

- (1) (5 Points) Set up an appropriate particular solution  $y_p$ , for the differential equation,

$$y^{(3)} - y'' - 12y' = x - 2xe^{-3x}$$

which have complementary function given by;

$$y_c = C_1 + C_2e^{-3x} + C_3e^{4x}$$

(Do not determine the values of coefficients).

- (1pt.) Any work
- (2 pt.) Initial guess is true;  $(A + Bx) + (C + Dx)e^{-3x}$
- (2pt.) Multiplying by  $x$  and saying  $y_p = x.(A + Bx) + x.(C + Dx)e^{-3x}$   
(if student forgets to multiply two of those terms by  $x$ , consider giving 1 partial credit for this case)

- (2) (5 Points) Solve the initial value problem;

$$y'' + 4y = 2x; \quad y(0) = 1, y'(0) = 2$$

whose particular solution is given by;

$$y_p = \frac{x}{2}.$$

- (2 pt.) Finding  $y_c = c_1\cos 2x + c_2\sin 2x$
- (1 pt.) Saying  $y_g = c_1\cos 2x + c_2\sin 2x + x/2$
- (2 pt.) Computing  $c_1 = 1$  and  $c_2 = 3/4$  (for each small algebra mistakes, if the rest of it true, you can deduct 1pt)