= vec4( LightIntensity*uColor.rgb, 1. );
    }
}

```

Remember that the cross product of two vectors gives you a vector that is perpendicular to both. So, the cross product of two tangent vectors gives you a good approximation to the surface normal.

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**Terrain Height Bump-mapping: Exaggerating the Height**

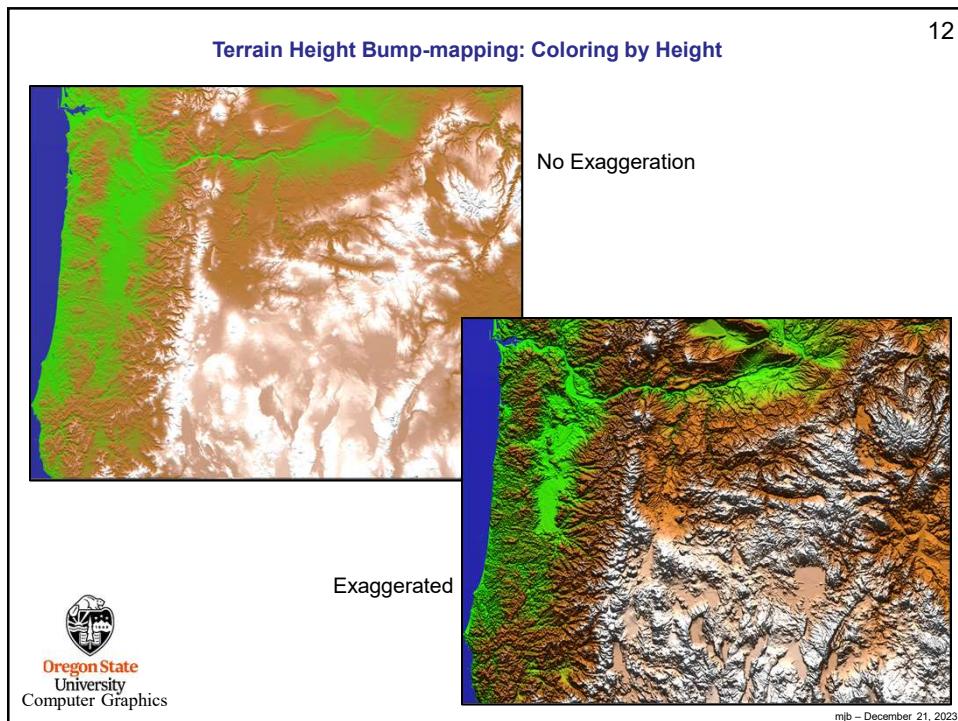
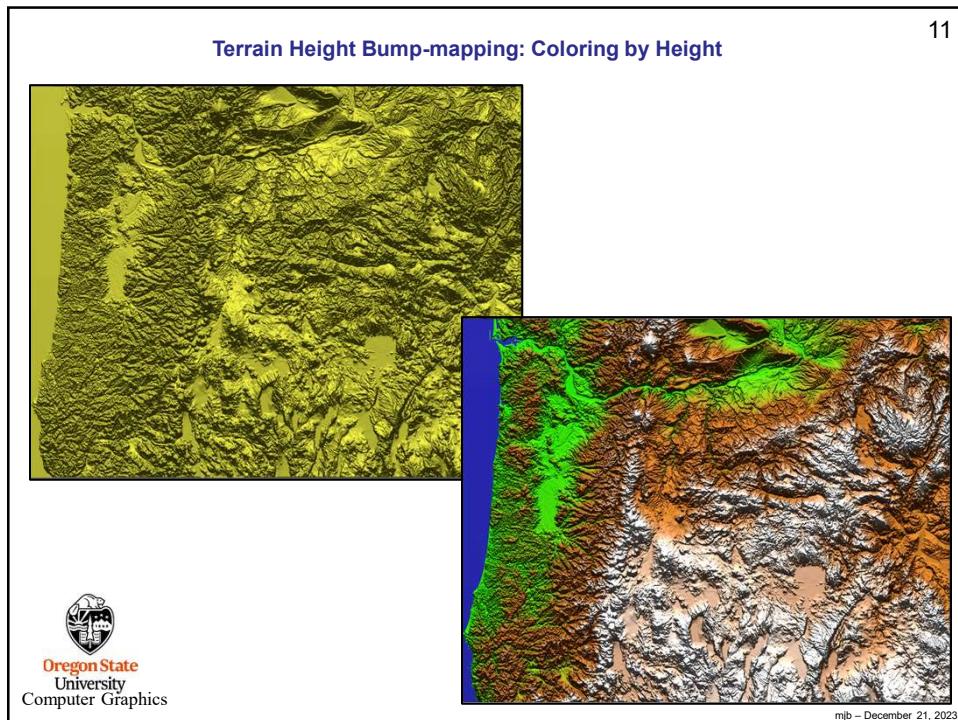
No Exaggeration

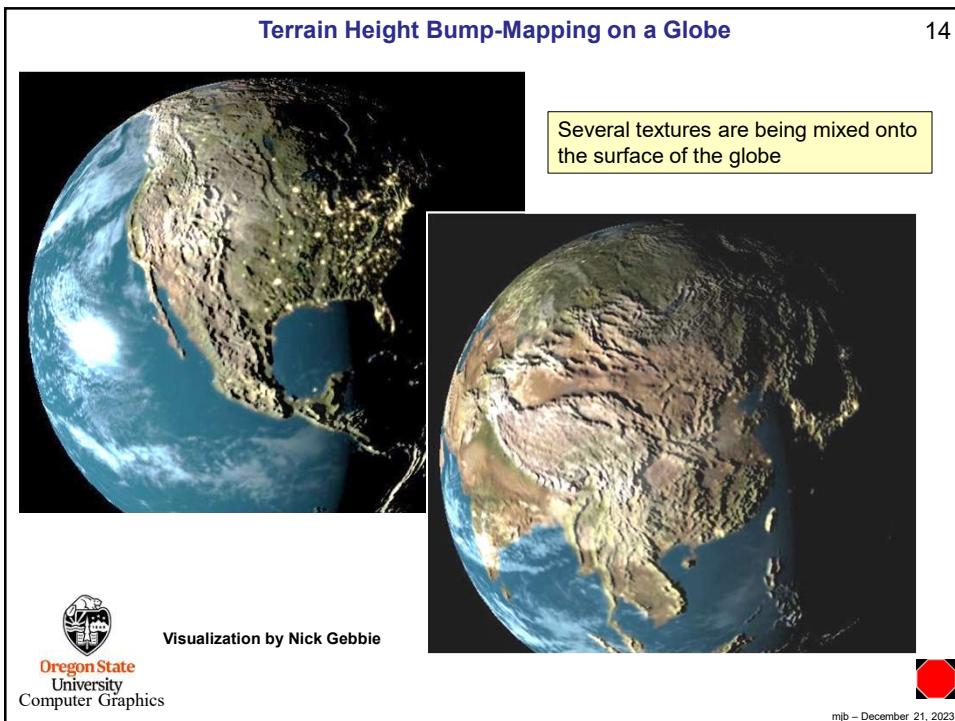
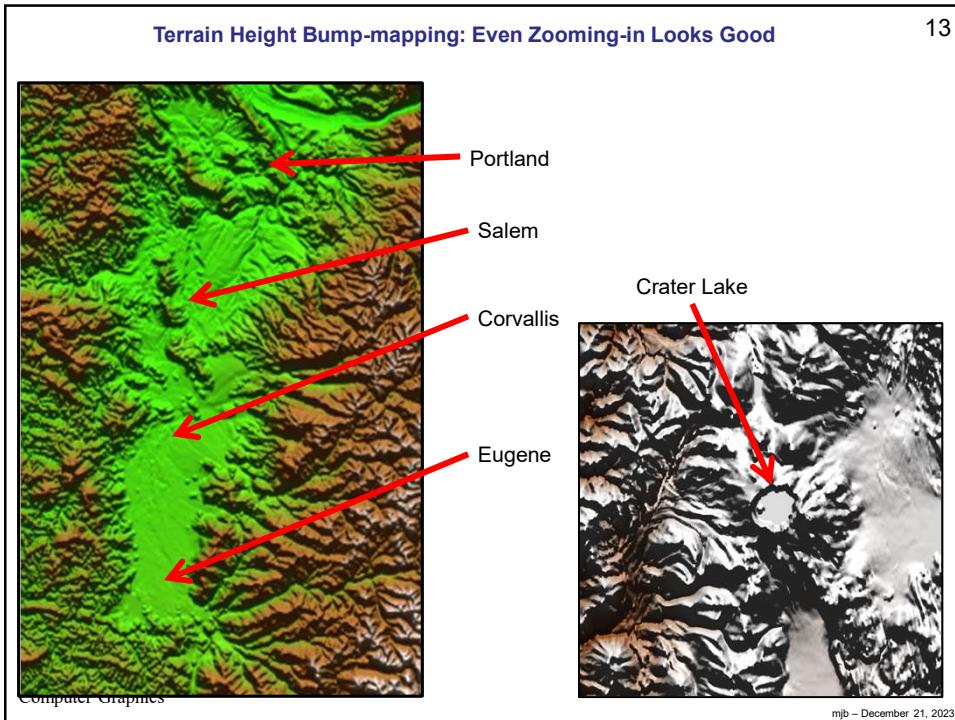
This entire geometry consists of just a single quadrilateral!

Exaggerated

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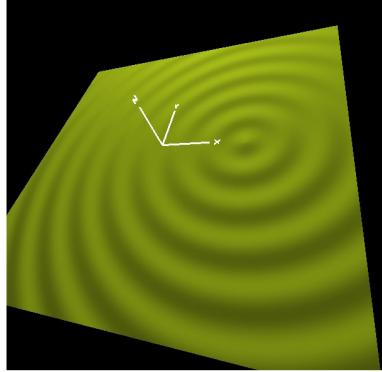
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The Second Most Straightforward Type of Bump-Mapping is  
*Height Field Equations*

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Rock Dropped

This is the coordinate system we will be using.  
The plane is X-Y with Z pointing up



