Performing Reductions in OpenCL

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Recall the OpenCL Memory Model

- Kernel
  - Global Memory
  - Constant Memory
  - WorkGroup
    - Shared Memory
      - WorkItem: Private Memory
      - WorkItem: Private Memory
      - WorkItem: Private Memory
Here’s the Problem We are Trying to Solve

Like the first.cpp demo program, we are piecewise multiplying two arrays. Unlike the first demo program, we want to then add up all the products and return the sum.

\[
\begin{align*}
& A \times B \rightarrow \text{prods} \\
& \sum \text{prods} \rightarrow C
\end{align*}
\]

After the array multiplication, we want each work-group to sum the products within that work-group, then return them to the host in an array for final summing.

To do this, we will not put the products into a large global device array, but into a `prods[]` array that is shared within its work-group.
Reduction Takes Place in a Single Work-Group

numItems = 8;

If we had 8 work-items in a work-group, we would like the threads in each work-group to execute the following instructions . . .

Thread #0:
prods[ 0 ] += prods[ 1 ];

Thread #2:
prods[ 2 ] += prods[ 3 ];

Thread #4:
prods[ 4 ] += prods[ 5 ];

Thread #6:
prods[ 6 ] += prods[ 7 ];

. . . but in a more general way than writing them all out by hand.
Here's What You Would Change in your Host Program

```c
size_t numWorkGroups = NUM_ELEMENTS / LOCAL_SIZE;

float * hA = new float [ NUM_ELEMENTS ];
float * hB = new float [ NUM_ELEMENTS ];
float * hC = new float [ numWorkGroups ];
size_t abSize = NUM_ELEMENTS * sizeof(float);
size_t cSize = numWorkGroups * sizeof(float);

cl_mem dA = clCreateBuffer( context, CL_MEM_READ_ONLY,   abSize, NULL, &status );
cl_mem dB = clCreateBuffer( context, CL_MEM_READ_ONLY,   abSize, NULL, &status );
cl_mem dC = clCreateBuffer( context, CL_MEM_WRITE_ONLY ,   cSize, NULL, &status );

status = clEnqueueWriteBuffer( cmdQueue, dA, CL_FALSE, 0, abSize, hA, 0, NULL, NULL );
status = clEnqueueWriteBuffer( cmdQueue, dB, CL_FALSE, 0, abSize, hB, 0, NULL, NULL );

cl_kernel kernel = clCreateKernel( program, "ArrayMultReduce", &status );

status = clSetKernelArg( kernel, 0, sizeof(cl_mem), &dA );
status = clSetKernelArg( kernel, 1, sizeof(cl_mem), &dB );
status = clSetKernelArg( kernel, 2, LOCAL_SIZE * sizeof(float), NULL );
status = clSetKernelArg( kernel, 3, sizeof(cl_mem), &dC );
```

This NULL is how you tell OpenCL that this is a local (shared) array, not a global array.

\[ A \times B \rightarrow \text{prods} \]
\[ \sum \text{prods} \rightarrow C \]
The Arguments to the Kernel

```c
kernel void ArrayMultReduce( global const float *dA, global const float *dB, local float *prods, global float *dC )
{
    int gid = get_global_id( 0 );       // 0 .. total_array_size-1
    int numItems = get_local_size( 0 );     // # work-items per work-group
    int tnum = get_local_id( 0 );        // thread (i.e., work-item) number in this work-group
                                            // 0 .. numItems-1
    int wgNum = get_group_id( 0 );      // which work-group number this is in

    prods[ tnum ] = dA[ gid ] * dB[ gid ];   // multiply the two arrays together

    // now add them up – come up with one sum per work-group
    // it is a big performance benefit to do it here while “prods” is still available – and is local
    // it would be a performance hit to pass “prods” back to the host then bring it back to the device for reduction
```
Reduction Takes Place Within a Single Work-Group
Each work-item is run by a single thread

Thread #0:
prods[ 0 ] += prods[ 1 ];
Thread #2:
prods[ 2 ] += prods[ 3 ];
Thread #4:
prods[ 4 ] += prods[ 5 ];
Thread #6:
prods[ 6 ] += prods[ 7 ];

Offset = 1; Mask = 1;

offset = 4; mask = 7;

offset = 2; mask = 3;

A work-group consisting of numItems work-items can be reduced to a sum in \( \log_2(\text{numItems}) \) steps. In this example, numItems=8.

