



# faster malicious 2pc with online/offline dual execution


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אוניברסיטת בר-אילן

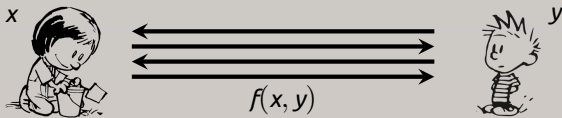
# two-party secure computation



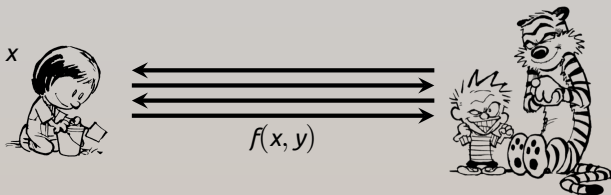
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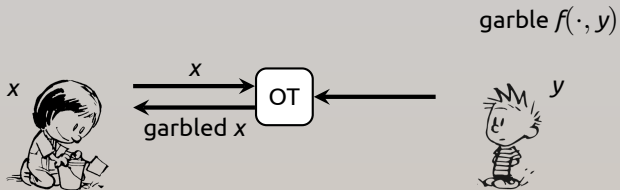
- ▶ Security against malicious adversaries

# yao's 2pc protocol

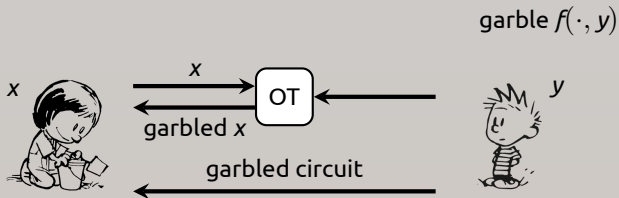
garble  $f(\cdot, y)$



# yao's 2pc protocol

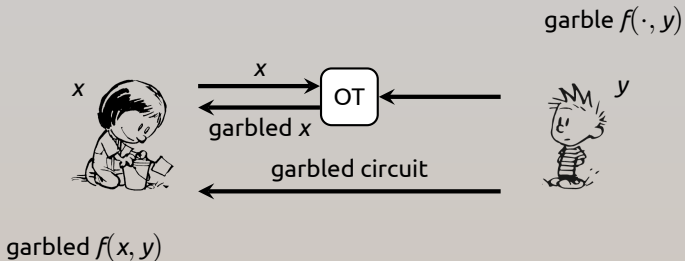


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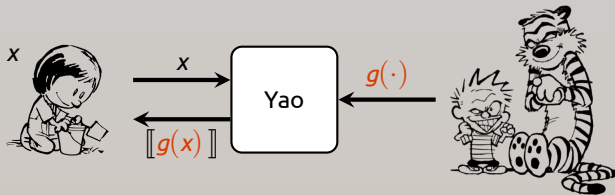
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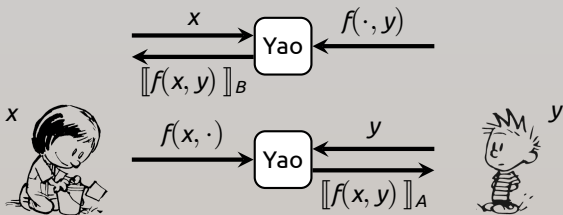


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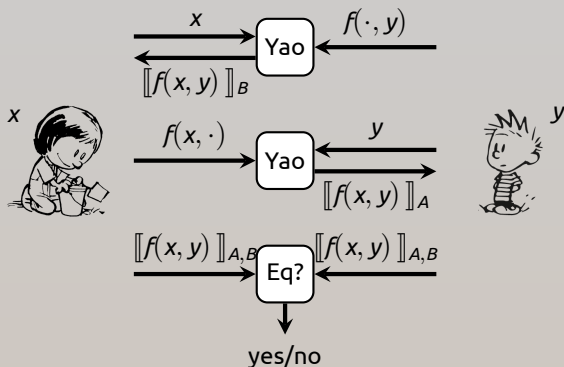


- ▶ Full security against malicious receiver
- ▶ Malicious sender can construct bad garbled circuit

# dual execution protocol [MohasselFranklin06]

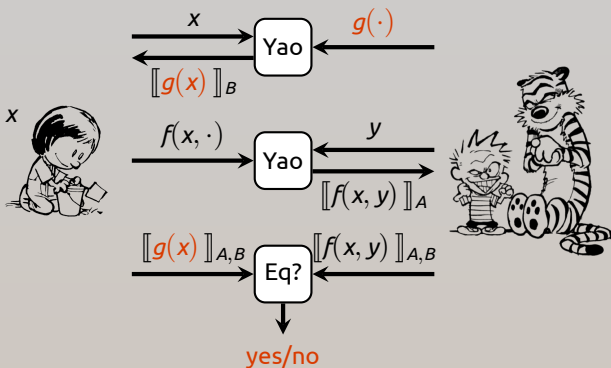


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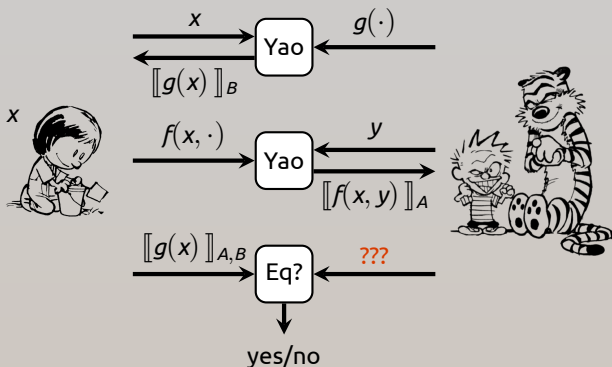
- ▶ Define a **common** garbled encoding:  $\llbracket z \rrbracket_{A,B} \stackrel{\text{def}}{=} \llbracket z \rrbracket_A \oplus \llbracket z \rrbracket_B$

