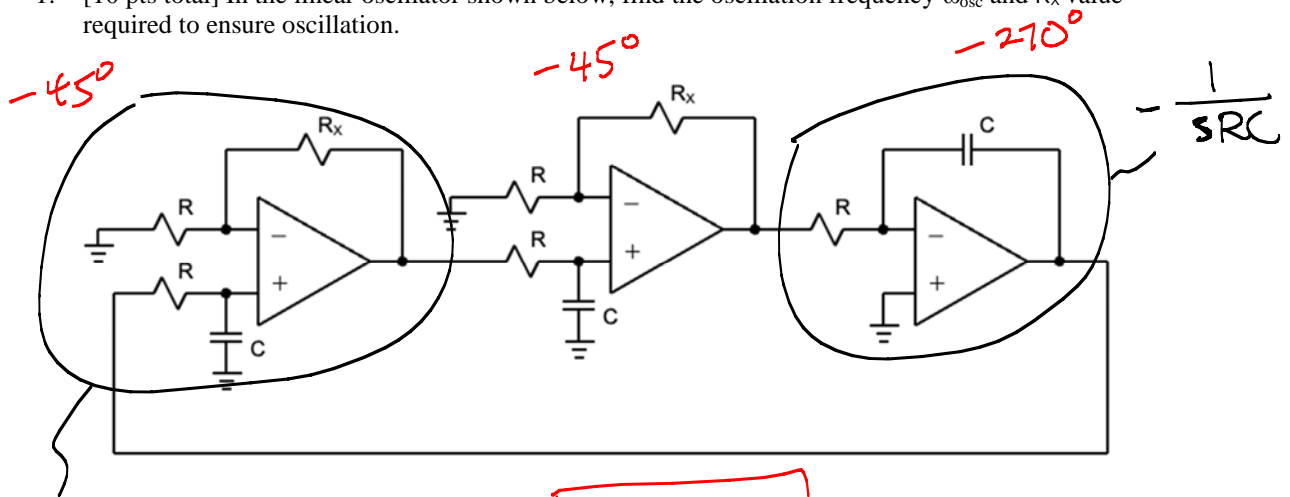


1. [10 pts total] In the linear oscillator shown below, find the oscillation frequency ω_{osc} and R_x value required to ensure oscillation.

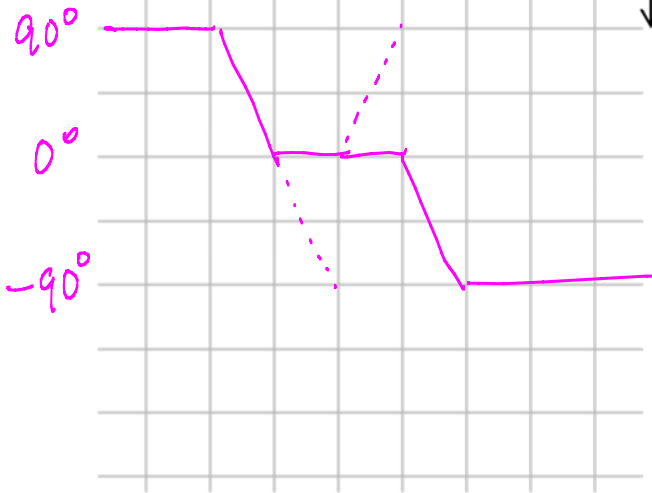
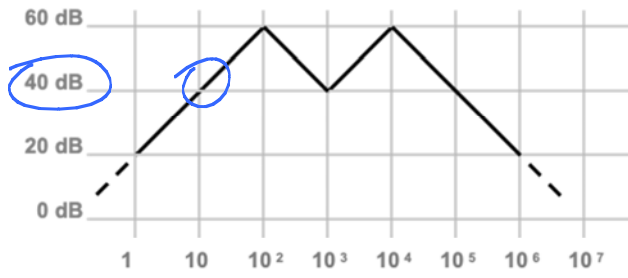


$$\frac{1}{1+sRC} \left(1 + \frac{R_x}{R}\right) \rightarrow \boxed{\omega_{osc} = \frac{1}{RC}}$$

$$|\text{loopgain}@ \omega_{osc}| = \left[\frac{1}{\sqrt{2}} \left(1 + \frac{R_x}{R}\right) \right]^2 \cdot 1 \geq 1$$

$$\rightarrow 1 + \frac{R_x}{R} \geq \sqrt{2} \rightarrow \boxed{R_x \geq R(\sqrt{2}-1)}$$

