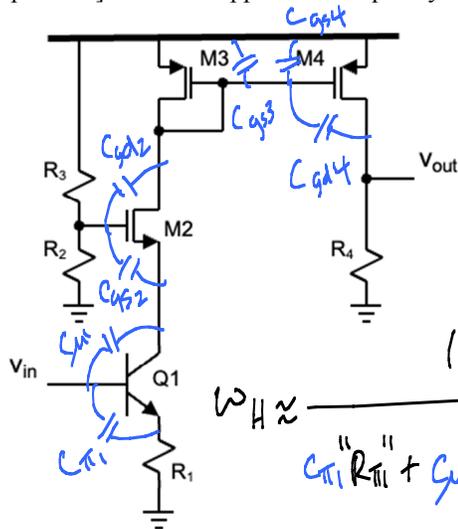


1. [10 pts total] Find the "upper 3dB frequency"  $\omega_H$  considering intrinsic capacitances.



$$\omega_H \approx \frac{1}{C_{\pi 1} R_{\pi 1} + C_{\mu 1} R_{\mu 1} + C_{gs2} R_{gs2} + C_{gd2} R_{gd2} + (C_{gs3} + C_{gs4}) R_{gs3} + C_{gd4} R_{gd4}}$$

$$R_{\pi 1} = R_1 \parallel \left( \frac{R_{\pi 1}}{1 + \beta_1} \right)$$

$$R_{\mu 1} = \frac{1}{g_{m2}}$$

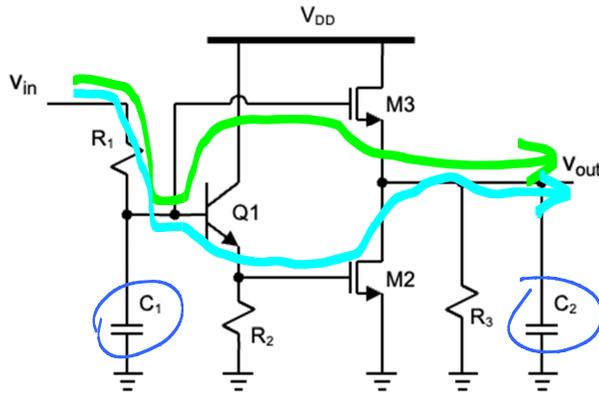
$$R_{gs2} = \frac{(R_2 \parallel R_3) + \infty}{1 + g_{m2} \infty} = \frac{1}{g_{m2}}$$

$$R_{gd2} = (R_2 \parallel R_3) (1 - 0) + \frac{1}{g_{m3}} = (R_2 \parallel R_3) + \frac{1}{g_{m3}}$$

$$R_{gs3} = \frac{1}{g_{m3}}$$

$$R_{gd4} = \frac{1}{g_{m3}} (1 + g_{m4} R_4) + R_4$$

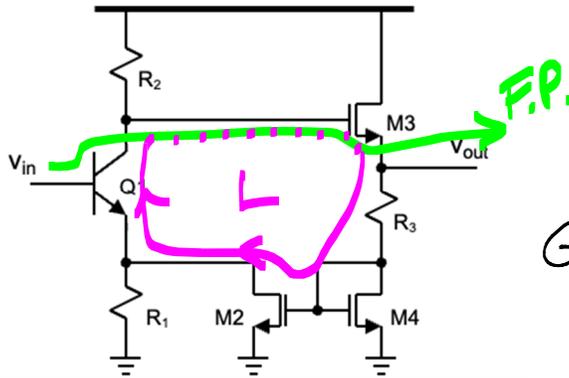
2. [10 pts total] Find the input to output (small-signal gain) transfer function  $H(s)$ . Ignore intrinsic capacitances.



$$H(s) = \frac{V_{\pi_1} + R_2(1 + \beta_1)}{R_1 + V_{\pi_1} + R_2(1 + \beta_1)} \left( \frac{R_3}{\frac{1}{g_{m3}} + R_3} - \frac{R_2(1 + \beta_1)}{V_{\pi_1} + R_2(1 + \beta_1)} \cdot g_{m2} \left[ \frac{1}{g_{m3}} \parallel R_3 \right] \right) \frac{1}{(1 + sC_1R_1)(1 + sC_2R_2)}$$

$R_1'' = R_1 \parallel (R_{\pi_1} + R_2[1 + \beta_1])$   
 $R_2'' = R_3 \parallel \frac{1}{g_{m3}}$

3. [10 pts total] Find the input to output small-signal gain.



$$\text{Gain} = \frac{F.P.}{1 - L}$$

$$F.P. = - \frac{r_{\pi 1}}{r_{\pi 1} + R_1(1 + \beta_1)} \cdot g_{m1} R_2 \cdot \frac{R_3 + \frac{1}{g_{m4}}}{\frac{1}{g_{m3}} + R_3 + \frac{1}{g_{m4}}}$$

$$L = - g_{m2} \left( R_1 \parallel \left( \frac{r_{\pi 1}}{1 + \beta_1} \right) \right) g_{m1} R_2 \cdot \frac{\frac{1}{g_{m4}}}{\frac{1}{g_{m3}} + R_3 + \frac{1}{g_{m4}}}$$