

MATH 8702
Additional Problems for Homework Assignment #3

Due 03/01

INSTRUCTOR: Anar Akhmedov

1. Prove that the complex plane slit along the union of rays $\bigcup_{k=1}^n \{A_k + iy : A_k \text{ is real and } y \leq 0\}$ is simply connected.
2. Prove that the function u defined by $u(x, y) = \operatorname{Re}\left(\frac{i+z}{i-z}\right)$ and $u(0, 1) = 0$ is harmonic in the unit disc and vanishes on its boundary.