2. [10 pts total] Given the magnitude Bode plot shown below, find the corresponding transfer function and the phase plot that goes with it.



$$H(s) = K \frac{s \cdot (s+1000)^2}{(s+100)^2 (s+10000)^2}$$

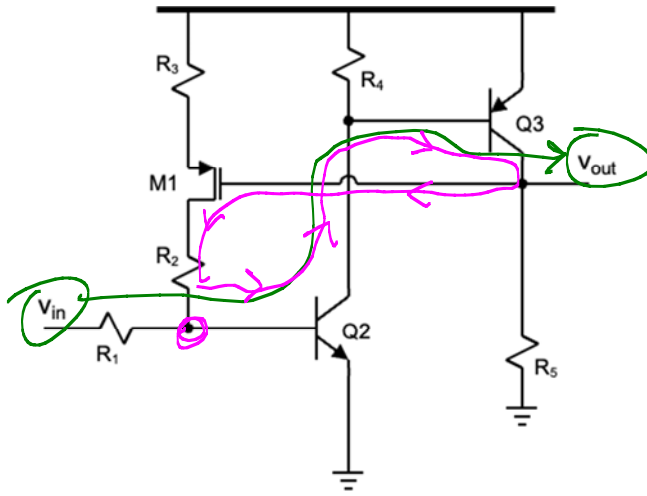
$$|H(s=j\omega)| = \left| K \frac{j\omega \cdot (s+1000)^2}{(s+100)^2 (s+10000)^2} \right|$$

$$= K \frac{10 \cdot (1000)^2}{(100)^2 (10000)^2} = 100$$

↑
40dB

$$\rightarrow \boxed{K = 10^7}$$

3. [10 pts total] Find the input to output small-signal gain.

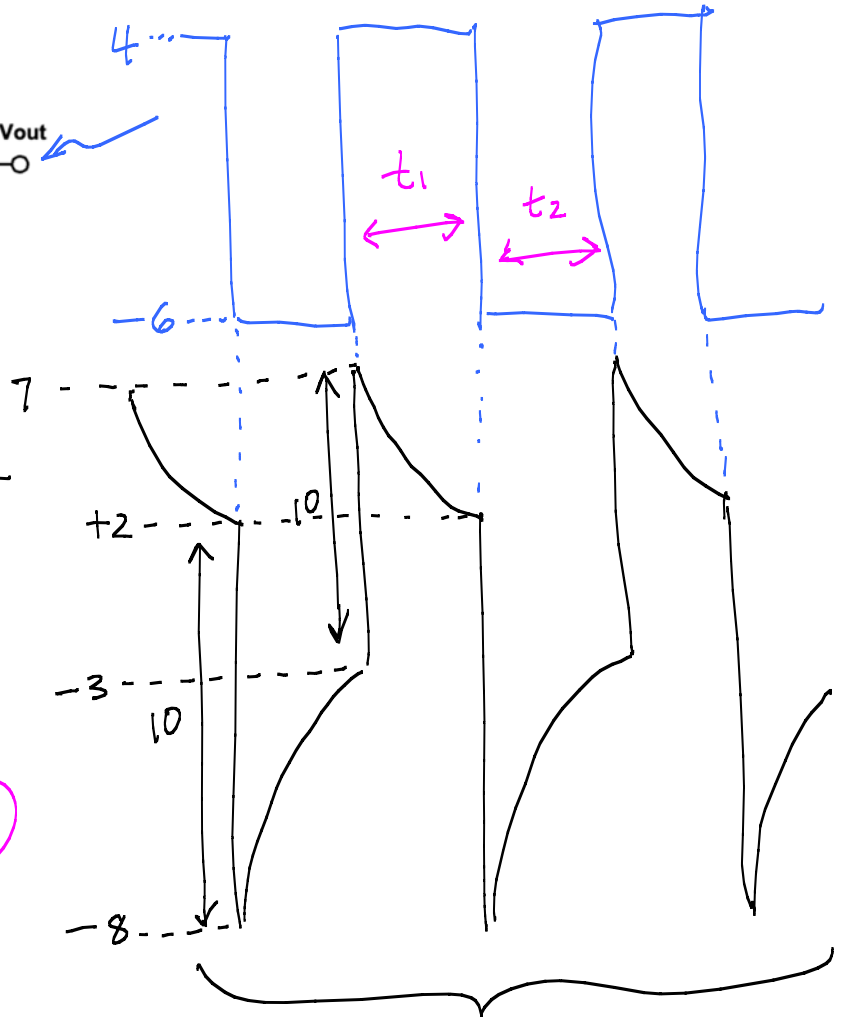
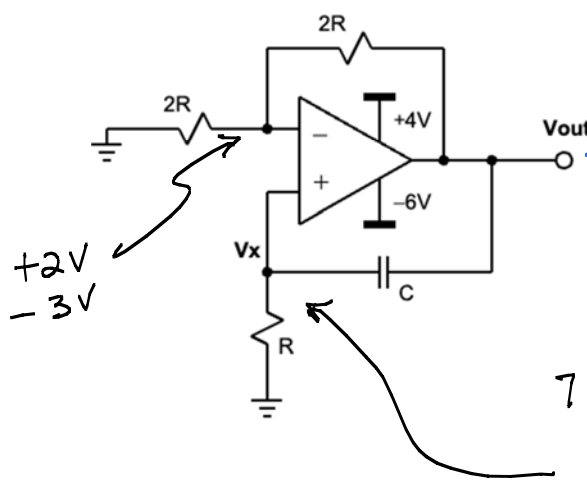