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The Second Most Straightforward Type of Bump-Mapping is  
*Height Field Equations*

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$z = A\cos(2\pi Br + C)e^{-Dr}$  ← Radial-ripple height equation with decay

$\text{normal} = \text{xtangent} \times \text{ytangent}$  ← If we can get the two tangent vectors, then their **cross product** will give us the surface normal

$$\text{xtangent} = \text{vec3}(1., 0., \frac{\partial z}{\partial x}) \quad \text{ytangent} = \text{vec3}(0., 1., \frac{\partial z}{\partial y})$$

$$\frac{\partial z}{\partial x} = \frac{\partial z}{\partial r} \frac{\partial r}{\partial x} \quad \frac{\partial z}{\partial y} = \frac{\partial z}{\partial r} \frac{\partial r}{\partial y}$$

$$\frac{\partial z}{\partial r} = -A\sin(2\pi Br + C)(2\pi B)e^{-Dr} + A\cos(2\pi Br + C)(-D)e^{-Dr}$$

$r^2 = x^2 + y^2$ 
 $2r \frac{\partial r}{\partial x} = 2x$ 
 $\frac{\partial r}{\partial x} = \frac{x}{r}$

$2r \frac{\partial r}{\partial y} = 2y$ 
 $\frac{\partial r}{\partial y} = \frac{y}{r}$ 

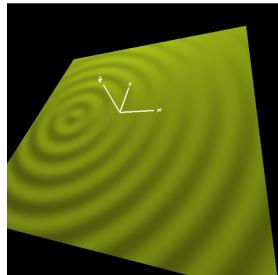
