

ECE 468: Digital Image Processing

Lecture 4

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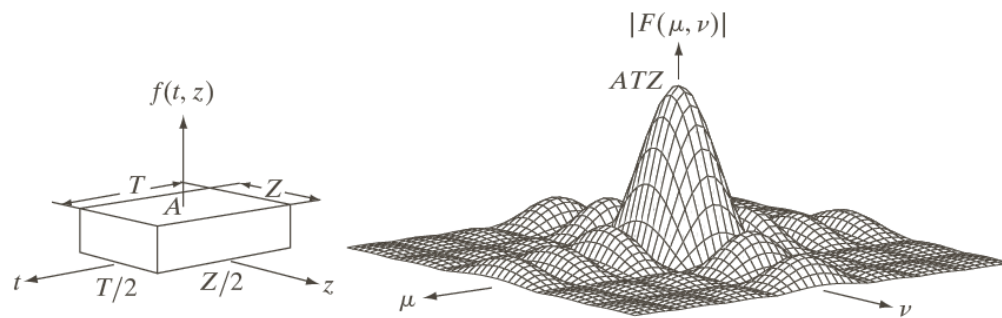
Disclaimer

The following slides are just excerpts
from the textbook.

You should learn all material presented
in chapter 4 in the textbook!

2

CFT of Rectangular Pulse



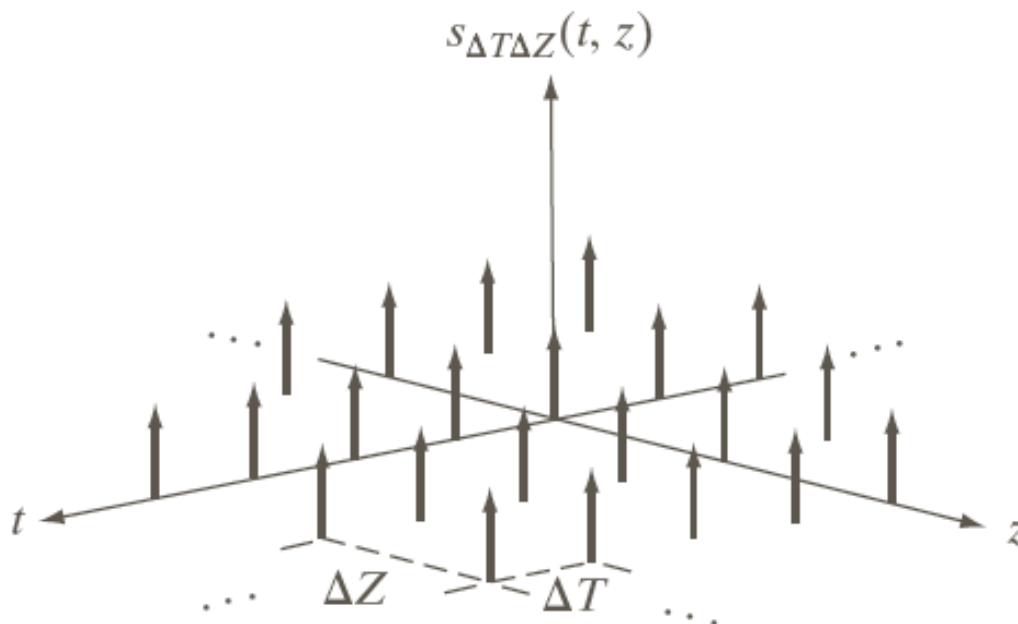
a b

FIGURE 4.13 (a) A 2-D function, and (b) a section of its spectrum (not to scale). The block is longer along the t -axis, so the spectrum is more “contracted” along the μ -axis. Compare with Fig. 4.4.

$$F(\mu, \nu) = ATZ \frac{\sin(\pi\mu T)}{\pi\mu T} \frac{\sin(\pi\nu T)}{\pi\nu T}$$

