

Worksheet  
2/21/2020

Name: \_\_\_\_\_

1. Let  $V$  be an inner product vector space. Let  $u$  and  $v$  be perpendicular vectors in  $V$ . Prove the Pythagorean identity:

$$\|u + v\|^2 = \|u\|^2 + \|v\|^2$$

see Lecture 19.

2. On  $\mathbb{R}^2$ , define an operator  $\|\cdot\|$  as  $\|x\| = |x_1| + 2|x_2|$  where  $x = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$ .  
Show that  $\|\cdot\|$  is a norm on  $\mathbb{R}^2$ .

*See Lecture 19.*