(Note:  $x/r$  and  $y/r$  are actually the cosine and sine of the polar angle.)



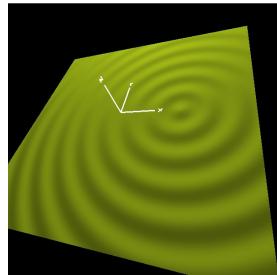
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The Second Most Straightforward Type of Bump-Mapping is  
*Height Field Equations*

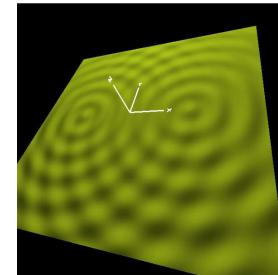
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Rock A Dropped



Rock B Dropped



Both Rocks Dropped

You can sum the individual height field equations and get the same result as summing the height field displacements



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**The *ripples* Bump-Map Shader**

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```
ripples.glib
##OpenGL GLIB

Perspective 70
LookAt 0 0 8 0 0 0 0 1 0

Vertex ripples.vert
Fragment ripples.frag
Program Ripples
    uLightX <-10. 0. 10.0>
    uLightY <-10. 10. 10.0>
    uLightZ <-10. 10. 10.0>
    uColor {0.7 0.8 0.1 1.}
    uTime <0. 0. 10.>
    uPd <.2 1. 1.5>
    uAmp0 <0. .05 .05>
    uAmp1 <0. 0. .05>
    uPhaseShift <0. 0. 6.28>

QuadXY -.1 5.
```