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- ▶ Malicious Bob learns whether  $g(x) = f(x, y)$  (only 1 bit)

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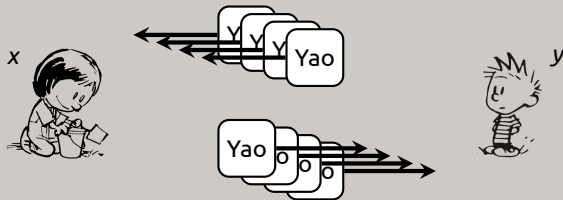


- ▶ Define a **common** garbled encoding:  $[[z]]_{A,B} \stackrel{\text{def}}{=} [[z]]_A \oplus [[z]]_B$
- ▶ Malicious Bob learns whether  $g(x) = f(x, y)$  (only 1 bit)
- ▶ Malicious Bob can't predict  $[[z]]_{A,B}$  for  $z \neq f(x, y)$ 
  - ⇒ can't make Alice accept incorrect output!

# reducing leakage [KolesnikovMohasselRivaR15]



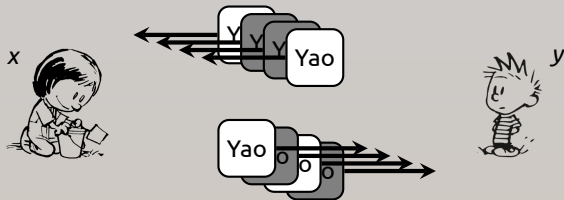
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Main idea:

- ▶ Run  $\kappa$  copies of Yao's protocol in each direction

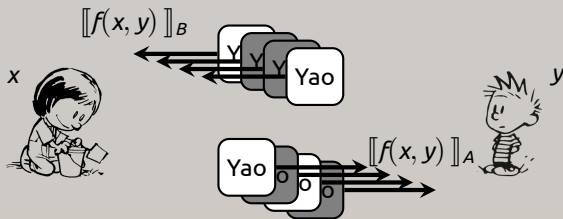
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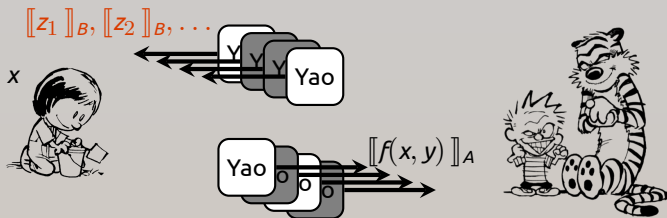
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Main idea:

- ▶ Run  $\kappa$  copies of Yao's protocol in each direction
- ▶ Cut and choose: check each garbled circuit with probability 1/2.
- ▶ Garbled circuits in same direction have same output encoding
- ▶ What to do when Alice gets disagreeing outputs?

# reconciliation technique

$[[Z^*]]_B$



$[[Z^*]]_A$



- ▶ Honest parties can compute common  $[[Z^*]]_{A,B} \stackrel{\text{def}}{=} [[Z^*]]_B \oplus [[Z^*]]_A$

# reconciliation technique

$$[[z_1]]_B, [[z_2]]_B, \dots$$



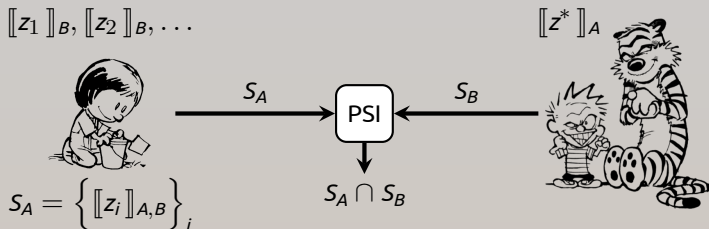
$$S_A = \left\{ \left[ [z_i] \right]_{A,B} \right\}_i$$

$$[[z^*]]_A$$



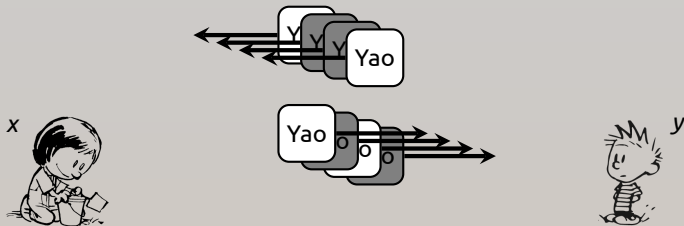
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- ▶ If disagreeing outputs, compute **set of candidates**

# reconciliation technique



- ▶ Honest parties can compute common  $[[z^*]]_{A,B} \stackrel{\text{def}}{=} [[z^*]]_B \oplus [[z^*]]_A$
- ▶ If disagreeing outputs, compute **set of candidates**
- ▶ Do **private set intersection** on the sets!
  - ⇒ PSI output identifies the “correct”  $z_i$

