

$$t = 3^x$$

$$3^x + 2(3^{-x}) = 3 \rightarrow t + 2(1/t) = 3 \rightarrow (t + \frac{2}{t} = 3) \cdot t$$

$$t^2 + 2 = 3t \rightarrow$$

$$t^2 - 3t + 2 = 0$$

$$(t-1)(t-2) \quad t=1$$

$$t=2$$

$$t=1 \rightarrow 3^x=1 \quad \log_3(1) = 0$$

$$t=2 \rightarrow 3^x=2 \quad \log_3(2) = 0.631$$

solving equations cont

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ex) solve $e^{2x} - 3e^x - 10 = 0$

$$t = e^x$$

$$t^2 - 3t - 10 = 0$$

$$(t-5)(t+2)$$

$$t=5 \rightarrow e^x=5$$

$$\ln(5) = 1.609$$

$$t^2 + 2t - 5t - 10$$

$$t=-2 \rightarrow e^x=-2$$

$$\ln(-2) = \text{N/A}$$

ex) $\left(\frac{2}{3+2(5^{0.1x})} = \frac{1}{2} \right) \cdot 3+2(5^{0.1x})$

$$\frac{1}{2} = 5^{0.1x} \quad (a^b = c \Leftrightarrow b = \log_a(c))$$

$$\left(2 = \frac{1}{2} (3+2(5^{0.1x})) \right) \cdot 2 \quad 0.1x = \log_5(1/2) = \frac{\ln(1/2)}{\ln(5)} = -0.4307$$

$$\frac{4}{-3} = \frac{3+2(5^{0.1x})}{-3}$$

$$x = \frac{-0.4307}{0.1} = \boxed{-4.307}$$

$$\frac{1}{2} = \frac{2(5^{0.1x})}{2}$$

Solving inequalities w/ expon func

- Keep in mind:

• If $a > 1$: $a^b > c \iff b > \log_a(c)$ (same sign)

• If $0 < a < 1$: $a^b > c \iff b < \log_a(c)$ (switch sign)

ex) $2^x > 3 \rightarrow x > \log_2(3) \rightarrow x > \frac{\ln(3)}{\ln(2)} = 1.585$
 Solution: $x \in (\log_2(3), \infty)$ or $x \in (1.585, \infty)$

ex) $4\left(\frac{2}{3}\right)^x - 1 > 2 \rightarrow 4\left(\frac{2}{3}\right)^x > 3 \rightarrow \left(\frac{2}{3}\right)^x > \frac{3}{4}$
+1 +1 $\times \frac{1}{4}$ \hookrightarrow less than 1

$x < \log_{2/3}\left(\frac{3}{4}\right) \rightarrow x < \frac{\ln(3/4)}{\ln(2/3)} = 0.7095$
 Solution: $x \in (-\infty, 0.7095)$

ex) $2 - 3(5^{-x}) \leq 1$
-2 -2 $x \leq -\log_5(1/3)$

$(-3(5^{-x}) \leq -1) \cdot \frac{1}{-3}$
 $5^{-x} \geq 1/3$
 $(-x \geq \log_5(1/3)) \cdot -1$
 Solution: $x \in (-\infty, -\log_5(1/3))$

ex) $e^{2x} - 3e^x + 2 < 0$ $t = e^x$
 $t^2 - 3t + 2 < 0$ $\rightarrow \ln 1 < \ln e^x < \ln 2$
 $(t-2)(t-1) < 0$ $0 < x < \ln 2$
 $1 < t < 2 \rightarrow 1 < e^x < 2$

| | | |
|------------|---|---|
| t | 1 | 2 |
| t-1 | - | + |
| t-2 | - | + |
| (t-1)(t-2) | + | - |

Domain:
 Solution: $x \in (0, \ln 2)$

has to be
 < 0 , so -