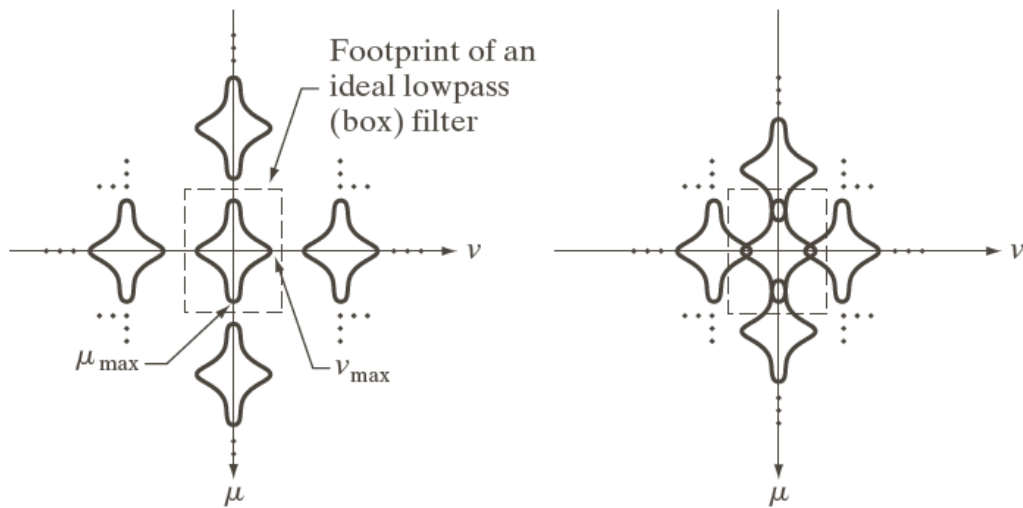
3

Sampling Theorem



4

Sampling Theorem



$$\bar{F}(\mu, \nu) = \frac{1}{TZ} \sum_{m=-\infty}^{\infty} \sum_{n=-\infty}^{\infty} F\left(\mu - \frac{m}{T}, \nu - \frac{n}{T}\right)$$

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Aliasing

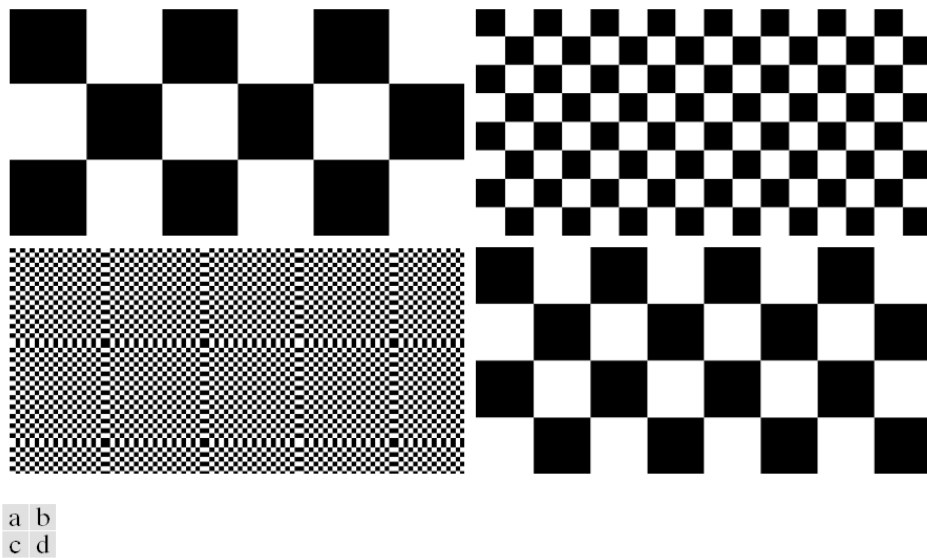


FIGURE 4.16 Aliasing in images. In (a) and (b), the lengths of the sides of the squares are 16 and 6 pixels, respectively, and aliasing is visually negligible. In (c) and (d), the sides of the squares are 0.9174 and 0.4798 pixels, respectively, and the results show significant aliasing. Note that (d) masquerades as a “normal” image.

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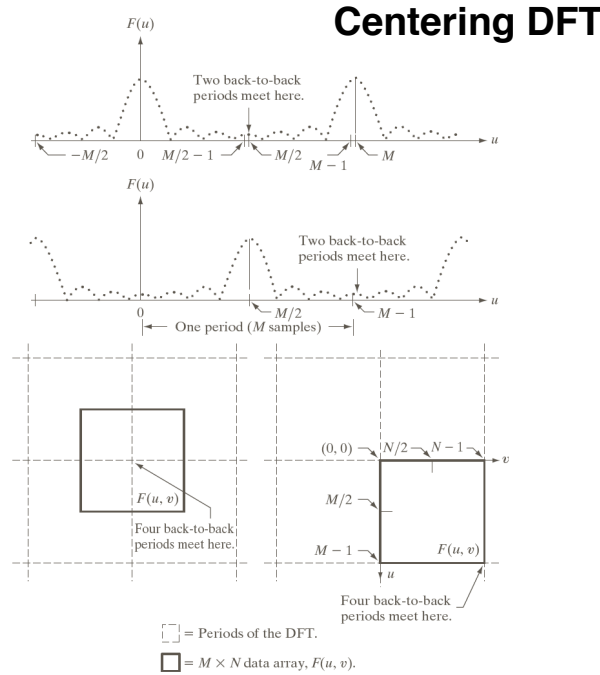
Aliasing Due to Subsampling



