## MATH 251, MIDTERM, FALL 2022

INSTRUCTOR: TUAN PHAM

| Name |
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## Instructions:

- This is a closed-book exam, 50 minutes long.
- A single sided, handwritten, 3 " x 5 " note card is allowed. A scientific calculator is allowed. Graphing/programmable/transmittable calculators are not allowed.
- For Problems 1-7, fill in the bubbles on this front page. To each problem, only one answer is correct.
- For Problems 8, 9 and 10, make sure to show all necessary steps. Mysterious answers will receive little or no credit.

| 1. | (A) |
| :---: | :---: |
| 2. | (A) (B) (C) |
| 3. | (A) (B) (C) (D) |
| 4. | (A) (B) (C) (D) |
| 5. | (A) (B) (C) (D) |
| 6. | (A) (B) (C) |
| 7. | (A) (B) (C) (D) |


| Problem | Possible points | Earned points |
| :---: | :---: | :---: |
| $1-7$ | 14 |  |
| 8 | 5 |  |
| 9 | 5 |  |
| 10 | 5 |  |
| Total | 29 |  |

Problem 1. (2 points) Let $f(x)=x^{2}+1$ and $g(x)=\frac{1}{x}$. Which of the following is the composite function $f \circ g$ ? That is, function $f(g(x))$.
A. $\frac{1}{x^{2}+1}$
B. $\frac{2}{x^{2}}$
C. $\frac{1}{x^{2}}+1$
D. $\frac{1}{(x+1)^{2}}$

Problem 2. (2 points) Suppose a function $f$ is not defined at $x=a$. Which of the following statements is false?
A. $f$ is not continuous at $a$.
B. $f$ is not differentiable at $a$.
C. $\lim _{x \rightarrow a} f(x)$ does not exist.

Problem 3. (2 points) If the $\lim _{x \rightarrow a^{-}} f(x) \neq \lim _{x \rightarrow a^{+}} f(x)$ then $f$ is discontinuous at $a$. True or false?
A. True
B. False

Problem 4. (2 points) Choose the correct value of the limit

$$
\lim _{x \rightarrow-\infty} \frac{x}{\sqrt{x^{2}+1}}
$$

A. 1
B. -1
C. $\infty$
D. $-\infty$

Problem 5. (2 points) Choose the correct value of the limit

$$
\lim _{x \rightarrow \infty} \frac{x\left(2 x^{2}-3 x+5\right)}{\left(x^{2}+1\right)(x+1)}
$$

A. 1
B. 2
C. 0
D. $\infty$

Problem 6. (2 points) Let $f(x)=x+\frac{x}{x+1}$. Find $f^{\prime}(1)$.
A. $-1 / 4$
B. $1 / 4$
C. $3 / 4$
D. $5 / 4$

Problem 7. (2 points) The figure below contains the graphs of $f, f^{\prime}$, and $f^{\prime \prime}$. The graphs of these functions in that order are

A. $\mathrm{a}, \mathrm{b}, \mathrm{c}$
B. $\mathrm{a}, \mathrm{c}, \mathrm{b}$
C. $\mathrm{b}, \mathrm{a}, \mathrm{c}$
D. $\mathrm{b}, \mathrm{c}, \mathrm{a}$

Problem 8. (5 points) Evaluate the polynomial $x^{3}-3 x+1$ at $x=-2,-1,0,1,2$ and explain why it has three distinct roots.

Problem 9. (5 points) Use the limit laws you learned to find the limit

$$
\lim _{x \rightarrow-1} \frac{x^{2}-2 x-3}{x^{2}+4 x+3}
$$

Problem 10. (5 points) Find the point on the parabola $y=x^{2}+x$ at which the tangent line to the parabola is parallel to the line $y=3 x$. What is the equation for the tangent line at that point?