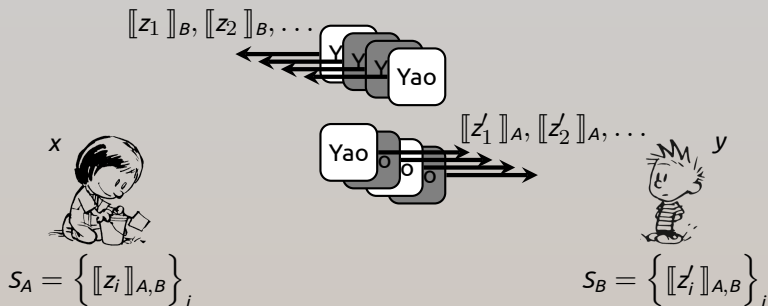
# protocol summary



- ▶  $\kappa$  instances of Yao in each direction, check random subset

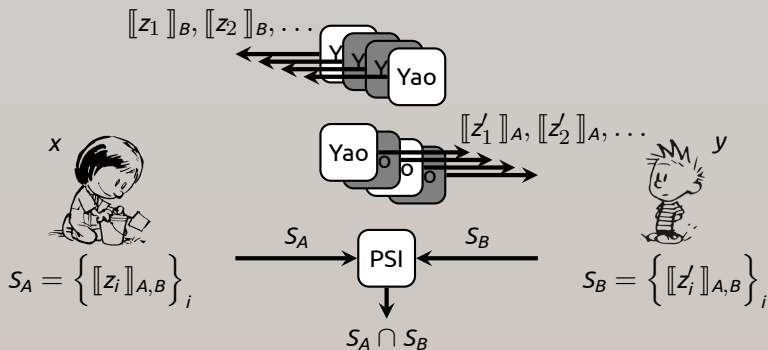


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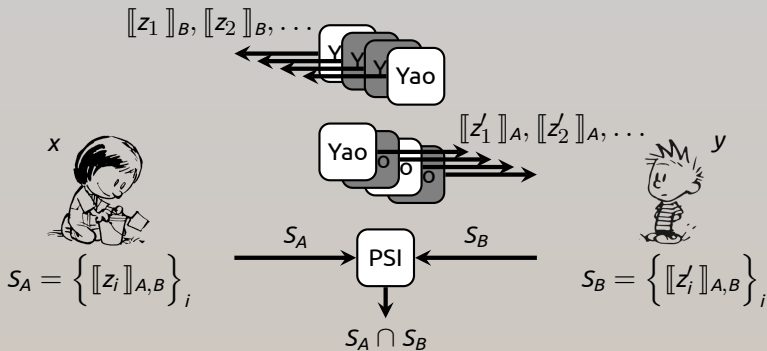
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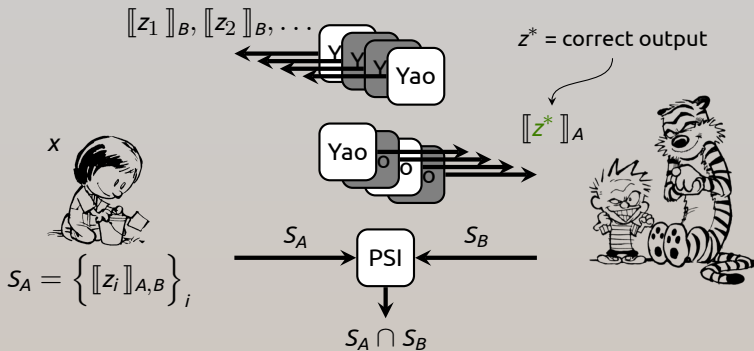


- ▶  $\kappa$  instances of Yao in each direction, check random subset
- ▶ Compute set of reconciliation values
- ▶ Private set intersection to identify correct output

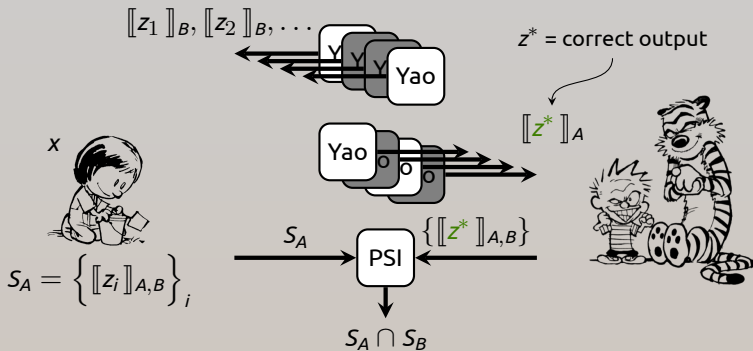
# protocol analysis



# protocol analysis: corrupt Bob

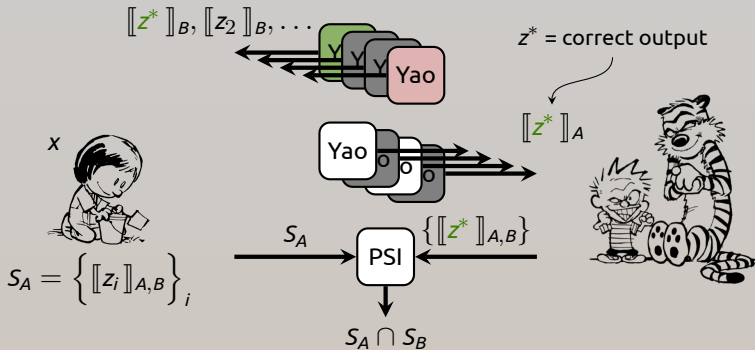


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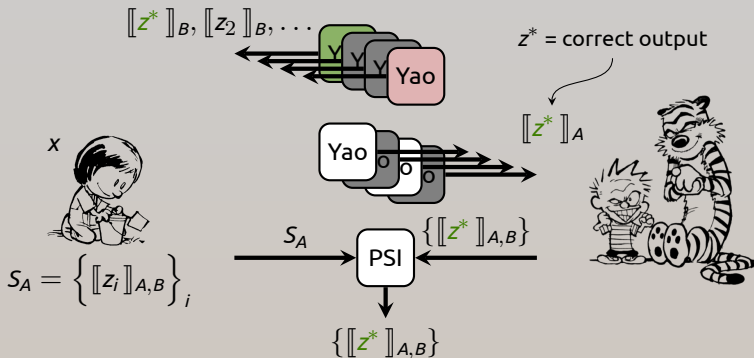
- ▶ Bob's only "useful" PSI input is  $[z^*]_{A,B}$

