Principal Curvature-Based Region Detector for Object Recognition

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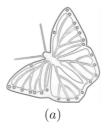
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Abstract

This paper presents a new structure-based interest region detector called Principal Curvature-Based Regions (PCBR) which we use for object class recognition. The PCBR interest operator detects stable watershed regions within the multi-scale principal curvature image. To detect robust watershed regions, we "clean" a principal curvature image using a combination of grayscale morphological closing and a new "eigenvector flow" hysteresis thresholding. Robustness across scales is achieved by selecting the maximal stable regions across consecutive scales. PCBR typically detects distinctive patterns distributed evenly on the objects and it shows significant robustness to local intensity perturbations and intra-class variations. We evaluate PCBR both qualitatively (through visual inspection) and quantitatively (by measuring repeatability and classification accuracy in real-world object-class recognition problems). Experiments on different benchmark datasets show that PCBR is comparable or superior to state-of-art detectors for both feature matching and object recognition problems. Moreover, we demonstrate the application of PCBR to symmetry detection.

1. Introduction

In many object recognition tasks, within-class changes in pose, lighting, color, and texture can cause considerable variation in local intensities. Consequently, local intensity no longer provides a stable detection cue. As such, intensity-based interest operators (e.g., Harris, Kadir)—and the object recognition systems based on them (e.g., Opelts [1])—often fail to identify discriminative features. An alternative to local intensity cues is to capture semi-local structural cues such as edges and curvilinear shapes [23]. These structural cues tend to be more robust to intensity, color, and pose variations. As such, they provide the basis for a more stable interest operator, which in turn improves object recognition accuracy. In this paper, we introduce a new detector that exploits curvilinear structures to reliably de-



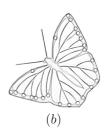


Figure 1. Comparison of the gradient magnitude and principal curvature responses of the image in Figure 2(a). (a) Gradient magnitude response. (b) Principal curvature response.

tect interesting regions. The detector, called the Principal Curvature-Based Region (PCBR) detector, identifies stable watershed regions within the multi-scale principal curvature image.

Curvilinear structures are lines (either curved or straight) such as roads in aerial or satellite images or blood vessels in medical scans. They provide a kind of sketch of the objects appearing in images. These curvilinear structures can be detected over a range of viewpoints, scales, and illumination changes. The PCBR detector employs the first steps of Steger's curvilinear detector algorithm [23]. It computes the eigenvalues of the Hessian matrix at each pixel and then forms an image that is composed of one of the two eigenvalues. We call this the principal curvature image, as it approximates the principal curvature of the image intensity surface. This process generates a single response for both lines and edges, producing a clearer structural sketch of an image than is usually provided by the gradient magnitude image (see Fig. 1).

We develop a process that detects structural regions efficiently and robustly using the watershed transform of the principal curvature image across scale space. The watershed algorithm provides a more efficient mechanism for defining structural regions than previous methods of fitting circles, ellipses, and parallelograms [10, 26]. However, the watershed algorithm is sensitive to noise and other small image perturbations. To improve robustness to noise, we "clean" the principal curvature image with a grayscale mor-

phological close operation followed by a new hysteresis thresholding method based on local eigenvector flow. The watershed transform is then applied to the cleaned principal curvature image and the resulting watershed regions (i.e., the catchment basins) define the PCBR regions. To achieve robust detections across multiple scales, the watershed is applied to the maxima of three consecutive images in the principal curvature scale space–similar to local scale-space extrema used by Lowe [14], Mikolajczyk and Schmidt [17], and others–and we further search for stable PCBR regions across consecutive scales–an idea adapted from the stable regions detected across multiple threshold levels used by the MSER detector [16].

This work makes two contributions. First, we develop a new interest operator that utilizes principal curvature to extract robust and invariant region structures based on both edge and curvilinear features. Second, we introduce an enhanced principle-curvature-based watershed segmentation and robust region selection process that is robust to intra-class variations and is more efficient than previous structure-based detectors. We demonstrate the value of our PCBR detector by applying it to object-class recognition problems and symmetry detection.

