Bump Mapping

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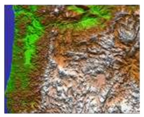
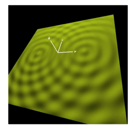
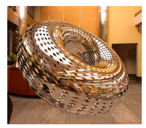


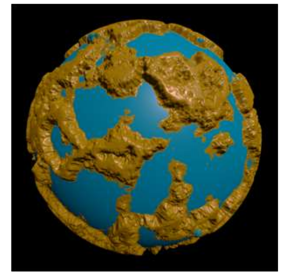




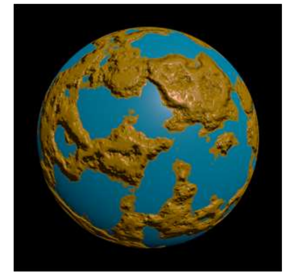
What is Bump-Mapping?

Bump-mapping is the process of creating the illusion of 3D depth by using a manipulated surface normal in the lighting, rather than actually creating the extra surface detail.

Displacement-mapped

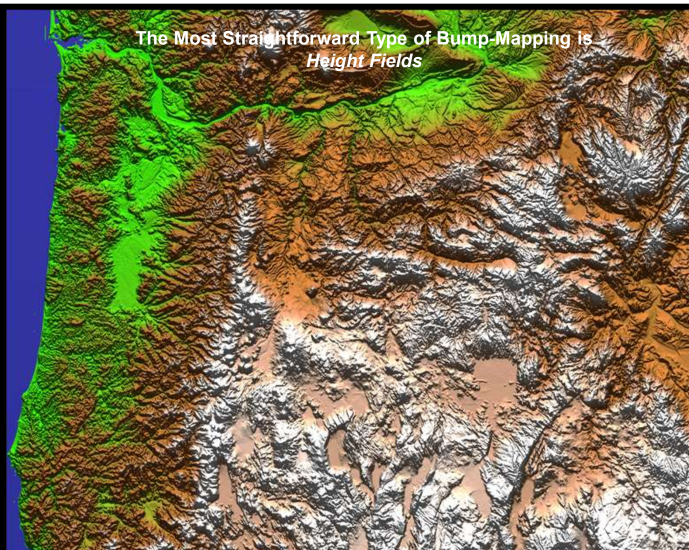


Bump-mapped

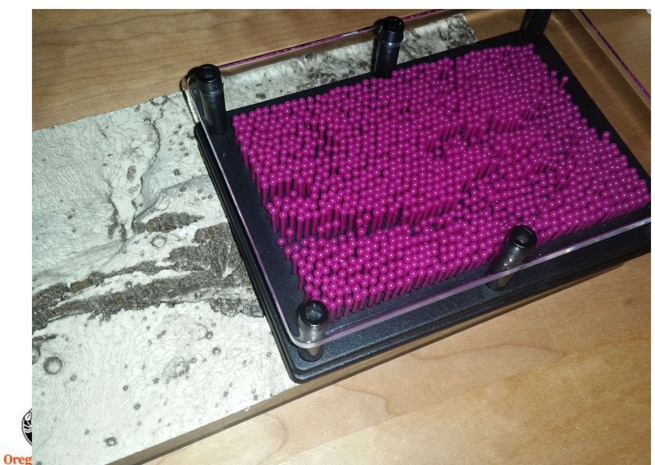


This is a good trick!
Displacement-mapping is **per-vertex** and requires a lot of triangles.
Bump-mapping is **per-fragment** and since you needed to process all those fragments anyway, you might as well do slightly more.

The Most Straightforward Type of Bump-Mapping is *Height Fields*



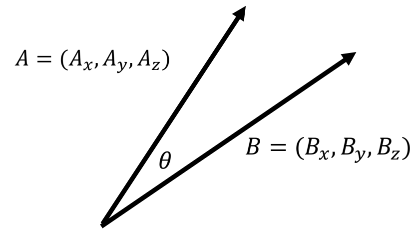
Definition of Height Fields -- Think of the Pin Box!



terrain.vert

```
#version 330 compatibility
out vec3  vMCposition;
out vec3  vECposition;
out vec2  vST;

void
main( )
{
   vST = gl_MultiTexCoord0.st;
   vMCposition = gl_Vertex .xyz;
   vECposition = ( gl_ModelViewMatrix * gl_Vertex ).xyz;
   gl_Position = gl_ModelViewProjectionMatrix * gl_Vertex;
}
```