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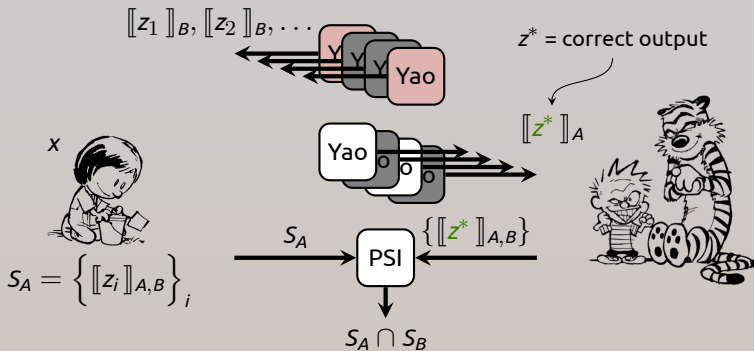
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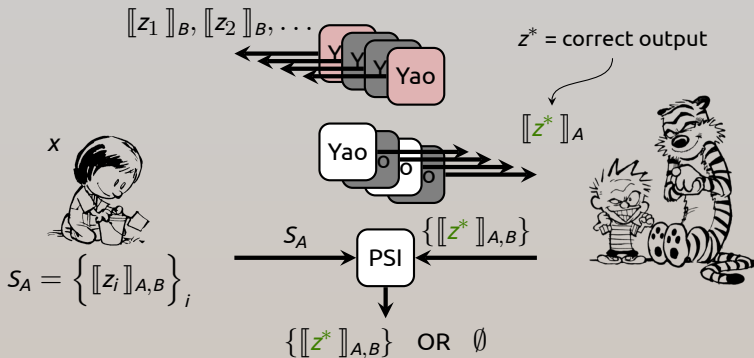
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# protocol analysis: corrupt Bob



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- ▶ One of Bob's garbled circuits **correct**  $\Rightarrow$  PSI output leaks nothing!
- ▶ None of Bob's garbled circuits correct  $\Rightarrow$  PSI output leaks just 1 bit

# “dual-ex+PSI” summary

$\kappa$  garbled circuits in each direction (can be done simultaneously)

Adversary cannot violate output correctness

Adversary learns a single bit with probability  $1/2^\kappa$ ; only when:

- ▶ All opened circuits are correct
- ▶ All evaluated circuits are incorrect

# rest of the talk

Online/offline, multi-execution setting

- ▶ Reducing # of garbled circuits

Adapting “dual-execution+PSI” protocol to online/offline setting:

[RindalR16]

- ▶ Ensuring input consistency
- ▶ Lightweight private set intersection

Implementation, performance

- ▶ Comparison to [LindellRiva15] and info-theoretic protocols

# online/offline setting

Want to do 2PC of same circuit  $N$  times?

[HuangKatzKolesnikovKumaresanMalozemoff14,LindellRiva14]

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generate a lot of garbled circuits

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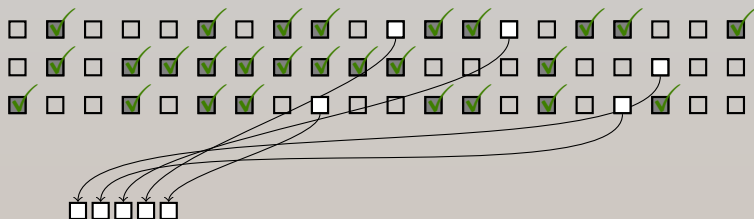


open and check some fraction of them

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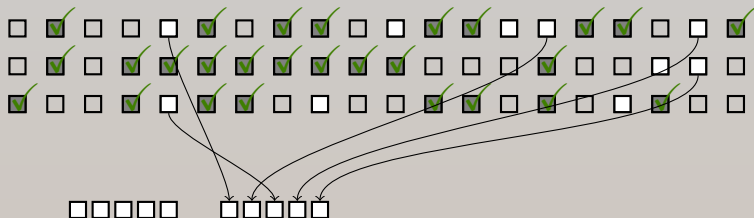


pick a random “bucket” of available circuits and evaluate them

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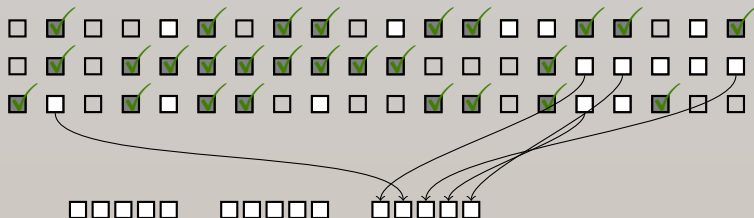
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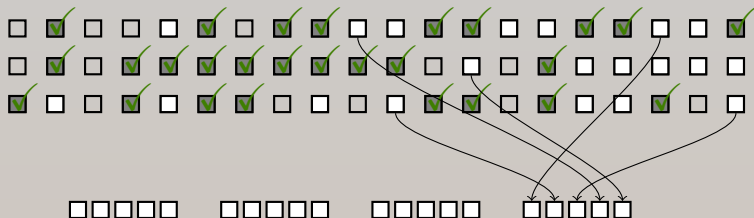