2. Related Work

Interest operators can typically be classified into two categories: intensity-based detectors and structure-based detectors [19]. Intensity-based detectors depend on analyzing local differential geometry or intensity patterns to find points or regions that satisfy some uniqueness and stability criteria. The Harris corner detector [7] finds points or pixels where both eigenvalues of the second moment matrix are large by evaluating the simple-to-computer "Harris measure". The Harris-affine and Hessian-affine detectors [17, 18] compute maximum determinants of the second moment matrix and the Hessian matrix respectively across scale space and then apply Laplacian-based characteristic scale selection [12] and second-moment-matrixbased shape adaptation [13, 2]. MSER [16] uses a threshold selection process to detect stable regions that are either brighter or darker than the surrounding region. SIFT (i.e., the DoG extrema detector used by Lowe in [14]) finds local extrema across three consecutive difference-of-Gaussian scales and then removes spurious detections via a DoGresponse threshold followed by a Harris-like metric to eliminate edge detections. Kadir's salient region detector [24] calculates the entropy of the probability density function (PDF) of intensity values over the scale and ellipse parameter spaces to find regions with entropy extrema. Other intensity-based detectors include SUSAN [22], intensity extrema-based regions (IBR) [25], and the work of Moravec [9] and Beaudet [3].

Structure-based detectors depend on structural image

features such as lines, edges, curves, etc. to define interest points or regions. These detectors tend to be very computationally expensive and typically depend on reliable prior detection of structural features. Early structure-based detectors analyzed various 2D curves such as the curvature primal sketch or B-splines extracted from edges, ridges, troughs, etc. and then selected high curvature points, line or curve intersections, corners, ends, bumps, and dents as interest points [8, 6, 20, 21, 5]. Tuytelaar's edge-based region (EBR) detector [26] fits a parallelogram defined by Harris corner point and points on two adjacent edge contours (extracted by the Canny detector [4]). Scale-invariant shape features (SISF) [10] detects circles at different locations and scales by evaluating salient convex arrangements of Canny edges based on a measure that maximizes how well a circle is supported by surrounding edges.

3. Principal curvature-based Region Detector

3.1. Principal Curvature Image

There are two types of structures that have high curvature in one direction and low curvature in the orthogonal direction: lines (i.e., straight or nearly straight curvilinear features) and edges. Viewing an image as an intensity surface, the curvilinear structures correspond to ridges and valleys of this surface. The local shape characteristics of the surface at a particular point can be described by the Hessian matrix,

$$\mathbf{H}(\mathbf{x}, \sigma_D) = \begin{bmatrix} I_{xx}(\mathbf{x}, \sigma_D) & I_{xy}(\mathbf{x}, \sigma_D) \\ I_{xy}(\mathbf{x}, \sigma_D) & I_{yy}(\mathbf{x}, \sigma_D) \end{bmatrix}, \quad (1)$$

where I_{xx} , I_{xy} and I_{yy} are the second-order partial derivatives of the image evaluated at the point \mathbf{x} and σ_D is the Gaussian scale at which the second partial derivatives are computed.

We note that both the Hessian matrix and the related second moment matrix have been applied in several other interest operators (e.g., the Harris [7], Harris-affine [19], and Hessian-affine [18] detectors) to find image positions where the local image geometry is changing in more than one direction. Likewise, Lowe's maximal difference-of-Gaussian (DoG) detector [14] also uses components of the Hessian matrix (or at least approximates the sum of the diagonal elements) to find points of interest. However, our PCBR detector is quite different from these other methods and is complementary to them. Rather than finding extreme "points", our detector applies the watershed algorithm to ridges, valleys, and cliffs of the image intensity surface to find "regions". Just like extreme points, the ridges, valleys, and cliffs can be detected over a range of viewpoints, scales, and appearance changes.