The reduction begins with the individual products in prods[0] .. prods[7].

The final sum will end up in prods[0], which will then be copied into dC[wgNum].
A Review of Bitmasks

Remember *Truth Tables*?

\[
\begin{array}{c|c|c|c}
& F & F & T & T \\
\hline
& \mathbf{F} & \mathbf{F} & \mathbf{T} & \mathbf{T} \\
\hline
& \mathbf{F} & \mathbf{F} & \mathbf{F} & \mathbf{T} \\
\end{array}
\]

Or, with Bits:

\[
\begin{array}{c|c|c|c}
0 & 0 & 1 & 1 \\
\hline
& 0 & 1 & 0 & 1 \\
\hline
& 0 & 0 & 0 & 1 \\
\end{array}
\]

Or, with Multiple Bits:

\[
\begin{array}{c|c|c|c|c|c|c}
000 & 001 & 010 & 011 & 100 & 101 \\
\hline
& 011 & 011 & 011 & 011 & 011 & 011 \\
\hline
& = 000 & = 001 & = 010 & = 011 & = 000 & = 001 \\
\end{array}
\]
Reduction Takes Place in a Single Work-Group
Each work-item is run by a single thread

Thread #0:
prods[ 0 ] += prods[ 1 ];

Thread #2:
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Thread #4:
prods[ 4 ] += prods[ 5 ];

Thread #6:
prods[ 6 ] += prods[ 7 ];

offset = 1;
mask = 1;

offset = 2;
mask = 3;

offset = 4;
mask = 7;

offset = 1;
mask = 1;

offset = 2;
mask = 3;

offset = 4;
mask = 7;

\[ \sum \text{prods} \rightarrow C \]

numItems = 8;

// all threads execute this code simultaneously:
for(int offset = 1; offset < numItems; offset *= 2)
{
    int mask = 2*offset - 1;
    barrier(CLK_LOCAL_MEM_FENCE); // wait for all threads to get here
    if((tnum & mask) == 0) // bit-by-bit and'ing tells us which
    { // threads need to do work now
        prods[tnum] += prods[tnum + offset];
    }
}

barrier(CLK_LOCAL_MEM_FENCE);
if(tnum == 0)
    dC[wgNum] = prods[0];

Kernel void
ArrayMultReduce( ... )
int gid = get_global_id( 0 );
int numItems = get_local_size( 0 );
int tnum = get_local_id( 0 ); // thread number
int wgNum = get_group_id( 0 ); // work-group number
And, Finally, in your Host Program

Wait( cmdQueue );
double time0 = omp_get_wtime( );

status = clEnqueueNDRangeKernel( cmdQueue, kernel, 1, NULL, globalWorkSize, localWorkSize, 0, NULL, NULL );
PrintCLError( status, "clEnqueueNDRangeKernel failed: " );

Wait( cmdQueue );
double time1 = omp_get_wtime( );

status = clEnqueueReadBuffer( cmdQueue, dC, CL_TRUE, 0, numWorkGroups*sizeof(float), hC, 0, NULL, NULL );
PrintCLError( status, "clEnqueueReadBufferI failed: " );
Wait( cmdQueue );

float sum = 0.;
for( int i = 0; i < numWorkgroups; i++ )
{
    sum += hC[i];
}
Reduction Performance
Work-Group Size = 32

Array Size (MegaNumbers) vs. GigaNumbers Multiplied and Reduced Per Second