The Vector Cross Product



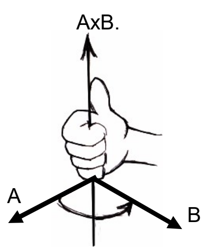
$$A \times B = (A_y B_z - A_z B_y, A_z B_x - A_x B_z, A_x B_y - A_y B_x)$$

$$\|A \times B\| = \|A\| \|B\| \sin\theta$$

Because it produces a vector result (i.e., three numbers), this is also called the *Vector Product*

The Perpendicular Property of the Vector Cross Product

The vector $A \times B$ is both perpendicular to A and perpendicular to B



The Right-Hand-Rule Property of the Cross Product

Curl the fingers of your right hand in the direction that starts at A and heads towards B. Your thumb points in the direction of AxB.

terrain.frag, I

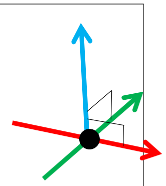

```
#version 330 compatibility

uniform float           uLightX, uLightY, uLightZ;
uniform float           uExag;
uniform vec4            uColor;
uniform sampler2D       uHgtUnit;
uniform bool            uUseColor;
uniform float           uLevel1;
uniform float           uLevel2;
uniform float           uTol;
uniform float           uDelta;

in vec3                 vMCposition;
in vec3                 vECposition;
in vec2                 vST;

const  float  DELTA =   0.001;

const vec3 BLUE  =    vec3( 0.1, 0.1, 0.5 );
const vec3 GREEN =    vec3( 0.0, 0.8, 0.0 );
const vec3 BROWN = vec3( 0.6, 0.3, 0.1 );
const vec3 WHITE =    vec3( 1.0, 1.0, 1.0 );

const float LNGMIN  = -579240./2.;          // in meters, same as heights
const float LNGMAX =  579240./2.;
const float LATMIN   = -419949./2.;
const float LATMAX  =  419949./2.;
```

Floating-point texture whose **.r** component actually contains the heights (in meters)

It turns out that textures are a great place to “hide” data. They are allowed to be very large and they are fast to lookup values in.

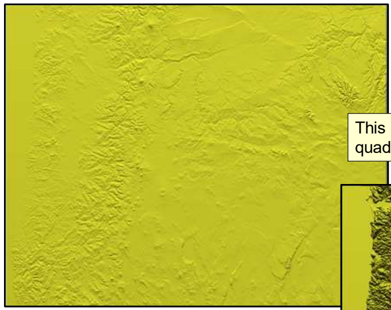
terrain.frag, II

```
void main( )
{
        vec2 stp0 = vec2( DELTA,  0. );
        vec2 st0p = vec2( 0.   ,  DELTA );
        float west  =  texture2D( uHgtUnit, vST-stp0 ).r;
        float east   =  texture2D( uHgtUnit, vST+stp0 ).r;
        float south =  texture2D( uHgtUnit, vST-st0p ).r;
        float north  =  texture2D( uHgtUnit, vST+st0p ).r;

        vec3 stangent = vec3( 2.*DELTA*(LNGMAX-LNGMIN), 0., uExag * ( east - west ) );
        vec3 ttangent  = vec3( 0., 2.*DELTA*(LATMAX-LATMIN), uExag * ( north - south ) );
        vec3 normal = normalize(  cross( stangent, ttangent )  );

        float LightIntensity  = dot( normalize( vec3(uLightX,uLightY,uLightZ) – vMCposition ), normal );
        if( LightIntensity < 0.1 )
                LightIntensity = 0.1;
        if( uUseColor )
        {
                float here = texture2D( uHgtUnit, vST ).r;
                vec3 color = BLUE;
                if( here > 0. )
                {
                        float t = smoothstep( uLevel1-uTol, uLevel1+uTol, here );
                        color = mix( GREEN, BROWN, t );
                }
                if( here > uLevel1+uTol )
                {
                        float t = smoothstep( uLevel2-uTol, uLevel2+uTol, here );
                        color = mix( BROWN, WHITE, t );
                }
                gl_FragColor = vec4( LightIntensity*color, 1. );
        }
        else
        {
                gl_FragColor= vec4( LightIntensity*uColor.rgb, 1. );
        }
}
```



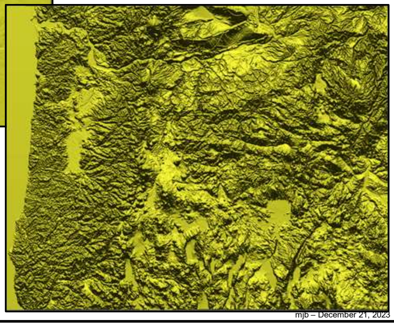
Remember that the cross product of two vectors gives you a vector that is perpendicular to both. So, the cross product of two tangent vectors gives you a good approximation to the surface normal.