a b c

FIGURE 4.17 Illustration of aliasing on resampled images. (a) A digital image with negligible visual aliasing. (b) Result of resizing the image to 50% of its original size by pixel deletion. Aliasing is clearly visible. (c) Result of blurring the image in (a) with a 3×3 averaging filter prior to resizing. The image is slightly more blurred than (b), but aliasing is not longer objectionable. (Original image courtesy of the Signal Compression Laboratory, University of California, Santa Barbara.)

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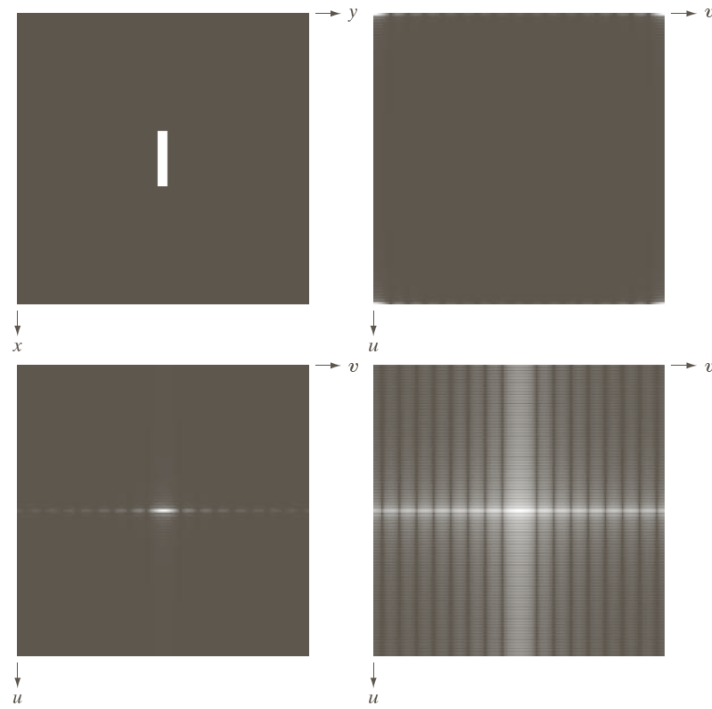
$$f(x, y)(-1)^{x+y} \rightarrow F\left(u - \frac{M}{2}, v - \frac{N}{2}\right)$$

a
b
c d

FIGURE 4.23 Centering the Fourier transform. (a) A 1-D DFT showing an infinite number of periods. (b) Shifted DFT obtained by multiplying $f(x)$ by $(-1)^x$ before computing $F(u)$. (c) A 2-D DFT showing an infinite number of periods. The solid area is the $M \times N$ data array, $F(u, v)$, obtained with Eq. (4.5-15). This array consists of four quarter periods. (d) A Shifted DFT obtained by multiplying $f(x, y)$ by $(-1)^{x+y}$ before computing $F(u, v)$. The data now contains one complete, centered period, as in (b).

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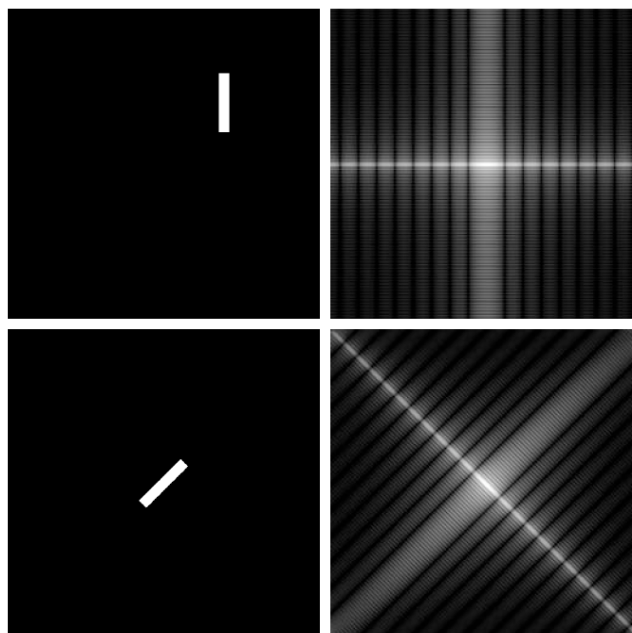
Example