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- ▶ for security  $1/2^{\kappa}$ , need  $O(\kappa/\log N)$  circuits per execution
- ▶ example:  $N = 1024, \kappa = 40 \Rightarrow 4$  circuits per execution

# online/offline dual-ex [RindalR16]

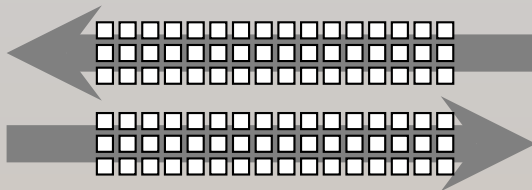


*offline phase*

*online phase*



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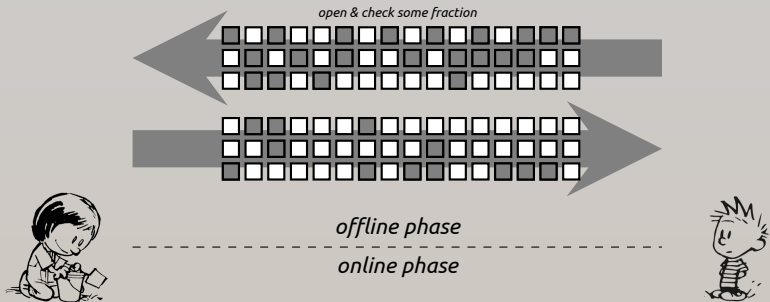


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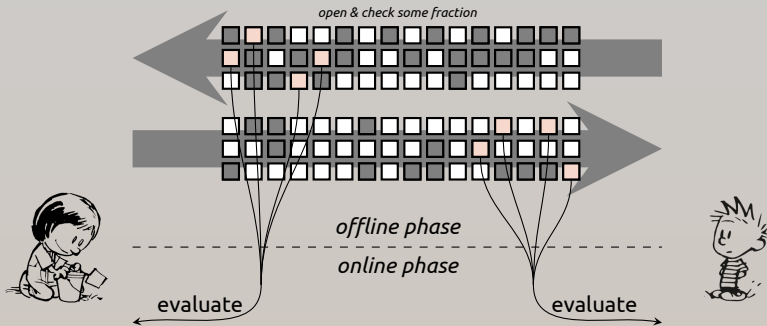
*online phase*



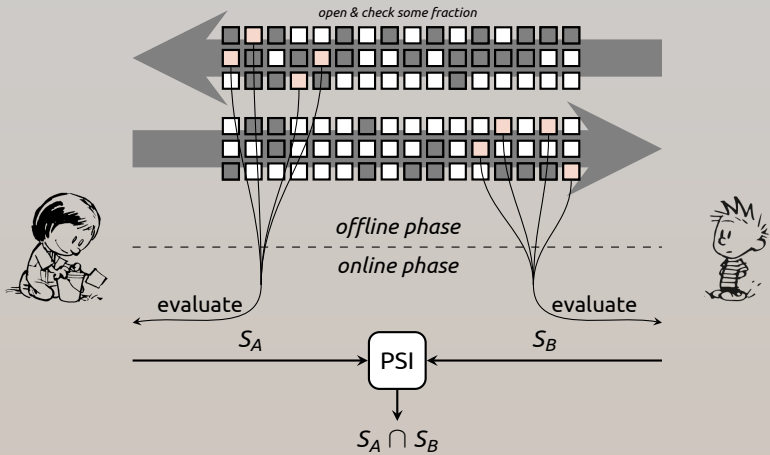
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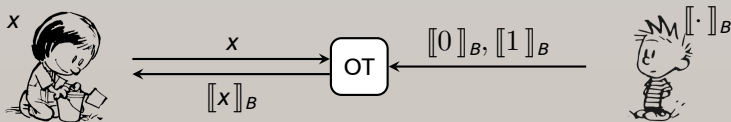
# challenge #1: input consistency

*How to ensure same inputs in Alice/Bob circuits?*

[KolesnikovMohasselRivaR15,shelatShen13] technique incompatible with offline circuit garbling

