

# Types

# Outline

## Introduction

- Concepts and terminology
- The case for static typing

## Implementing a static type system

- Basic typing relations
- Adding context

# What is a type?

## Static types

A set of **syntactic terms (ASTs)** that share the same behavior

## Dynamic types

A set of **runtime values** that share the same behavior

Types define an **interface** for terms/values:

- what operations can be applied to them?
- in what contexts can they appear?

Examples in Haskell: **Int**, **Bool**, **String**, **Maybe Bool**, **[[Int]]**, **Int -> Bool**

# Type errors

## Static typing

Occurs **during type checking** when a term cannot be assigned a type

## Dynamic typing

Occurs **at runtime** when a value cannot be created, or when an invalid operation is applied to a value

Causes of type errors:

- undefined variables
- violation of the type interface (e.g. invalid operations)

If type errors are not caught/prevented, the program will either crash or do something unpredictable!

# Type safety

A **type system** detects and prevents/reports type errors

A language is **type safe** if an implementation can detect all type errors

- **statically**: by proving the absence of type errors
- **dynamically**: by detecting and reporting all type errors at runtime

## Type safe languages

- Haskell, SML      *static*
- Python, Ruby      *dynamic*
- Java, Go      *mixed*

## Unsafe languages

- C, C++      *pointers*
- PHP, Perl, JavaScript      *conversions*

## Implicit type conversions: strong vs. weak typing

Many languages **implicitly convert** between types – is this safe?

Only if it's determined by the **types**, *not* the runtime values!

Java (safe)

```
int n = 42;  
String s = "Answer: " + n;
```

PHP, Perl (unsafe)

```
n = "4" + 2;  
s = "Answer: " + n
```

Fun diabolical example: <http://www.jsfuck.com/>  
[programming with implicit conversions!](#)

# Static vs. dynamic typing

## Static typing

- types are associated with **syntactic terms** (ASTs)
- type errors are reported at **compile time** (and typically prevent execution)
- type checker **proves** that no type errors will occur at runtime

## Dynamic typing

- types are associated with **runtime values**
- type errors are reported at **runtime** (e.g. by throwing an exception)
- type checker is **integrated** into the runtime system

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# Benefits of static typing

## Usability and comprehension

1. **machine-checked documentation**
  - guaranteed to be correct and consistent with implementation
2. **better tool support**
  - e.g. code completion, navigation
3. **supports high-level reasoning**
  - by providing named abstractions for shared behavior

# Benefits of static typing (continued)

## Correctness

4. **a partial correctness proof** – no runtime type errors
  - improves robustness, focus testing on more interesting errors

## Efficiency

5. **improved code generation**
  - can apply type-specific optimizations
6. **type erasure**
  - no need for type information or checking at runtime

## Drawback: static typing is conservative

Q: What is the type of this expression?

```
if 3 > 4 then True else 5
```

A: Static typing: **type error**

Dynamic typing: **Int**

Q: What is the type of this one?

```
\x -> if x > 4 then True else x+2
```

A: Static typing: **type error**

Dynamic typing: **???**

Silly examples, but ...

- many advanced type features created to “reclaim” expressiveness

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# Static typing is a “static semantics”

## Dynamic semantics (a.k.a. execution semantics)

- *what is the meaning of this program?*
- relates an AST to a **value** (denotational semantics)
- describes meaning of program **at runtime**

**sem** :: Exp -> Value

## Static semantics

- *which programs have meaning?*
- relates an AST to a **type**
- describes meaning of program **at compile time**

**typeOf** :: Exp -> Type

Typing is just a semantics with a different semantic domain

# Defining a static type system

1. Define the **abstract syntax**,  $E$   
*the set of abstract syntax trees*
2. Define the structure of **types**,  $T$   
*another abstract syntax*
3. Define the **typing relation**,  $E : T$   
*the mapping from ASTs to types*

Example encoding in Haskell:

```
data Exp = ...
```

```
data Type = ...
```

```
typeOf :: Exp -> Type
```

Then, we can define a dynamic semantics that **assumes** there are no type errors

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# Typing contexts

Often we need to keep track of some information during typing

- types of top-level functions
- types of local variables
- an implicit program stack
- set of declared classes and their methods
- ...

Put this information in the **typing context** (a.k.a. the **environment**)

```
typeOf :: Exp -> Env -> Type
```