Terrain Height Bump-mapping: Exaggerating the Height



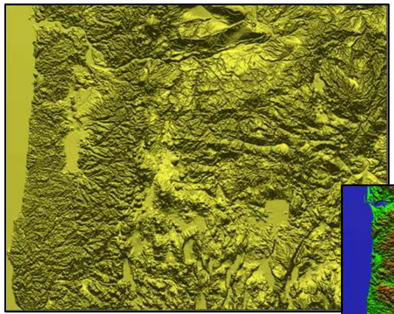
No Exaggeration

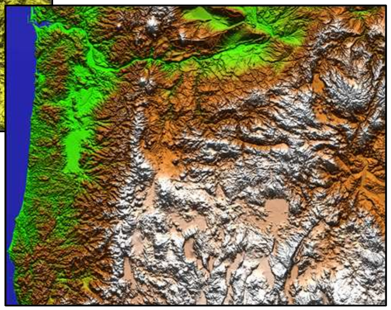
This entire geometry consists of just a single quadrilateral!



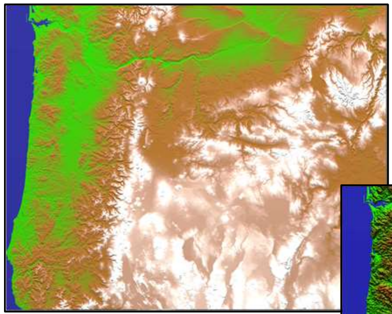
Exaggerated

Terrain Height Bump-mapping: Coloring by Height

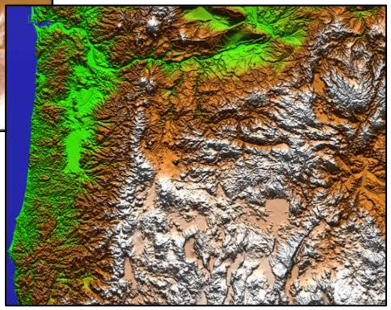




Terrain Height Bump-mapping: Coloring by Height

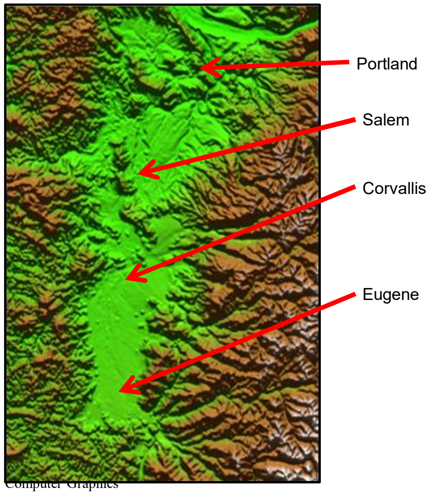


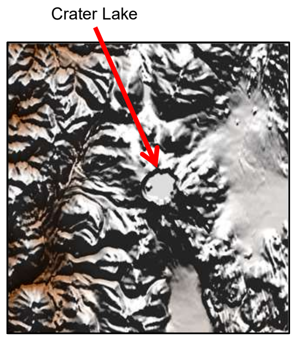
No Exaggeration



Exaggerated

Terrain Height Bump-mapping: Even Zooming-in Looks Good



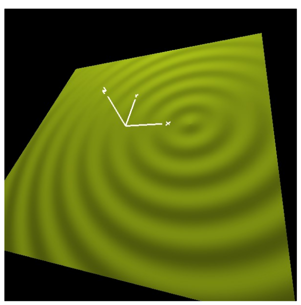


Terrain Height Bump-Mapping on a Globe

Several textures are being mixed onto the surface of the globe

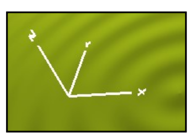
Visualization by Nick Gebbie

The Second Most Straightforward Type of Bump-Mapping is *Height Field Equations*



Rock Dropped

This is the coordinate system we will be using.
The plane is X-Y with Z pointing up



The Second Most Straightforward Type of Bump-Mapping is *Height Field Equations*

$$z = A\cos(2\pi Br + C)e^{-Dr}$$ ← Radial-ripple height equation with decay

$$normal = xtangent \;\; \mathrm{x} \;\; ytangent$$ ← If we can get the two tangent vectors, then their **cross product** will give us the surface normal

$$xtangent = vec3(1.,0.,\frac{\partial z}{\partial x}) \qquad ytangent = vec3(0.,1.,\frac{\partial z}{\partial y})$$

$$\frac{\partial z}{\partial x} = \frac{\partial z}{\partial r}\frac{\partial r}{\partial x} \qquad \frac{\partial z}{\partial y} = \frac{\partial z}{\partial r}\frac{\partial r}{\partial y}$$

$$\frac{\partial z}{\partial r} = -A\sin(2\pi Br + C)(2\pi B)e^{-D} + A\cos(2\pi Br + C)(-D)e^{-Dr}$$