Many of the interest point detectors mentioned previously [7, 19, 18] apply the Harris measure (or a similar met-

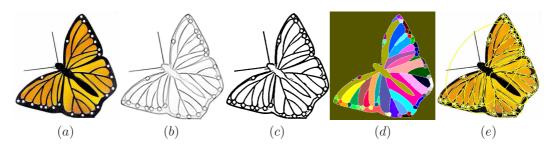


Figure 2. Interest Regions detected by the PCBR detector. (a) Original butterfly image. (b) Principal curvature and (c) cleaned binary images. (d) Watershed regions. (e) Detected regions represented by ellipses.

ric [14]) to determine a point's saliency. The Harris measure is given by $det(\mathbf{A}) - k \cdot tr^2(\mathbf{A}) > threshold$ where det is the determinant, tr is the trace, and the matrix \mathbf{A} is either the Hessian matrix or the second moment matrix. The Harris measure penalizes (i.e., produces low values for) "long" structures for which the first or second derivative in one particular orientation is very small. One advantage of the Harris metric is that it does not require explicit computation of the eigenvalue or eigenvectors. However, computing the eigenvalues and eigenvectors for a 2×2 matrix requires only a single Jacobi rotation to eliminate the off-diagonal term, I_{xy} , as noted by Steger [23].

Our PCBR detector complements the previous interest point detectors in that we abandon the Harris measure and exploit those very long structures as detection cues. The principal curvature image is given by either

$$P(\mathbf{x}) = \max(\lambda_1(\mathbf{x}), 0) \tag{2}$$

or

$$P(\mathbf{x}) = \min(\lambda_2(\mathbf{x}), 0) \tag{3}$$

where $\lambda_1(\mathbf{x})$ and $\lambda_2(\mathbf{x})$ are the maximum and minimum eigenvalues, respectively, of H at \mathbf{x} . Eq. 2 provides a high response only for dark lines on a light background (or on the dark side of edges) while Eq. 3 is used to detect light lines against a darker background.

Principal curvature images are calculated in scale space in a fashion similar to that of SIFT [14]. We first double the size of the original image to produce our initial image, I_{11} , and then produce increasingly Gaussian smoothed images, I_{1j} , with scales of $\sigma=k^{j-1}$ where $k=2^{1/3}$ and j=2..6. This set of images spans the first octave consisting of 6 images, I_{11} to I_{16} . Image I_{14} is downsampled to half its size to produce image I_{21} , which becomes the first image in the second octave. We apply the same smoothing process to build the second octave, and continue to create a total of n=log2(min(w,h))-3 octaves, where w and h are the width and height of the doubled image, respectively. Finally, we calculate a principal curvature image, P_{ij} , for each smoothed image by computing the maximum eigenvalue (Eq. 2) of the second derivative Hessian matrix at

each pixel. For computational efficiency, each smoothed image and its corresponding Hessian image is computed from the previous smoothed image using an incremental Gaussian scale.

Given the principal curvature scale space images, we calculate the maximum curvature over every three consecutive principal curvature images to form the following set of four images in each of the n octaves:

where $MP_{ij} = \max(P_{ij-1}, P_{ij}, P_{ij+1})$.

Figure 2(b) shows one of the maximum curvature images, MP, created by maximizing the principal curvature at each pixel over three consecutive principal curvature images. From these maximum principal curvature images we find the stable regions via our watershed algorithm.

