Name: $\qquad$

1. Let $V=\{u:[0,1] \rightarrow \mathbb{R}, u$ is continuous $\}$ be an inner product space with the inner product

$$
(u, v)=\int_{0}^{1} u(x) v(x) d x
$$

Find an orthonormal basis of $P_{2}(\mathbb{R})$.

$$
\text { see Lecture } 24
$$

2. Find the orthogonal projection of $u(x)=\cos x$ on the space $P_{2}(\mathbb{R})$.

$$
\begin{aligned}
& \text { See Lecture } 24 \text { (and the later } \\
& \text { part of Lecture 23). }
\end{aligned}
$$