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Translation in Space $\rightarrow$ No change in Spectrum

Rotation in Space $\rightarrow$ Rotation in Spectrum



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Example

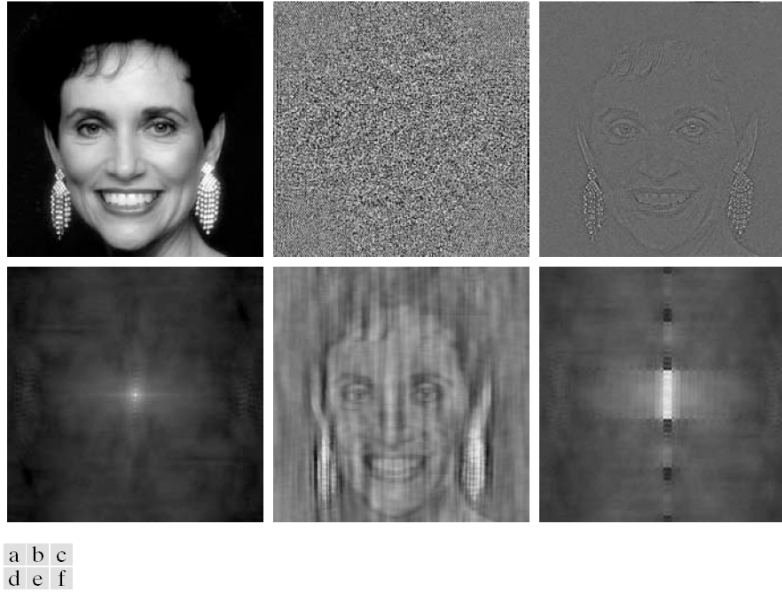


FIGURE 4.27 (a) Woman. (b) Phase angle. (c) Woman reconstructed using only the phase angle. (d) Woman reconstructed using only the spectrum. (e) Reconstruction using the phase angle corresponding to the woman and the spectrum corresponding to the rectangle in Fig. 4.24(a). (f) Reconstruction using the phase of the rectangle and the spectrum of the woman.

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Circular Convolution

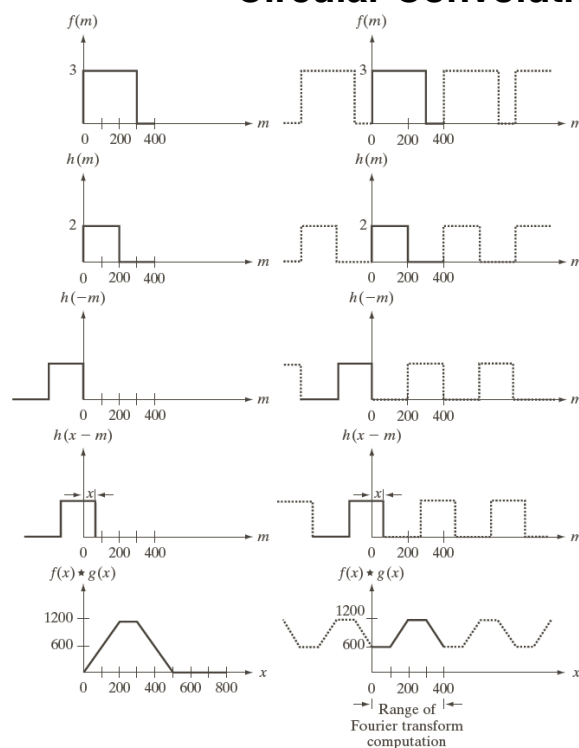


FIGURE 4.28 Left column: convolution of two discrete functions obtained using the approach discussed in Section 3.4.2. The result in (e) is correct. Right column: Convolution of the same functions, but taking into account the periodicity implied by the DFT. Note in (j) how data from adjacent periods produce wraparound error, yielding an incorrect convolution result. To obtain the correct result, function padding must be used.

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