3.2. Enhanced Watershed Regions Detections

The watershed transform is an efficient technique that is widely employed for image segmentation. It is normally applied either to an intensity image directly or to the gradient magnitude of an image. We instead apply the watershed transform to the principal curvature image. However, the watershed transform is sensitive to noise (and other small perturbations) in the intensity image. A consequence of this is that the small image variations form local minima that result in many, small watershed regions. Figure 3(a) shows the oversegmentation results when the watershed algorithm is applied directly to the principal curvature image in Figure 2(b)). To achieve a more stable watershed segmentation, we first apply a grayscale morphological closing followed by hysteresis thresholding. The grayscale morphological closing operation is defined as $f \bullet b = (f \oplus b) \ominus b$ where f is the image MP from Eq. 4, b is a disk-shaped structuring element, and \oplus and \ominus are the grayscale dilation and erosion, respectively. The closing operation removes small "potholes" in the principal curvature terrain, thus eliminating many local minima that result from noise and that would otherwise produce watershed catchment basins.

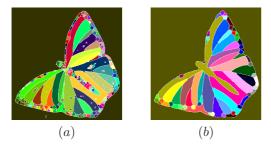


Figure 3. (a) Watershed segmentation of original principal curvature image (Fig. 2b). (b) Watershed segmentation of the "clean" principal curvature image (Fig. 2c).

However, beyond the small (in terms of area of influence) local minima, there are other variations that have larger zones of influence and that are not reclaimed by the morphological closing. To further eliminate spurious or unstable watershed regions, we threshold the principal curvature image to create a clean, binarized principal curvature image. However, rather than apply a straight threshold or even hysteresis thresholding-both of which can still miss weak image structures-we apply a more robust eigenvector-guided hysteresis thresholding to help link structural cues and remove perturbations. Since the eigenvalues of the Hessian matrix are directly related to the signal strength (i.e., the line or edge contrast), the principal curvature image may, at times, become weak due to low contrast portions of an edge or curvilinear structure. These low contrast segments may potentially cause gaps in the thresholded principal curvature image, which in turn cause watershed regions to merge that should otherwise be seperate. However, the directions of the eigenvectors provide a strong indication of where curvilinear structures appear and they are more robust to these intensity pertubations than is the eigenvalue magnitude.

In eigenvector-flow hysteresis thresholding, there are two thresholds (high and low) just as in traditional hysteresis thresholding. For this application, we have set the high threshold at 0.04 to indicate a strong principal curvature response. Pixels with a strong response act as seeds that expand out to include connected pixels that are above the low threshold. Unlike traditional hysteresis thresholding, our low threshold is a function of the support that each pixel's major eigenvector receives from neighboring pixels. The low threshold is set on every pixel by comparing the direction of the major (or minor) eigenvector to the direction of the adjacent pixels' major (or minor) eigenvectors. This can be done by taking the absolute value of the inner product of a pixel's normalized eigenvector with that of each neighbor. If the average dot product over all neighbors is high enough, we set the low-to-high threshold ratio to 0.2 (for a low threshold of $0.04 \cdot 0.2 = 0.008$); otherwise the lowto-high ratio is set to 0.7 (giving a low threshold of 0.028). These ratios were chosen based on experiments with hundreds of images.

Figure 4 illustrates how the eigenvector flow supports an otherwise weak region. The red arrows are the major eigenvectors, and the yellow arrows are the minor eigenvectors. To improve visibility, we draw them at every fourth pixel. At the point indicated by the large white arrow, we see that the eigenvalue magnitudes are small and the ridge there is almost invisible. Nonetheless, the directions of the eigenvectors are quite uniform. This eigenvector-based active thresholding process yields better performance in building continuous ridges and in handling perturbations, which results in more stable regions (Fig. 3(b)).

The final step is to perform the watershed transform on the clean binary image (Fig. 2(c)). Since the image is binary, all black (or 0-valued) pixels become catchment basins and the midlines of the thresholded white ridge pixels become watershed lines if they separate two distinct catchment basins. To define the interest regions of the PCBR detector in one scale, the resulting segmented regions are fit with ellipses, via PCA, that have the same second-moment as the watershed regions (Fig. 2(e)).