# pre-computing OTs [Beaver95]

*[for simplicity: 1 input bit from Alice]*



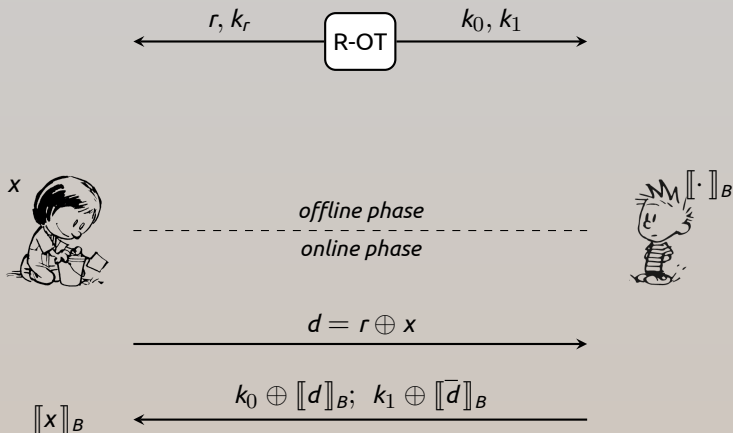
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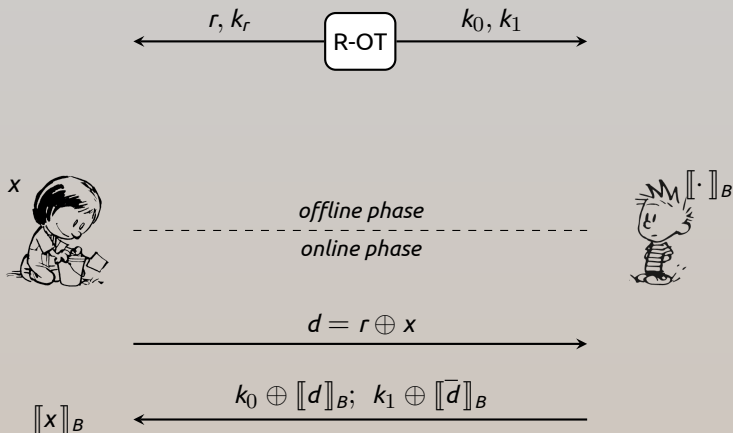
*offline phase*  
-----  
*online phase*



# pre-computing OTs [Beaver95]



# consistency b/w A & B circuits



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$[[\cdot]]_A, x$



*offline phase*

*online phase*



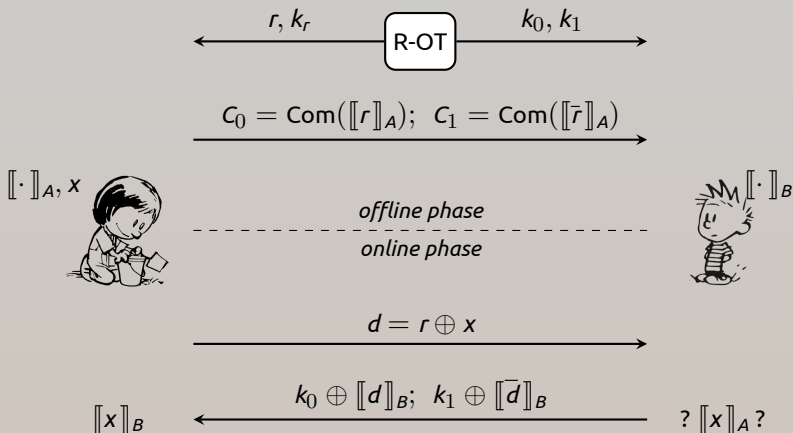
$$d = r \oplus x$$

$[[x]]_B$

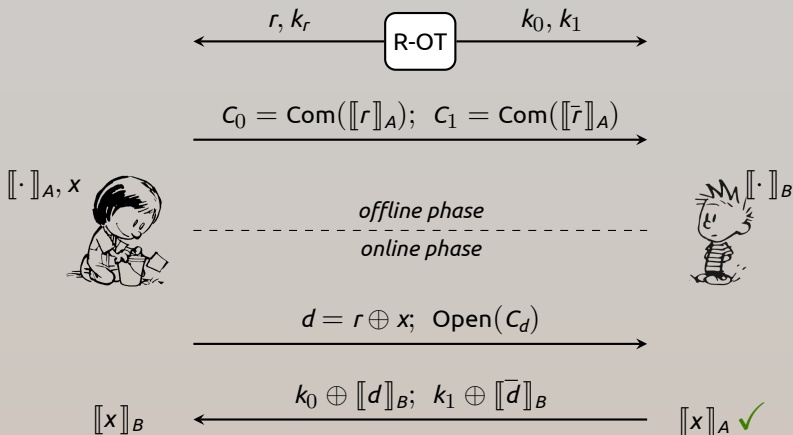
$$k_0 \oplus [[d]]_B; k_1 \oplus [[\bar{d}]]_B$$

?  $[[x]]_A$  ?

# consistency b/w A & B circuits

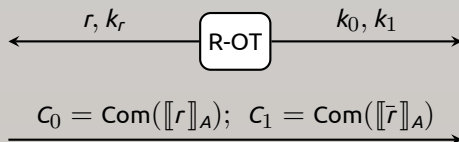


# consistency b/w A & B circuits





# consistency b/w A & B circuits



$\llbracket \cdot \rrbracket_A, X$



*offline phase*

*online phase*



Can check consistency of commitments in cut-and-choose:

- ▶ Alice can show  $k_r$  to prove what  $r$  she got from OT
- ⇒ at least one pair of A/B circuits with consistency

# input consistency

Within each bucket,

- ▶ Alice uses same input  $x$  on all Bob-circuits (easy)
- ▶ At least one Alice-circuit where Alice uses  $x$  (except prob  $1/2^k$ )

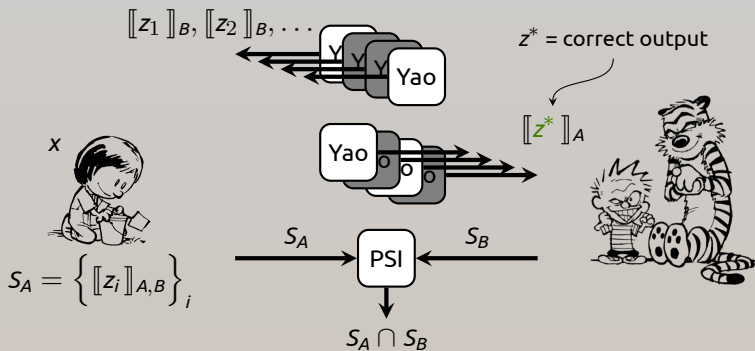
Suffices for security!