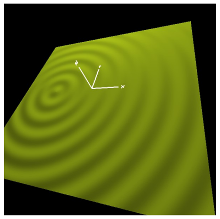
$$r^2 = x^2 + y^2$$

$$2r\frac{\partial r}{\partial x} = 2x \qquad \frac{\partial r}{\partial x} = \frac{x}{r}$$

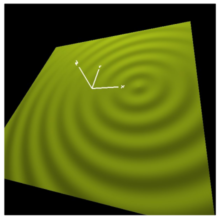
$$2r\frac{\partial r}{\partial y} = 2y \qquad \frac{\partial r}{\partial y} = \frac{y}{r}$$

(Note: x/r and y/r are actually the cosine and sine of the polar angle.)

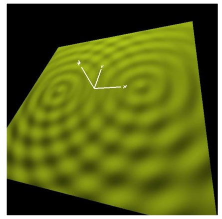
The Second Most Straightforward Type of Bump-Mapping is *Height Field Equations*



Rock A Dropped



Rock B Dropped



Both Rocks Dropped

You can sum the individual height field equations and get the same result as summing the height field displacements

The *ripples* Bump-Map Shader

ripples.glib

```
##OpenGL GLIB

Perspective 70
LookAt 0 0 8  0 0 0  0 1 0


Vertex   ripples.vert
Fragment ripples.frag
Program  Ripples                        \
      uLightX <-10.  0. 10.0>           \
      uLightY <-10. 10. 10.0>           \
      uLightZ <-10. 10. 10.0>           \
      uColor {0.7 0.8 0.1 1.}           \
      uTime <0. 0. 10.>                 \
      uPd <.2 1. 1.5>                   \
      uAmp0 <0. .05 .05>                \
      uAmp1 <0. 0. .05>                 \
      uPhaseShift <0. 0. 6.28>

QuadXY  -.1  5.
```


The *ripples* Bump-Map Shader

ripples.vert

```
#version 330 compatibility

out vec3  vMCposition;
out vec3  vECposition;

void
main( )
{
      vMCposition = gl_Vertex.xyz;
      vECposition = ( gl_ModelViewMatrix * gl_Vertex ).xyz;
      gl_Position = gl_ModelViewProjectionMatrix * gl_Vertex;
}
```


The *ripples* Bump-Map Shader

ripples.frag, I

```
#version 330 compatibility

uniform float uTime;
uniform float uAmp0, uAmp1;
uniform float uPhaseShift;
uniform float uPd;
uniform float uLightX, uLightY, uLightZ;
uniform vec4  uColor;

in vec3  vMCposition;
in vec3  vECposition;

const float TWOPI = 2.*3.14159265;
const vec3 C0 = vec3( -2.5, 0., 0. );
const vec3 C1 = vec3(  2.5, 0., 0. );

void
main( )
{
      float rad0 = length( vMCposition - C0 );
      float H0   = -uAmp0 * cos( TWOPI*rad0/uPd - TWOPI*uTime );

      float rad1 = length( vMCposition - C1 );
      float H1   = -uAmp1 * cos( TWOPI*rad1/uPd - TWOPI*uTime );

      float u = -uAmp0 * (TWOPI/uPd) * sin( TWOPI*rad0/uPd - TWOPI*uTime );
      float v = 0.;
      float w = 1.;
```

The *ripples* Bump-Map Shader

ripples.frag, II

```
	float ang = atan( vMCposition.y - C0.y, vMCposition.x - C0.x );
	float up = dot( vec2(u,v), vec2(cos(ang), -sin(ang)) );
	float vp = dot( vec2(u,v), vec2(sin(ang),  cos(ang)) );
	float wp = 1.;

	u = -uAmp1 * (TWOPI/uPd) * sin( TWOPI*rad1/uPd - TWOPI*uTime - uPhaseShift );
	v = 0.;
	ang = atan( vMCposition.y - C1.y, vMCposition.x - C1.x );
	up += dot( vec2(u,v), vec2(cos(ang), -sin(ang)) );
	vp += dot( vec2(u,v), vec2(sin(ang),  cos(ang)) );
	wp += 1.;
	vec3 normal = normalize( vec3( up, vp, wp ) );

	float LightIntensity  = abs( dot( normalize(vec3(uLightX,uLightY,uLightZ) - vECposition), normal ) );
	if( LightIntensity < 0.1 )
		LightIntensity = 0.1;

	gl_FragColor = vec4( LightIntensity*uColor.rgb, uColor.a );
}
```


Combining Bump and Cube Mapping