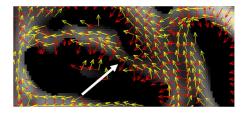


Figure 4. Illustration of how the eigenvector flow helps overcome weak principal curvature responses.

3.3. Stable Regions over Scales

Choosing maximum principal curvature images is only one way to achieve stable region detections. To improve robustness further, we adopt a key idea from MSER and keep only those regions that can be detected in at least three consecutive scales. In a method similar to the process of selecting stable regions via thresholding in MESR, we select regions that are stable across local scale changes. To achieve this, we compute the overlap error of the detected regions across each triplet of consecutive scales in every octave. The overlap error is calculated the same as in [19].

Overlapping regions that are detected at different scales normally exhibit some variation. This kind of variation is valuable for object recognition because it provides multiple descriptions of the same pattern. An object category normally exhibits large within-class variation even in the same area. Since detectors usually have difficulty in locating the interest area accurately, rather than attempt to find a single

region and extract a single descriptor vector, it is better to identify multiple overlapping regions and extract multiple descriptor vectors, provided that these multiple vectors can be handled properly by the classifier.

To determine a threshold value for the permitted amount of overlap, we analyze the sensitivity of the SIFT descriptor. Three transformations (translations from 1 to 10 pixels, rotations from 2 to 20 degrees and minor axis enlargements from 1 to 10 pixels) are applied on all detected regions in the Inria dataset [19]. Overlap errors and similarities of SIFT descriptors between the transformed regions and the originals are calculated. To keep regions that can be detected over local scales, only regions with overlap error less than 30% are chosen. However, as indicated in Figure 5, SIFT similarity decreases to 70% for regions that have an overlap error of 30%. As such, we keep all stable regions with an overlap error greater than 30% to maintain more descriptions for similar regions. We also notice that the similarity of the SIFT descriptors is above 90% when overlap error is less than 10%. These very similar regions are merged into a single region.

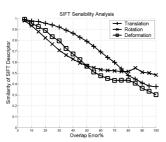


Figure 5. Sensitivity analysis of SIFT descriptor.

4. Evaluation and Discussion

We evaluate our PCBR detector in three ways: 1) qualitative visual inspection, 2) quantitative repeatability using a published framework [19], and 3) quantitative and qualitative evaluation using real world applications.

4.1. Visual Inspection

To provide a visual evaluation of PCBR, Figures 6 and 7 show PCBR detection results on a variety of different types of images. Fig. 6 shows PCBR detections on two graffiti images from the INRIA dataset [19] while Fig. 7 shows detection results for face, motorbike, and cars (rear) images from the Caltech dataset. In Figure 7, we remove background detections to improve visibility. From these images we note that PCBR detections appear to be evenly distributed, highly consistent, and robust to intra-class variations.





Figure 6. PCBR detections on the first and second graffiti images from the INRIA dataset [19].

Detectors	Motorbikes	Airplanes	Faces	Cars(Side)
PCBR	87.7	91.7	97.7	87
HL & HA	92.2	88.9	93.5	83

Table 1. Comparison of PCBR with the combination of Harris-Laplace and Harris-affine detectors on the Caltech dataset using Opelt's object-class recognition method [1].

4.2. Repeatability

Although the PCBR detector was designed for object-class recognition rather than repeatable wide-baseline feature matching, we still evaluate its repeatability and compare it to other detectors using the INRIA dataset and evaluation code [19]. The relative ranks of the PCBR detector compared to various other detectors are listed in Table 2. Ranks are determined from the repeatability vs. transformation curves as output by the INRIA evaluation code (with the overlap error parameter set to 20%). A rank of 1 represents the highest repeatability while 7 represents the lowest repeatability. From Table 2 we can see that PCBR is comparable to other detectors in terms of repeatability.

4.3. Applications

To quantitatively evaluate the PCBR detector on object recognition tasks, we have conducted two recognition tasks using the Caltech dataset and a database of larval stonefly images. To build a recognition system, we build SIFT descriptors for each detected (and normalized) region and then apply recent state-of-the-art object-class recognition algorithms to perform the final classification. We then measure classification accuracy using the PCBR detector and compare it to the accuracy using other interest operators.