$$G_{in} = \frac{F.P.}{1 - Loop}$$

$$F.P. = \frac{r_{\pi 2}}{R_1 + r_{\pi 2}} \cdot g_{m2} \cdot (R_4 \parallel r_{\pi 3}) \cdot g_{m3} \cdot R_5$$

$$Loop = - g_{m2} \cdot (R_4 \parallel r_{\pi 3}) \cdot g_{m3} \cdot R_5 \cdot \frac{g_{m1}}{1 + g_{m1} R_3} \cdot (R_1 \parallel r_{\pi 2})$$

4. [10 pts total] In the nonlinear oscillator shown below, sketch the waveforms at node V_x and V_{out} . Note all critical voltage levels especially in the V_x waveform. Find the resulting period (T_{osc}) of oscillation.



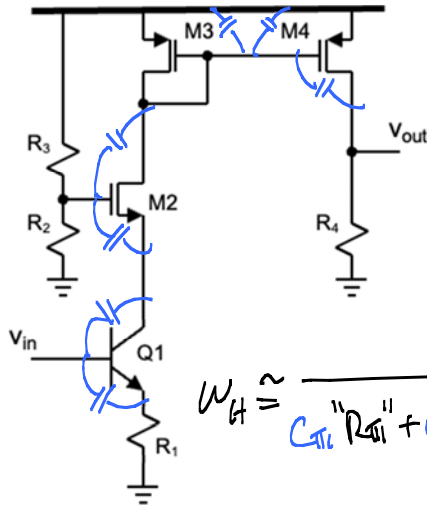
$$T_{osc} = t_1 + t_2$$

$$\frac{2}{7} = e^{-\frac{t_1}{RC}} \rightarrow t_1 = RC \cdot \ln\left(\frac{7}{2}\right)$$

$$\frac{3}{8} = e^{-\frac{t_2}{RC}} \rightarrow t_2 = RC \cdot \ln\left(\frac{8}{3}\right)$$

Not drawn to scale

5. [10 pts total] Find the input to output small-signal gain expression, then find the "upper 3dB frequency" ω_H (considering the intrinsic capacitances).



$$\text{gain} = \frac{v_{\pi 1}}{v_{\pi 1} + R_1 (1 + \beta_1)} \cdot g_{m1} \cdot \frac{g_{m4}}{g_{m3}} R_4$$

$$\omega_H \approx \frac{1}{C_{\pi 1} R_{\pi 1} + C_{\mu 1} R_{\mu 1} + C_{gs2} R_{gs2} + C_{gd2} R_{gd2} + (C_{gs3} + C_{gs4}) R_{gs3} + C_{gd4} R_{gd4}}$$

$$R_{\pi 1} = R_1 \parallel \frac{r_{\pi 1}}{1 + \beta_1} \quad R_{\mu 1} = \frac{1}{g_{m2}} \quad R_{gs2} = \frac{(R_2 \parallel R_3) + \infty}{1 + g_{m2} \cdot \infty} = \frac{1}{g_{m2}}$$

$$R_{gd2} = (R_2 \parallel R_3) (1 - 0) + \frac{1}{g_{m3}} = (R_2 \parallel R_3) + \frac{1}{g_{m3}}$$

$$R_{gs3} = \frac{1}{g_{m3}} \quad R_{gd4} = \frac{1}{g_{m3}} (1 + g_{m4} R_4) + R_4$$