Zero online cost for input consistency!

# challenge #2: psi

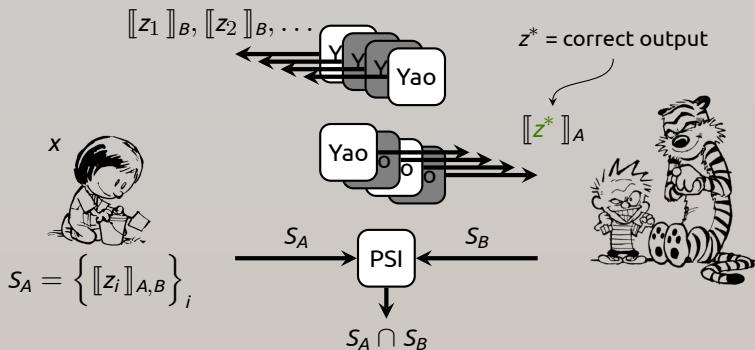
*How to efficiently instantiate PSI?*

# closer look at PSI



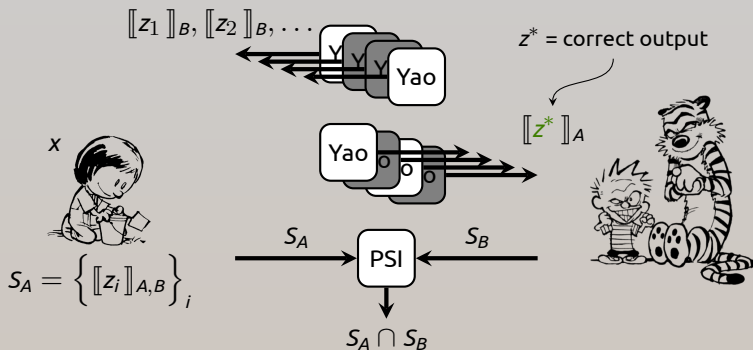
Bob's only "useful" PSI input is  $\llbracket z^* \rrbracket_{A,B}$

# closer look at PSI



- ▶ Simulator knows  $\llbracket z^* \rrbracket_{A,B,i}$ ; rest of  $S_A$  independent of Adv's view

# closer look at PSI



- ▶ Simulator knows  $\llbracket z^* \rrbracket_{A,B}$ ; rest of  $S_A$  independent of Adv's view
- ★ Simulator **does not need to extract** Adv's input  $S_B$ !  
... it suffices to check whether  $\llbracket z^* \rrbracket_{A,B} \in S_B$

# instantiating psi

[KolesnikovMohasselRivaR15]:

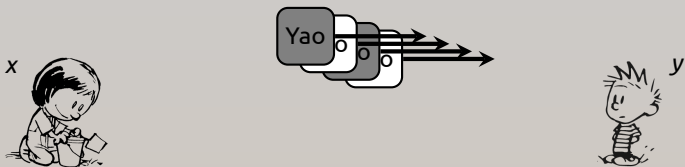
- ▶ Suggest using fully malicious PSI subprotocol

[RindalR16]:

- ▶ PSI protocol with “non-extracting security” suffices
- ▶ Implementation uses semi-honest PSI protocol of [PinkasSchneiderZohner14]
- ▶ Very cheap, based on pre-processed OTs (no public-key operations)

# comparison to [LindellRiva15]

[LindellRiva14/15]: online/offline, malicious security, based on “traditional cut and choose” [Lindell13]:



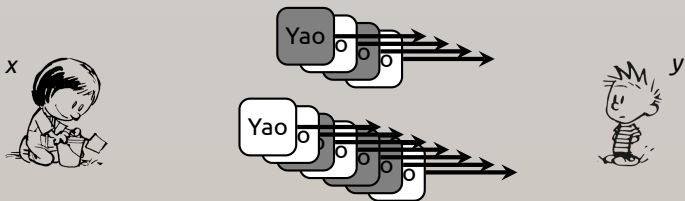
Two phases:

1.  $B$  circuits computing  $f(x, y)$



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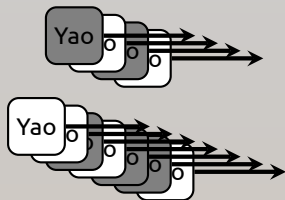
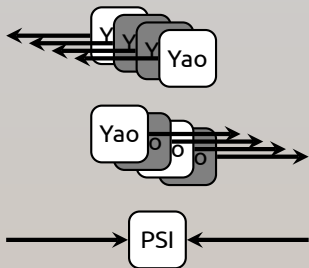
Two phases:

1.  $B$  circuits computing  $f(x, y)$
2.  $\sim 3B$  circuits computing:  
*“if Bob can prove Alice cheated in phase 1, then reveal  $x$  to Bob”*

# protocol comparison

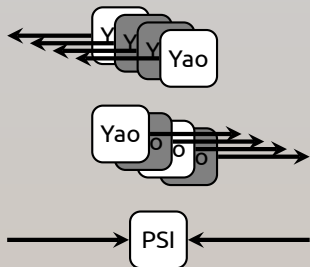
[KolesnikovMohasselRivaR15,RindalR16]:

[LindellRiva14/15]:

