Name: $\qquad$
$P_{2}(\mathbb{R})$ is an inner product space with

$$
(u, v)=\int_{0}^{1} u(x) v(x) d x
$$

Consider a linear map $G: P_{2}(\mathbb{R}) \rightarrow P_{2}(\mathbb{R})$ given by $G(u)(x)=u(x+1)$. Find the adjoint operator $G^{*}$. Is $G$ a unitary operator?

See Lecture 26.

