Name: _____

Consider a linear map $f: M_{2\times 2}(\mathbb{R}) \to M_{2\times 2}(\mathbb{R})$ given by

$$f\left(\left[\begin{array}{cc}a&b\\c&d\end{array}\right]\right)=\left[\begin{array}{cc}d&-b\\-c&a\end{array}\right].$$

Determine the eigenvalues and the corresponding eigenspaces (by finding basis) of f.

See Lecture 13 and 14 for a coordinate-based method. See Lecture 15 for a coordinate-free method.