Please show all necessary work completely and clearly.
(1) (5 Points) Show that $y(x)=1, y(x)=e^{-x}$, and $y(x)=e^{2 x}$ are linearly independent functions.
(2) (5 Points) Find the general solution to the differential equation

$$
y^{\prime \prime \prime}-y^{\prime \prime}-2 y^{\prime}=0
$$