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**The ripples Bump-Map Shader**

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ripples.vert

```
#version 330 compatibility

out vec3 vMCposition;
out vec3 vECposition;

void
main( )
{
    vMCposition = gl_Vertex.xyz;
    vECposition = ( gl_ModelViewMatrix * gl_Vertex ).xyz;
    gl_Position = gl_ModelViewProjectionMatrix * gl_Vertex;
}
```



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**The ripples Bump-Map Shader**

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ripples.frag, I

```
#version 330 compatibility

uniform float uTime;
uniform float uAmp0, uAmp1;
uniform float uPhaseShift;
uniform float uPd;
uniform float uLightX, uLightY, uLightZ;
uniform vec4 uColor;

in vec3 vMCposition;
in vec3 vECposition;

const float TWOPI = 2.*3.14159265;
const vec3 C0 = vec3( -2.5, 0., 0. );
const vec3 C1 = vec3( 2.5, 0., 0. );

void
main( )
{
    float rad0 = length( vMCposition - C0 );
    float H0  = -uAmp0 * cos( TWOPI*rad0/uPd - TWOPI*uTime );

    float rad1 = length( vMCposition - C1 );
    float H1  = -uAmp1 * cos( TWOPI*rad1/uPd - TWOPI*uTime );

    float u = -uAmp0 * (TWOPI/uPd) * sin( TWOPI*rad0/uPd - TWOPI*uTime );
    float v = 0.;
    float w = 1.;
```



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## The *ripples* Bump-Map Shader

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### ripples.frag, II

```

float ang = atan( vMCposition.y - C0.y, vMCposition.x - C0.x );
float up = dot( vec2(u,v), vec2(cos(ang), -sin(ang)) );
float vp = dot( vec2(u,v), vec2(sin(ang), cos(ang)) );
float wp = 1.;

u = -uAmp1 * (TWOPI/uPd) * sin( TWOPI*rad1/uPd - TWOPI*uTime - uPhaseShift );
v = 0.;

ang = atan( vMCposition.y - C1.y, vMCposition.x - C1.x );
up += dot( vec2(u,v), vec2(cos(ang), -sin(ang)) );
vp += dot( vec2(u,v), vec2(sin(ang), cos(ang)) );
wp += 1.;

vec3 normal = normalize( vec3( up, vp, wp ) );

float LightIntensity = abs( dot( normalize(vec3(uLightX,uLightY,uLightZ) - vECposition), normal ) );
if( LightIntensity < 0.1 )
    LightIntensity = 0.1;

gl_FragColor = vec4( LightIntensity*uColor.rgb, uColor.a );
}

```



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## Combining Bump and Cube Mapping

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