## First experiments with Mathematica

## 1 Get access

Mathematica is a mathematical software developed by Wolfram Research Company. Please see Page 4 of the syllabus for instructions on how to get access to Mathematica.

## 2 First experiments

(1) Type $35 / 6$, then Shift+Enter.
(2) Type N[35/6] (notice the square brackets), then Shift+Enter.
(3) Type Sqrt [2] (notice the capitalized S), then Shift+Enter.
(4) Type N [\%], then Shift+Enter.
(5) Type Sin [Pi] (notice the capitalized S and P), then Shift Enter.
(6) Type 34^100; (with the semicolon), then Shift Enter.
(7) Type 34^100 (without semicolon), then Shift Enter.

You may have noticed that the function $N$ is to evaluate a numerical value of an expression. Each function's name is capitalized and used with square brackets (not with parentheses as we usually write). The semicolon is to hold the output. One uses it when output is too long or not of interest. Next, try the following:
(8) Exp[1], then Shift+Enter.
(9) Log [2], then Shift+Enter.
(10) $f[x]:=\operatorname{Sin}[x]+\operatorname{Cos}[x]$ (notice the dash after $x$ ), then Shift+Enter.
(11) $f[P i]+f[P i / 4]$, then Shift+Enter.
(12) Clear [f], then Shift+Enter.
(13) $f[P i]+f[P i / 4]$, then Shift + Enter.

The natural logarithm function is named Log in Mathematica (not ln). Exp is the exponential function. Command (10) is to define a function. The dash is required in order to tell Mathematica that we are defining the function $f$. The function Clear is to remove a defined variable from the memory.

## 3 Plot the graph of a function

First, let us plot functions of one variable, for example the sine function $\sin (\mathrm{x})$. Try the following commands:
(14) $\operatorname{Plot}[\operatorname{Sin}[x],\{x, 0,2 * \operatorname{Pi}\}]$, then Shift+Enter.
(15) For decoration, try


Figure 1

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Plot[Sin[x], {x,0,2*Pi}, Filling->Axis]
```

Then Shift+Enter. Note that the arrow is typed as $->$.
(16) You can also give the function a name before plotting it. For example,

$$
\begin{aligned}
& \mathrm{f}[\mathrm{x}-]:=\operatorname{Sin}[\mathrm{x}] \\
& \text { Plot }[\mathrm{f}[\mathrm{x}],\{\mathrm{x}, 0,2 * \mathrm{Pi}\}, \text { Filling } \rightarrow \text { Axis }]
\end{aligned}
$$

Then Shift+Enter. Note that the dash following $x$ is no longer used after the definition of $f$. Next, let us plot functions of two variables, for example

$$
f(x, y)=x^{2} \sin (y)
$$

We will use the command Plot3D instead of Plot. Try the following commands:
(17) Plot3D[x^2*Sin[y], $\{x,-2,2\},\{y,-P i, P i\}]$, then Shift+Enter.


Figure 2: You can rotate the above surface with your mouse
(18) You can also give the function a name before plotting it. Try the following:

$$
\begin{gathered}
f\left[x_{-}, y_{-}\right]:=x^{\wedge} 2 * \operatorname{Sin}[y] \\
\operatorname{Plot}[f[y, \quad\{x,-2,2\}, \quad\{y,-P i, P i\}]
\end{gathered}
$$

There are many other interesting manipulation you can do on 3D graphs. Take a look at this Wolfram's webpage.