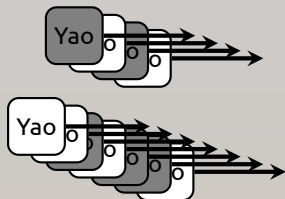


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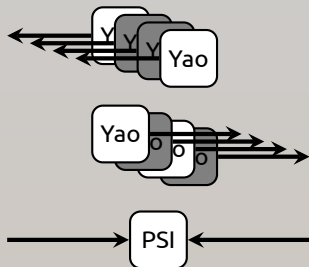


▶  $B$  primary circuits

- ▶  $B$  primary circuits in each direction (evaluated **simultaneously!**)

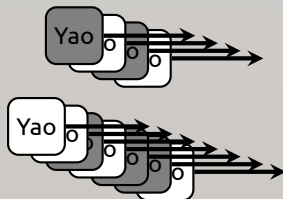
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[KolesnikovMohasselRivaR15,RindalR16]:



- ▶  $B$  primary circuits in each direction (evaluated **simultaneously!**)
- ▶ PSI computation scales only with  $B$

[LindellRiva14/15]:



- ▶  $B$  primary circuits
- ▶ Aux computation scales as  $3B \cdot \ell_{\text{input}}$

# a closer look at $\kappa$

$\kappa_C$ : Computational security parameter (e.g., 128)

$\kappa_S$ : Statistical security parameter: security properties violated with probability  $1/2^{\kappa_S}$  (e.g., 40)

“Traditional cut-and-choose” [LindellRiva14/15]:

- ▶ When cut-and-choose fails, adversary can completely break privacy & correctness
- ⇒ # of garbled circuits scales with  $\kappa_S$

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- ★  $\kappa_b$ : Bit-leaking parameter: privacy violated by a single bit (other security maintained) with probability  $1/2^{\kappa_b}$

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- $\kappa_s$ : Statistical security parameter: security properties violated with probability  $1/2^{\kappa_s}$  (e.g., 40)
- ★  $\kappa_b$ : Bit-leaking parameter: privacy violated by a single bit (other security maintained) with probability  $1/2^{\kappa_b}$

“Traditional cut-and-choose” [LindellRiva14/15]:

- ▶ When cut-and-choose fails, adversary can completely break privacy & correctness
- ⇒ # of garbled circuits scales with  $\kappa_s$

Dual-execution approach [KolesnikovMohasselRivaR15,RindalR16]:

- ▶ When cut-and-choose fails, adversary learns only a bit
- ⇒ # of garbled circuits scales with  $\kappa_b \leq \kappa_s$

# some parameter possibilities

[RindalR16] with  $\kappa_s = \kappa_b = 40$ :

- ▶ same security as [LindellRiva] with  $\kappa_s = 40$
- ▶ same # of garbled circuits



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[RindalR16] with  $\kappa_s = 40, \kappa_b = 30$ :

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- ▶ fewer garbled circuits (25% savings for  $N = 1024$ , 40% for  $N = 512$ )

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[RindalR16] with  $\kappa_s = 80, \kappa_b = 40$ :


- ▶ **strictly stronger** security than [LindellRiva] with  $\kappa_s = 40$
- ▶ same # of garbled circuits (only PSI cost increases)

# implementation

	[RindalR16]		[LindellRiva]		[DamgårdZakarias15]	
	offline	online	offline	online	offline	online
AES circuit	<b>5.1ms</b>	<b>1.3ms</b>	74ms	7ms	high?	6ms
SHA256 circuit	<b>48ms</b>	<b>8.4ms</b>	206ms	33ms	-	-

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Amortized cost over  $N = 1024$  executions:

- ▶ same hardware, LAN connection  
(Amazon c4.8xlarge = 36 core, 64GB RAM)
- ▶ same security ( $\kappa_s = \kappa_b = 40$ )

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Amortized cost over  $N = 1024$  executions:

- ▶ same hardware, LAN connection  
(Amazon c4.8xlarge = 36 core, 64GB RAM)
- ▶ same security ( $\kappa_s = \kappa_b = 40$ )

Maximum **throughput**: 0.26ms / AES block (3800+ Hz)

- ▶ [DamgårdZakarias15] reports 0.4ms

# summary

Online-offline dual execution:

- ▶ Fastest 2PC with malicious security to date: 1.3ms AES
- ▶ Some protocol advantages over “classic” cut-and-choose

Future work:

# summary

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Future work:

	garbled circ	info-theoretic
online latency	low ✓✓	low ✓
online throughput	high ✓	high ✓✓
constant rounds?	yes ✓	no ✗
offline time	low ✓	(very) high ✗
function-indep pre-processing?	no ✗	yes ✓

# summary

Online-offline dual execution:

- ▶ Fastest 2PC with malicious security to date: 1.3ms AES
- ▶ Some protocol advantages over “classic” cut-and-choose

Future work: Combine GC with info-theoretic? (at least for 2-party)

	garbled circ	info-theoretic	hybrid
online latency	low ✓✓	low ✓	low ✓
online throughput	high ✓	high ✓✓	high ✓✓
constant rounds?	yes ✓	no ✗	no ✗
offline time	low ✓	(very) high ✗	low ✓
function-indep pre-processing?	no ✗	yes ✓	yes ✓



*the end; thanks.*

***Richer Efficiency/Security Tradeoffs in 2PC***

Vladimir Kolesnikov, Payman Mohassel, Ben Riva & Mike Rosulek  
[ia.cr/2015/055](http://ia.cr/2015/055)

***Faster Malicious 2-party Secure Computation with Online/Offline Dual Execution***

Peter Rindal & Mike Rosulek  
in submission