Name: _____

 $P_2(\mathbb{R})$ is an inner product space with

$$(u,v) = \int_0^1 u(x)v(x)dx.$$

Consider a linear map $G: P_2(\mathbb{R}) \to P_2(\mathbb{R})$ given by G(u)(x) = u(x+1). Find the adjoint operator G^* . Is G a unitary operator?

See Lecture 26.