4.3.1 Object Recognition on Caltech Dataset

The Caltech dataset contains images from many different object classes. In this experiment, we measure recognition accuracy on four commonly-used object classes (motorbikes, airplanes, faces, and cars) using Opelt's object-class recognition algorithm [1]. We use Opelt's Matlab code (adapted to use the PCBR detector) with all the default parameter settings (see [1]) with the only variation being

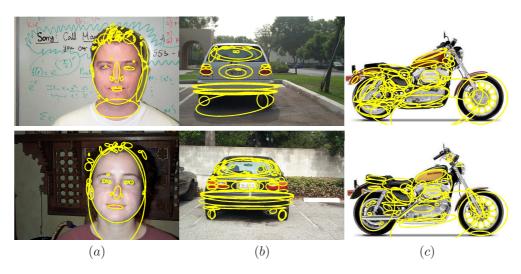


Figure 7. PCBR detections on faces, cars (rear), and motorbikes from the Caltech dataset.

Images	PCBR	Hessian-affine	Harris-Affine	MSER	IBR	EBR	Salient
Bikes	5	1	3	4	6	2	7
Trees	3	1	4	2	5	6	7
Boats	5	1	3	2	6	4	7
Leuven (cars)	3	2	4	1	5	6	7
Graffiti	2	5	6	1	3	4	7
Walls	4	2	3	1	5	6	7

Table 2. Repeatability ranking (1 is the best, 7 is the worst) for PCBR and various other detectors on the INRIA dataset [19].

that we use PCBR instead of the Harris-Laplace and Harris-affine detectors. The recognition performance is evaluated using ROC equal error rates. Table 1 compares recognition accuracy using PCBR with those reported by Opelt in [1] (using Harris-Laplace and Harris-affine detectors). We see from Table 1 that the PCBR detector produces higher recognition accuracy than the combination of Harris detectors on three of the four object-class datasets.

4.3.2 Object Recognition on Stonefly Dataset

Population counts of larval stoneflies inhabiting stream substrates are known to be a sensitive and robust indicator of stream health and water quality. Consequently, automated classification of stonefly larva can make great strides in overcoming current bottlenecks—such as the considerable time and technical expertise required—to large scale implementation of this important biomonitoring task. As such, we evaluate the effectiveness of our PCBR detector on a more fine-grained object-class recognition problem, that of distinguishing between two related species of stonefly larva, *Calineuria californica* and *Doroneuria baumanni*. These two stonefly species are from the same taxonomic family and, as such, are very similar in appearance. Indeed, this problem is challenging even for humans and is akin to vi-

sually distinguishing between nearly identical car models. As such, this problem is more difficult than differentiating between faces and airplanes as per the Caltech dataset.

Figure 8 (a-b) shows four specimens images (and their relative sizes) from each of the two taxa. To verify the difficulty of discriminating these two taxa, we conducted an informal study to test the human classification accuracy of *Calineuria* and *Doroneuria*. A total of 26 students and faculty were trained on 50 randomly-selected images of *Calineuria* and *Doroneuria*, and were subsequently tested with another 50 images. Most of the subjects (21) had some prior entomological experience. The mean human classification accuracy is 78.6% correctly identified (std. dev. = 8.4).

We compare PCBR with the Kadir salient region detector and the Hessian-affine detector on the stonefly recognition problem. All classification settings are identical except for the detector. For this comparison, we use the Hessian-affine and salient region detectors available on the web (http://www.robots.ox.ac.uk/~vgg/research/affine/). Figure 9 shows the detections for the four *Calinueria* images in Fig. 8(a). Notice again how well distributed and consistent the PCBR detections.

