

- (1) (3 points) Let  $\vec{a} = (-1, 0, 2)$  and  $\vec{b} = (-1, 2, 0)$ . Find  $|2\vec{a} - \vec{b}|$ .

1 point for scalar multiplication and subtraction of vectors,

1 point if the length formula of a vector is correct,

1 point for the answer.

ANS: square root of 21

- (2) (7 points) Consider the system of linear equations,

$$x_1 + 3x_2 + 3x_3 = 0$$

$$2x_1 + 7x_2 + 5x_3 = 0$$

Reduce the given system to echelon form to find a single solution vector  $\vec{u}$  such that the solution space is the set of all scalar multiples of  $\vec{u}$ .

(1 point) for writing the matrix,

(1 point) for finding the echelon form,

(1 point) for deciding free variable which is  $x_3$  in this case,

(2 point) saying;  $x_3 = s$  and writing other variables in terms of  $s$ ;  $x_1 = -6s$ ,  $x_2 = s$

(1 point) writing the solution as;  $(-6s, s, s)$

(1 point) for plug in 1 or take  $s$  out or plug in any number for  $s$  and write it a a vector.

here if the student's mistake is only one of those steps, deduct the corresponding amount of points,

if there is no mistake even the step is missing, still full credit.