

Lecture 10

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We will consider some limits of the indefinite form $\frac{0}{0}$. This is a tricky situation because you can't plug the number in (the function is not continuous). However, there are tricks to help find such limits.

Example 1:

$$\lim_{x \rightarrow 1} \frac{1-x}{2-3x+x^2}$$

We will try to factor the denominator.

Example 2:

$$\lim_{x \rightarrow 9} \frac{9-x}{3-\sqrt{x}}$$

We will multiply the numerator and the denominator by the conjugate of the denominator, which is $3 + \sqrt{x}$.

Example 3:

$$\lim_{t \rightarrow 0} \frac{\sqrt{1+t} - \sqrt{1-t}}{t}$$

We will multiply the numerator and the denominator by the conjugate of the numerator, which is $\sqrt{1+t} + \sqrt{1-t}$.

Squeeze theorem: If $f(x) \leq g(x) \leq h(x)$ for all x near a and $\lim_{x \rightarrow a} f(x) = \lim_{x \rightarrow a} h(x) = L$ then

$$\lim_{x \rightarrow a} g(x) = L.$$

Squeeze theorem is a very neat tool. It helps transform a complicated limit problem into a simpler limit problem.

Example 4:

$$\lim_{x \rightarrow 0} x \sin\left(\frac{x^2+1}{x}\right)$$