We apply two state-of-the-art object-class recognition algorithms to the stonefly dataset: logistic model trees (LMT) by Landwehr *et al.* [11] and Opelt's method [1]. We use

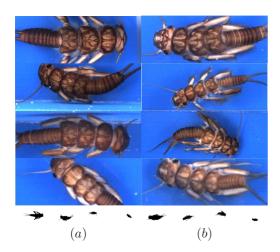


Figure 8. Visual comparison of *Calinueria* and *Doroneuria* and their relative specimen sizes. (a) Four different *Calinueria* and (b) *Doroneuria* specimens.

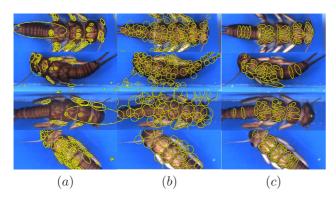


Figure 9. Comparison of three detectors on *Calinueria* images. (a) Hessian-affine, (b) Kadir salient regions, and (c) PCBR

Taxon	Specimens	Images	
Calineuria	85	400	
Doroneuria	91	463	

Table 3. Specimens and images employed in the study.

our own LMT implementation and, as before, use Opelt's Matlab code (adapted to use other detectors). The number of specimens and images used in this experiment is listed in Table 3 while Table 4 summarizes the classification accuracy for this two-class recognition problem. As can be seen, both classifiers yield better recognition accuracy with the PCBR detector than with the other two detectors.

4.3.3 Symmetry Detection

Symmetry is quite common in biological and artificial objects. Since our PCBR detector detects robust structure-based interest regions, it is good at detecting symmetrical regions in images containing objects with bilateral symme-

Hessian	Kadir		Accuracy[%]		
Affine	Entropy	PCBR	Opelt [1]	LMTs [11]	
			60.59	70.10	
			62.63	70.34	
			67.86	79.03	

Table 4. *Calineuria* and *Doroneuria* classification rates comparison of different detectors when applied with Opelt's method and LMTs. A $\sqrt{}$ indicates that the corresponding detector is used.

try. To demonstrate this, we combine the PCBR detector with (our implementation of) the SIFT-based symmetry detection method of Loy and Eklundh [15] and test it on various images. Figure 10 shows the symmetrical detections is several images. We can see that the detected symmetry regions are quite accurate and distinctive, so provide valuable cue for the detection and recognition of the symmetrical objects.

We also apply symmetry detection to choose good dorsal (or back side) views of stonefly larvae from among the various poses. Dorsal views exhibit more bilateral symmetry than do other poses. As such, symmetry detection is a useful mechanism for identifying those images that are best for classification. Figure 11 shows various poses of the stoneflies as contained in the database. Figure 12 shows the four selected dorsal views with symmetrical PCBR detections on them. The PCBR detector is better at finding bilaterally-symmetric regions in the stonefly images than are other detectors.



Figure 11. Different object poses in the stonefly database.



Figure 12. Good dorsal views selected using bilateral symmetry detection with PCBR.



Figure 10. Bilateral symmetry detection using PCBR.

5. Conclusion and Future Work

This paper has presented a new structure-based interest region detector called Principal Curvature-Based Regions (PCBR) and has demonstrated its successful application to several tasks. The PCBR interest operator detects stable watershed regions within the multi-scale principal curvature image that describes both edge and curvilinear structures. Grayscale morphology and a new eigenvector-flow hysteresis thresholding provide for robust watershed detections. Further, robustness across multiples scales is acheived by selecting the maximal stable regions across consecutive scales. Finally, we have demonstrated the utility of our PCBR detector to reliable wide-baseline feature detection, object-class recognition, and symmetry detection.

Unlike detectors designed for wide-baseline matching of rigid static scenes, detectors for object recognition should be more intelligent in identifying object-class-relevant regions. As such, a future direction for this work is to develop discriminative interest operators and region descriptors that learn to detect and describe characteristic regions on a per object-class basis.

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