

Worksheet  
6/7/2019

1. Consider function  $f(z) = \frac{\text{Log}(z+5)}{\sin z}$ .

(a) Determine all singular point(s) of  $f$  enclosed in the circle  $C_4(0)$ . Are they isolated singularities?

(b) Which kind of isolated singularity are they (removable, pole, essential)? If they are poles, determine their orders.

(c) Compute the residue of  $f$  at each of these singularities.

(d) Evaluate the integral  $\int_{\gamma} f(z)dz$  where  $\gamma$  is the circle  $C_4(0)$  oriented counterclockwise.

2. Compute  $\int_{\gamma} \frac{z+1}{(z-\frac{\pi}{2})^2 \sin z} dz$  where  $\gamma$  is the circle  $C_2(0)$  oriented counterclockwise.

3. Compute  $\int_{\gamma} z^2 \sin\left(\frac{1}{z}\right) dz$  where  $\gamma$  is the boundary of square with vertices at  $\pm 1 \pm i$  negatively oriented.