

Worksheet – Sections 7.1

Population: the complete set of objects or people under study

Sample: a collection of objects or people drawn from the population

Population parameter: a variable of interest about the population

Sample statistic: a variable measured from the sample used to estimate a population parameter

Simple random sampling: a method of selecting a sample of size n such that every group of size n from the population has an equal chance of being selected.

<i>Sample</i>		<i>Parameter</i>	
Sample mean	\bar{x}	Population mean	μ
Sample standard deviation	s	Population standard deviation	σ
Sample variance	s^2	Population variance	σ^2
Sample proportion	\hat{p}	Population proportion	p

1) A university has 8,500 undergraduate students. The registrar wants to study enrollment in Calculus I. A random sample of 200 students is selected, and 74 of them are enrolled in Calculus I this semester. University records show that 32% of all undergraduate students are enrolled in Calculus I.

- (a) What is the population?
- (b) What is the sample?
- (c) What is the sample size?
- (d) Compute the sample proportion of students enrolled in Calculus I.
- (e) Identify the population proportion.
- (g) Is 74 a statistic, a parameter, or neither?

2) A library contains 12,000 books. The average number of pages per book is 318, with a standard deviation of 52 pages. A librarian randomly selects 200 books and finds an average of 324 pages with a standard deviation of 49 pages.

- (a) What is the population?
- (b) What is the sample?
- (c) Determine the meaning and symbol (if it appears in the above table) of each of the given numbers.

3) A researcher wants a random sample of 20 employees from a company with 100 employees. He/she sends an email asking for volunteers and selects the first 20 people who respond. Explain why this is not a simple random sample.

4) A biologist wants a random sample of 5 trees from a park containing 25 trees. The trees are numbered 1–25. The biologist places the numbers in a box and draws one number at a time. After each draw, the number is returned to the box before the next draw. Is it a good sampling technique?

5) You sample a population of 4 individuals A, B, C, D to see if they have a certain property. Suppose that A and B has this property, while C and D don't.

(a) List all possible samples of size 2 (such as AB, AC, ...)

(b) For each of those samples, find the sample proportion \hat{p} .

(c) Make a table of probability distribution of \hat{p} .

(d) From the table above, use the following formula to find the mean and standard deviation of \hat{p} .

$$\text{Mean} = \sum vP(\hat{p} = v) =$$

$$\text{Std. dev.} = \sqrt{\sum (v - \text{mean})^2 P(\hat{p} = v) =}$$

6) Repeat Problem 5 but with sample of size 3.